

Ensemble Filters for Data Assimilation: Flexible, Powerful, and Ready for Prime-Time?

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Ensemble filters are:

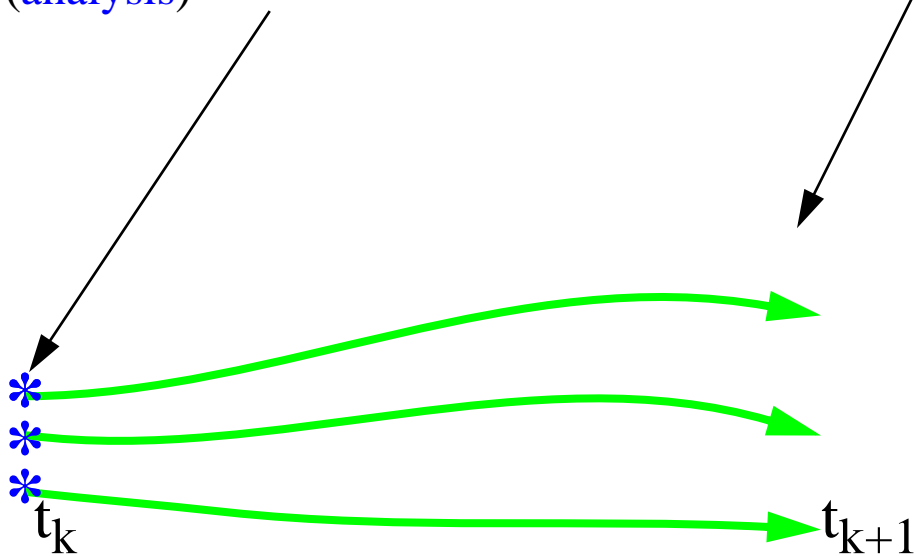
1. Easy to apply to complicated models and observations
2. Computationally competitive with variational methods
3. Able to extract information about all state variables using multivariate relations
4. Can be augmented to deal with model bias and nasty real observations

How an Ensemble Filter Works

1. Use model to advance **ensemble** (3 members here) to time at which next observation becomes available

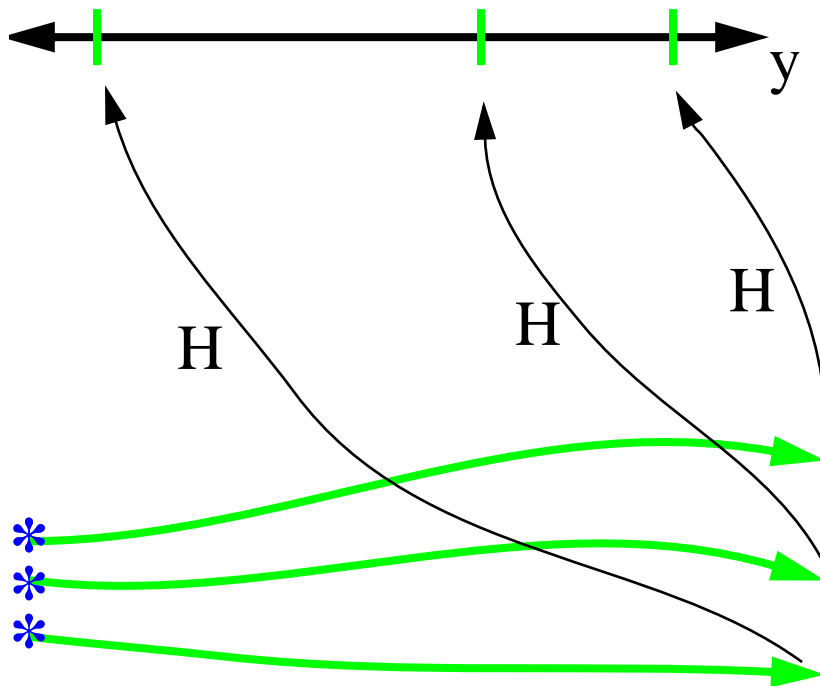
Ensemble state
estimate after using
previous observation
(analysis)

Ensemble state at time
of next observation
(prior)



How an Ensemble Filter Works

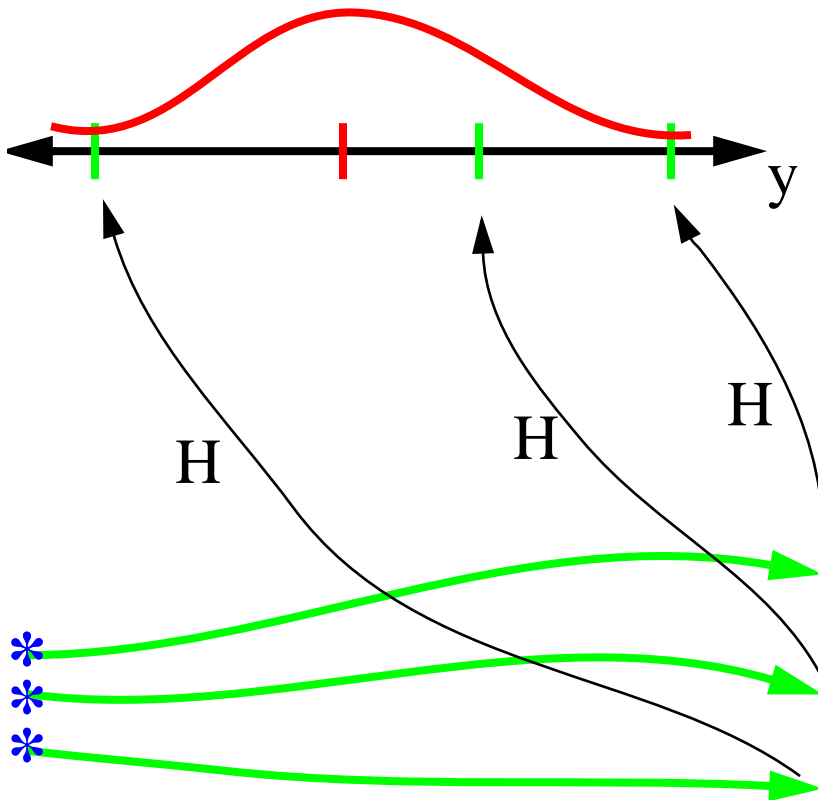
2. Get prior ensemble sample of observation, $y=H(x)$, by applying forward operator H to each ensemble member



Theory: observations from instruments with uncorrelated errors can be done sequentially.

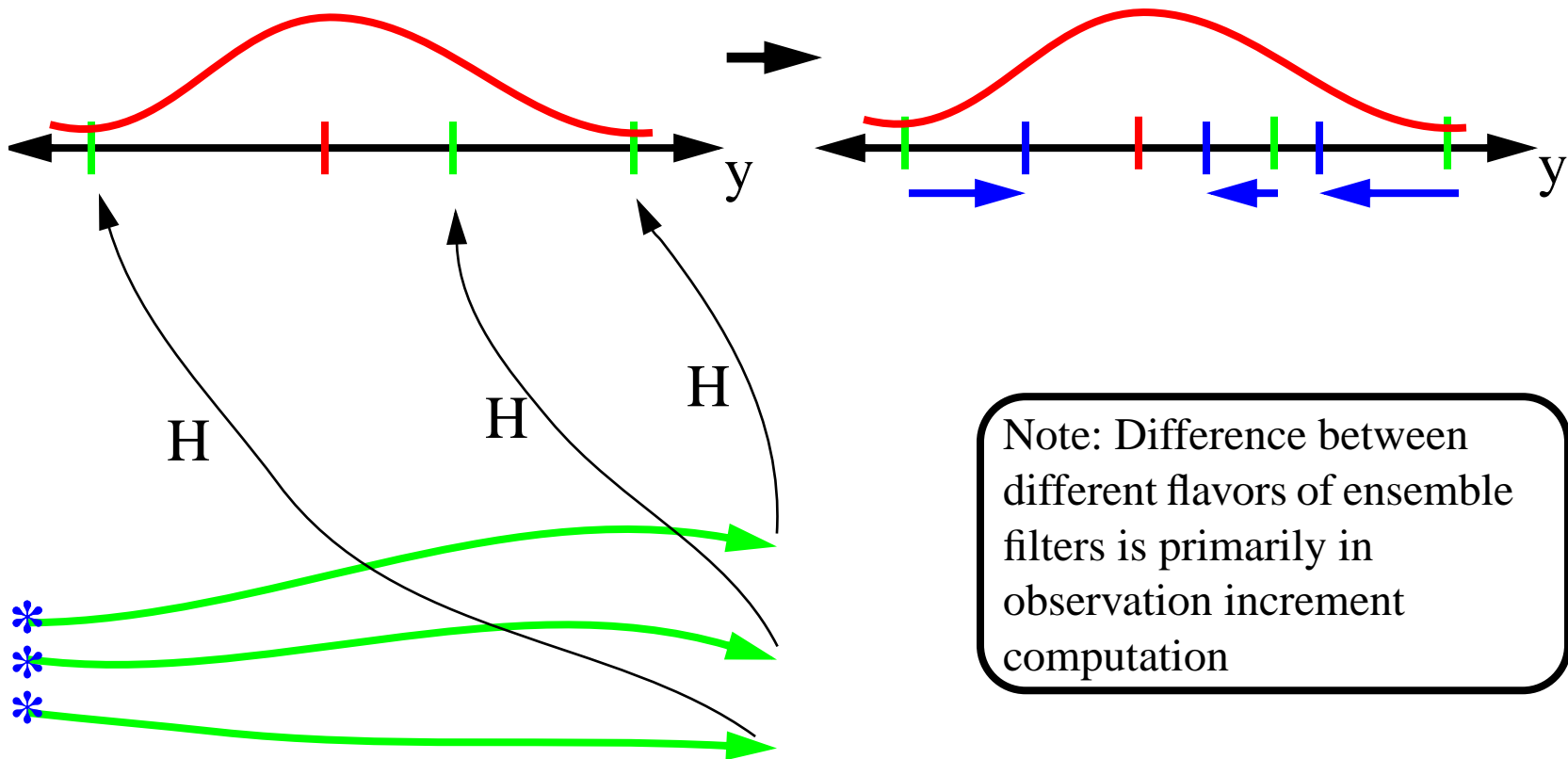
How an Ensemble Filter Works

3. Get **observed value** and **observational error distribution** from observing system



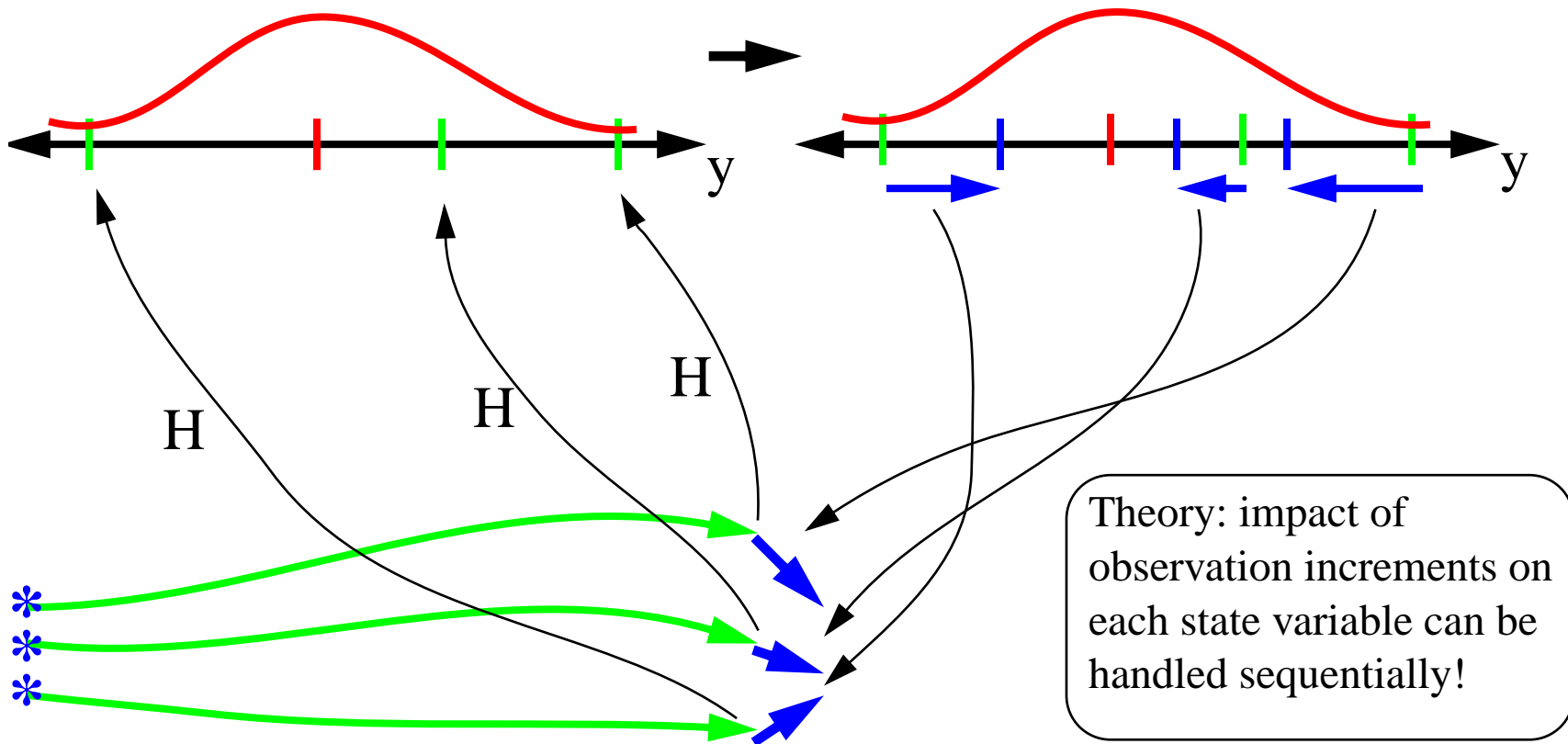
How an Ensemble Filter Works

4. Find **increment** for each prior observation ensemble
(this is a scalar problem for uncorrelated observation errors)



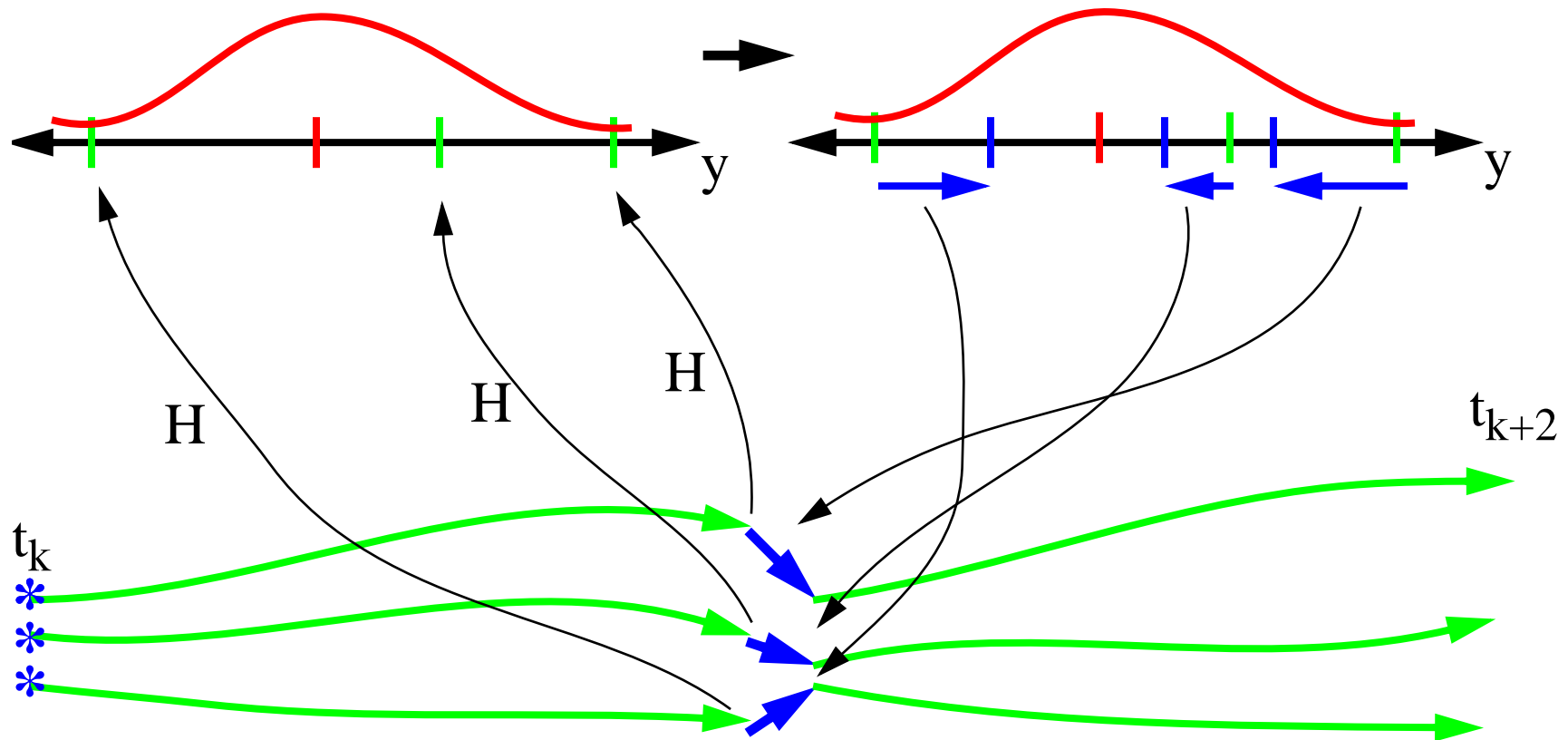
How an Ensemble Filter Works

5. Use ensemble samples of y and each state variable to linearly regress observation increments onto state variable increments



How an Ensemble Filter Works

6. When all ensemble members for each state variable are updated, have a new analysis. Integrate to time of next observation...



1. Filters are Easy to Apply

All one needs is:

- A. Ability to integrate a model forward in time
- B. Ability to compute forward observation operators

Collaborators have put GCMs in our framework in < 1 person month

2. Filters are computationally competitive

A. Model integrations required

Filter requires N forward integrations of model; $O(10)$ sufficient?

4D-var requires $K*L$ forward and backward integrations

K - number of observation intervals over which optimization is performed

L - average number of iterations of minimization solver

$K*L$ at least $O(10)$ for any envisioned application

B. Assimilation algorithm cost

Filter: $O(\alpha Nnm)$: N is ensemble size, n is model size, m is number of obs
 α related to what fraction of state variables are impacted by given ob.

In certain scenarios this may reduce order of cost

4D-var: $O(nm)$ in best of all possible cases

Relation of constant factors not clear, depends on ensemble size

Data Assimilation Research Testbed (DART)

Basic framework implemented

Primarily implementing ensemble (Kalman) filters

Variational for low-order models only

Plans MAY include a variational (4D-Var) capability

DART compliant models (largest collection ever with assim system)

CGD's CAM 2.0

GFDL FMS B-grid GCM

Many low-order models available

MMM's WRF model

NCEP MRF (GFS)

GFDL MOM ocean model partially incorporated in earlier version

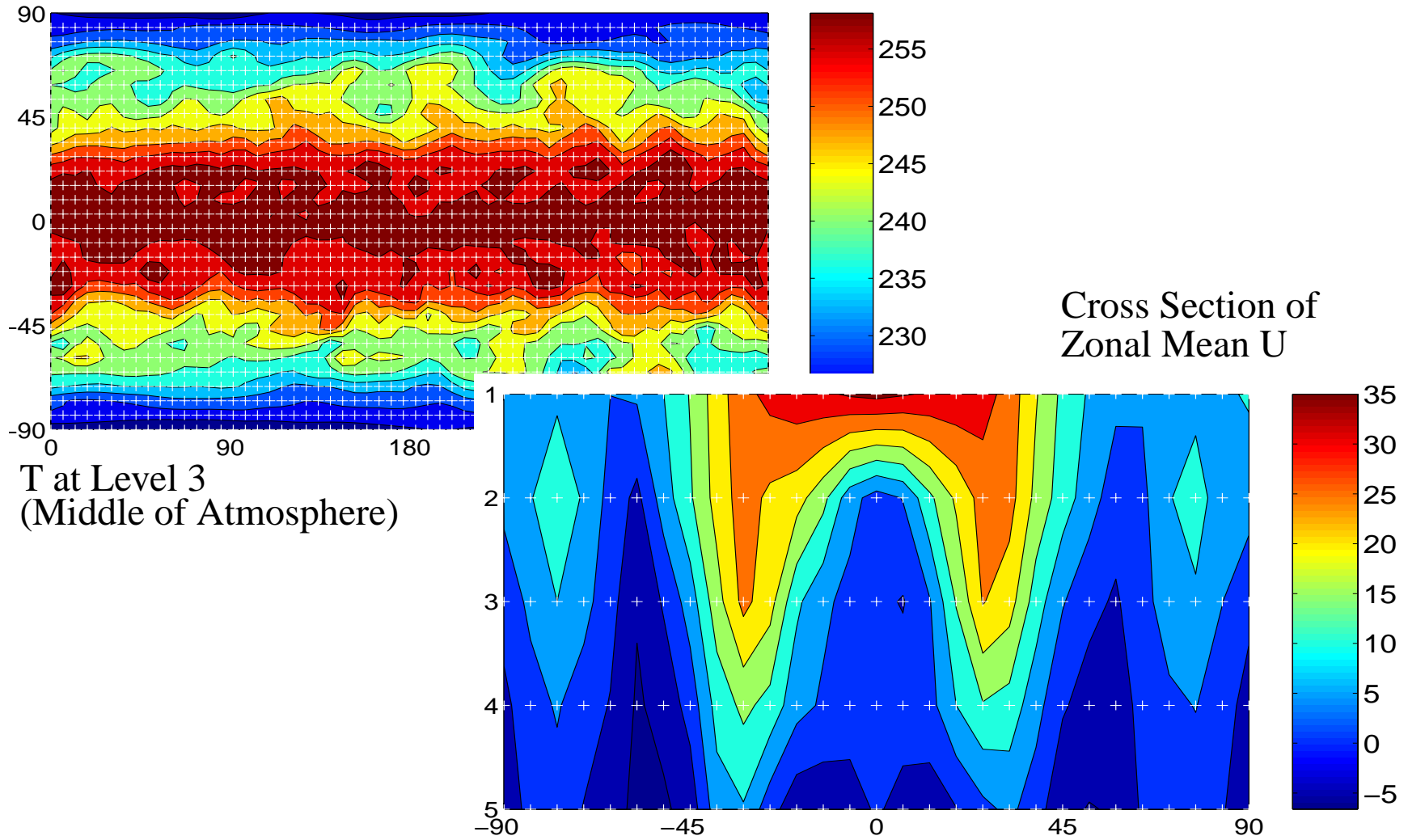
3. Extract amazing amounts of information in perfect model cases

WARNING: View Perfect Model Results with Skepticism

Predictability in an Idealized AGCM: GFDL FMS B-Grid Dynamical Core (Havana)

Held-Suarez Configuration (no zonal variation, fixed forcing)

Low-Resolution (60 lons, 30 lats, 5 levels); Timestep 1 hour (less for frequent observations)

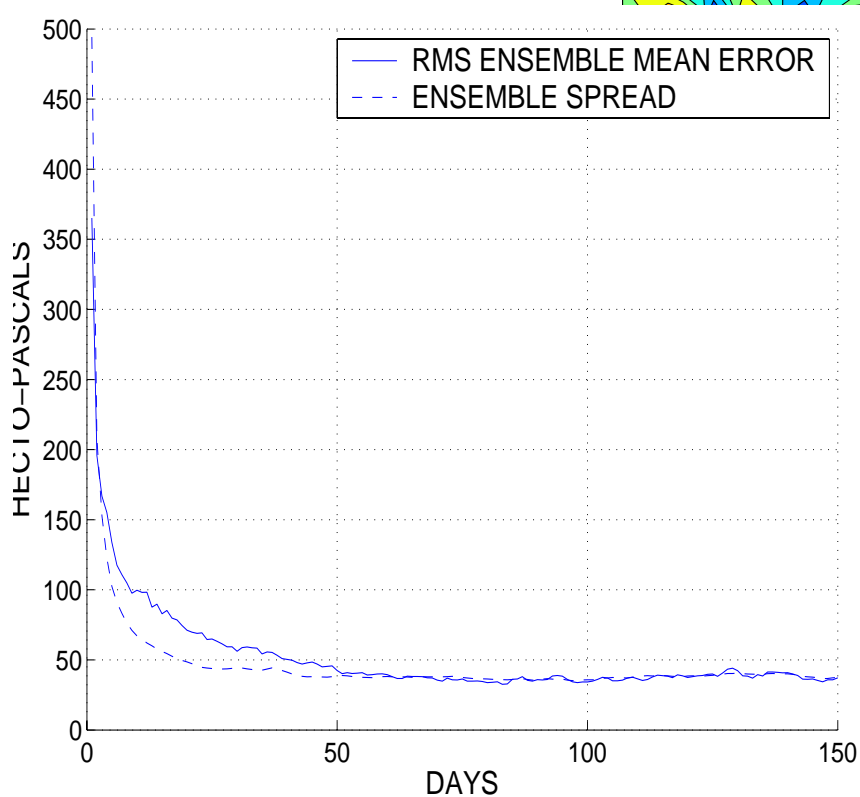
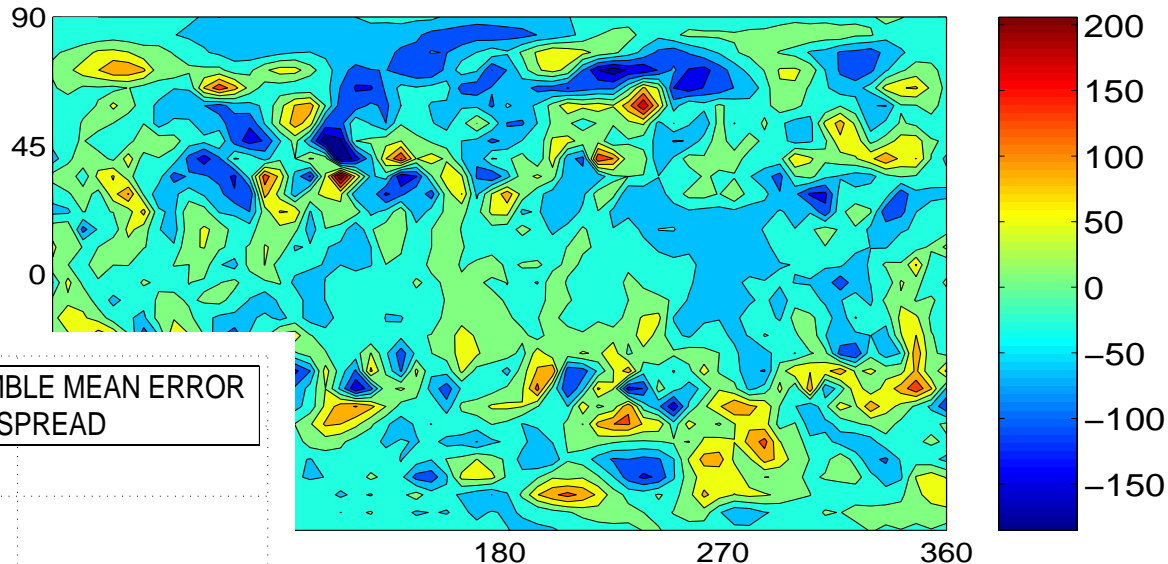


Has Baroclinic Instability

Baseline Case: 1800 PS Obs every 24 hours

Largest error in mid-latitudes, 'synoptic' scales after 400 days

Min = -185.1243 Max = 244.9236 RMS ERROR = 37.5623



PS Error Reduces by about factor of 10

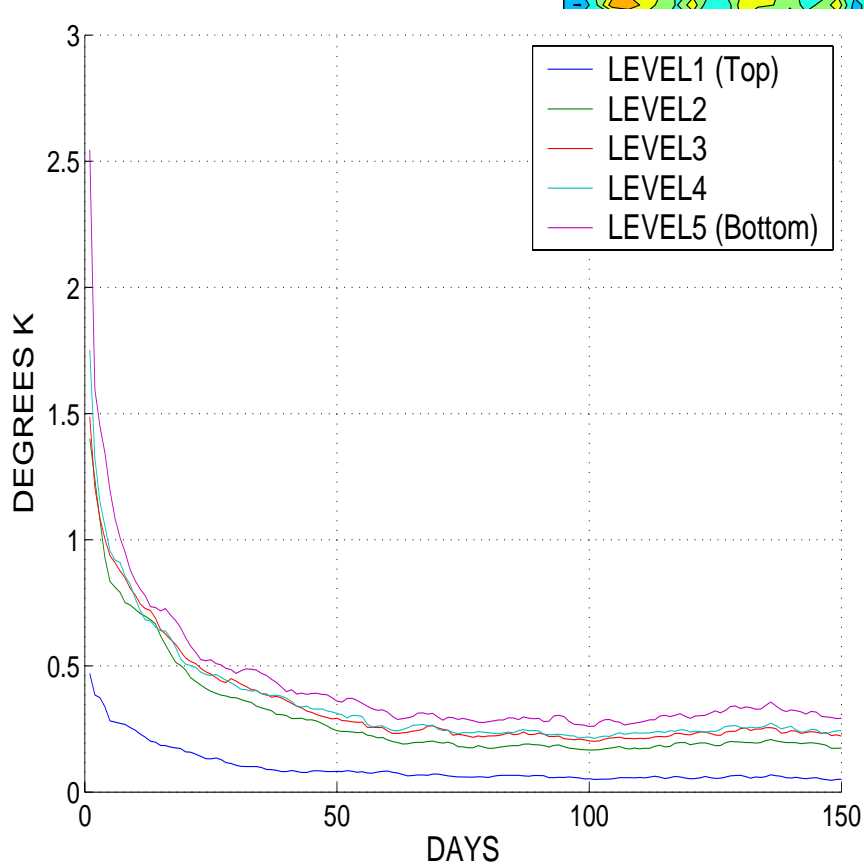
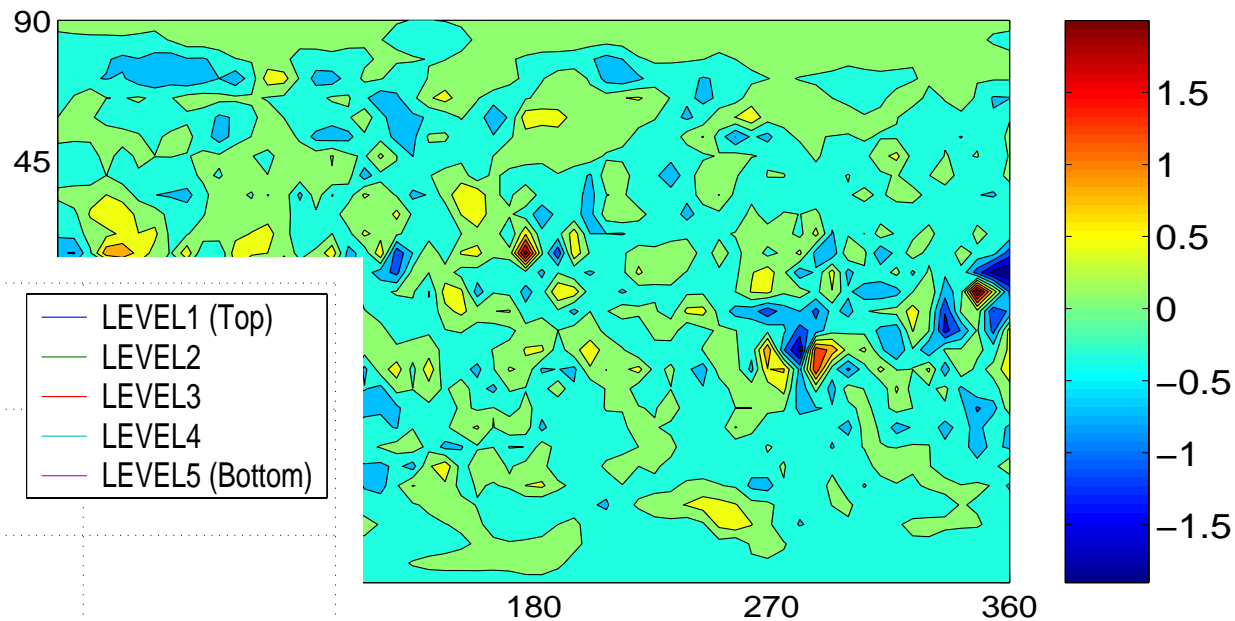
Asymptotes after about 50 days

Ensemble spread is approximately correlated with RMS error

Baseline Case: 1800 PS Obs every 24 hours

Largest T error in tropics for interior levels (level 3, day 400 shown)

Min = -1.9012 Max = 2.3893 RMS ERROR = 0.24305



T Error also reduced by about factor of 10

Asymptotes about day 70

Final error about 0.25 K for interior levels

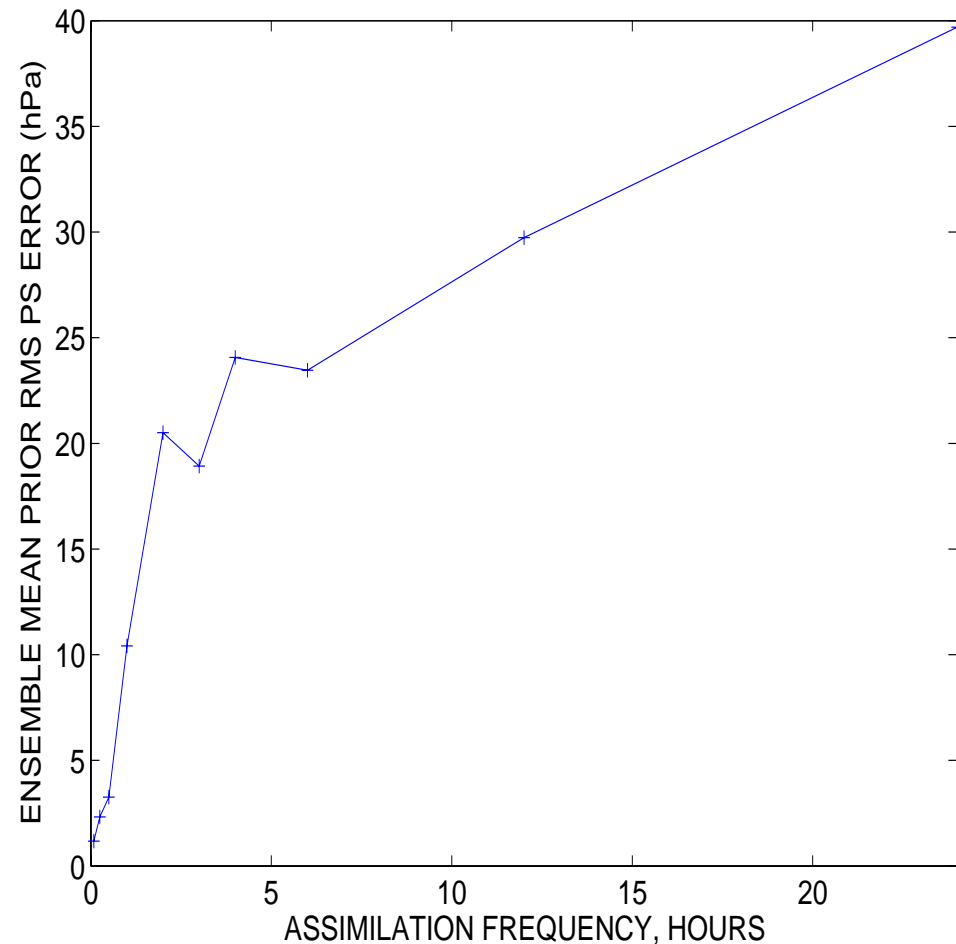
Impacts of frequency of PS observations on PS assimilation error

Cases with 1800 obs. every 24, 12, 6, 4, 3, 2, 1 hours; 30, 15, 5 minutes

Steady RMS decrease
as frequency increases

Much smaller RMS
than for high density
low frequency obs

RMS < 0.02mb for 5
minutes



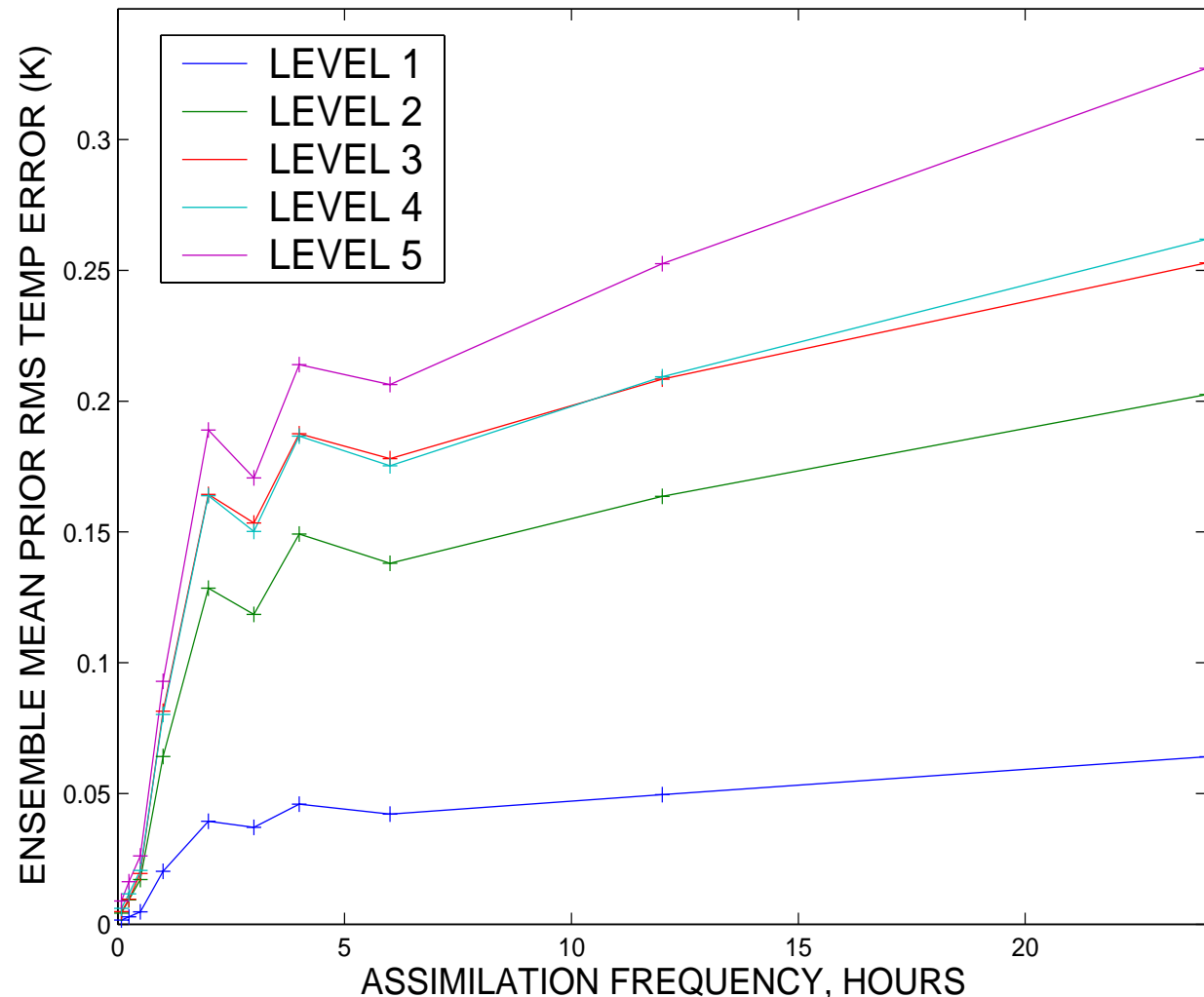
Impacts of frequency of PS observations on T assimilation error

Temperature (and U and V, not shown) similar to PS

Consistent decrease in RMS with increased obs frequency

Errors at 5 minute frequency less than 0.01 K!!!

How low can you go?



4. Can handle real (biased) model and real (ugly) observations

Model:

CAM 2.0 T42L26

U, V, T, Q and PS state variables impacted by observations

Land model (CLM 2.0) not impacted by observations

Observed SSTs

Assimilation / Prediction Experiments:

Uses observations used in reanalysis

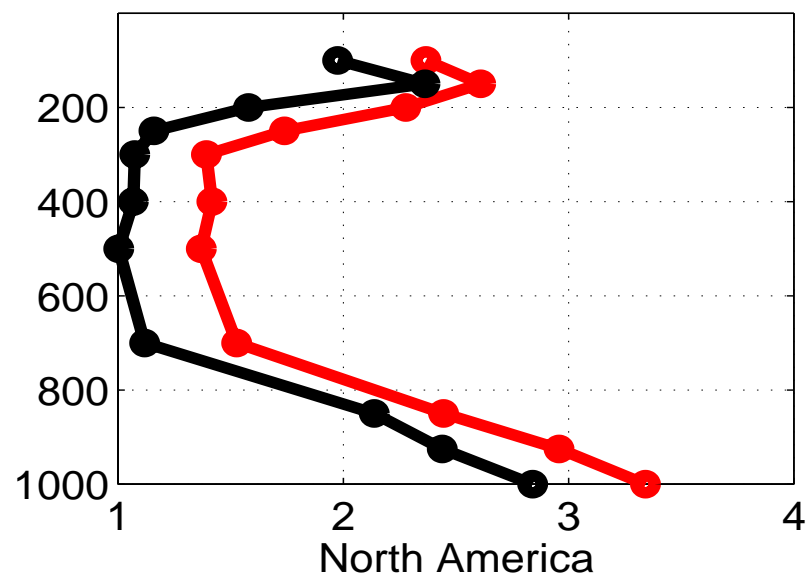
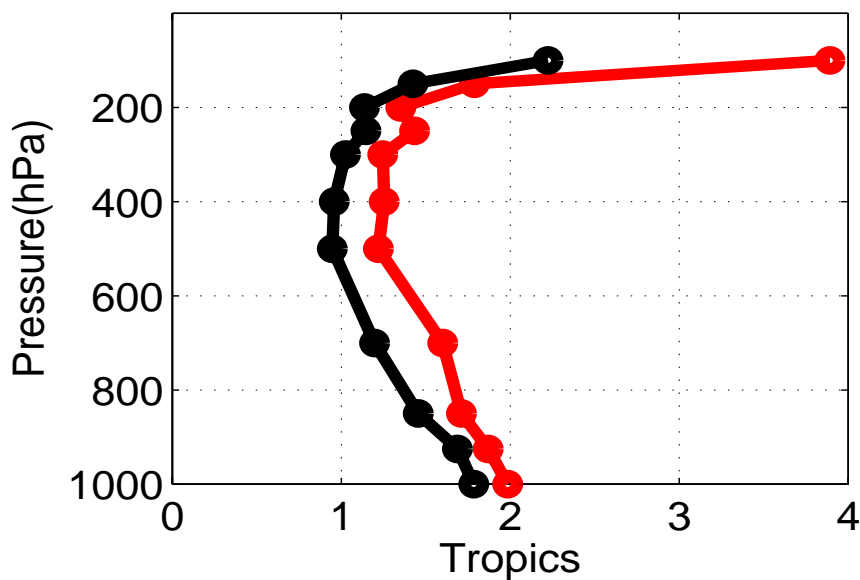
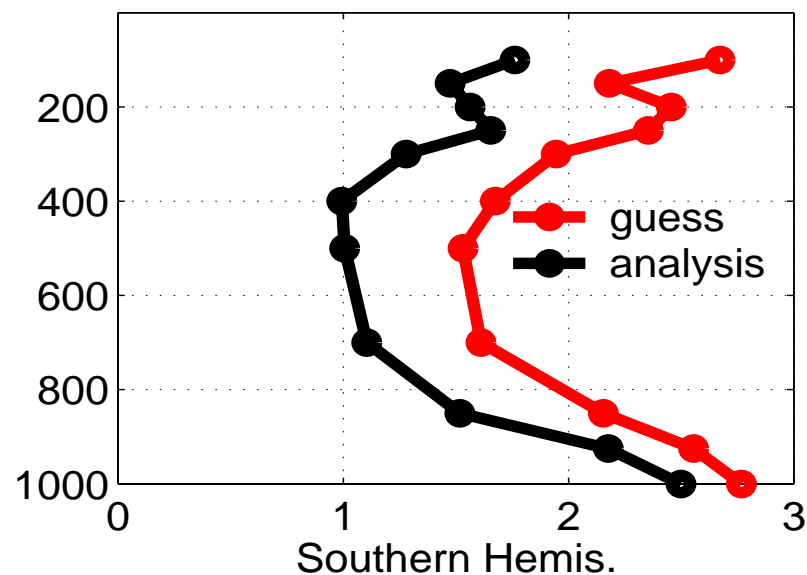
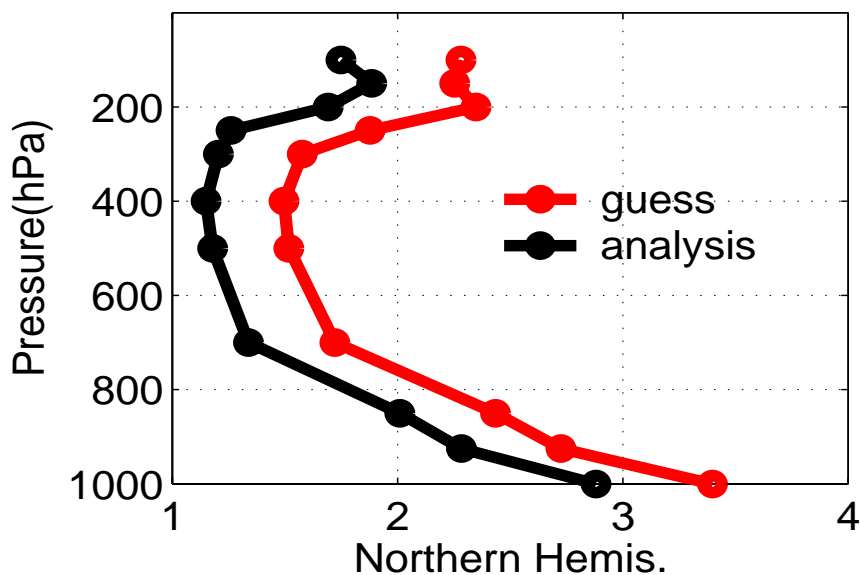
(Radiosondes, ACARS, Satellite Winds...)

Initial tests for first week of January, 2003

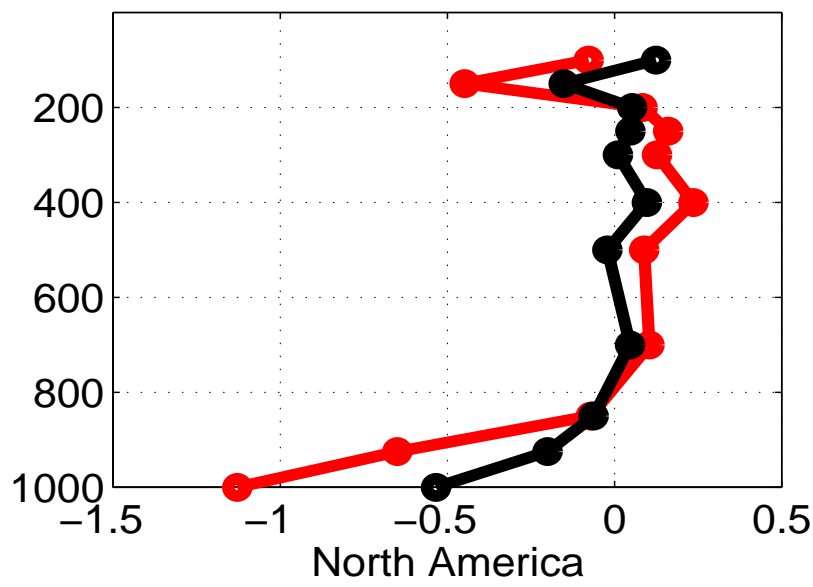
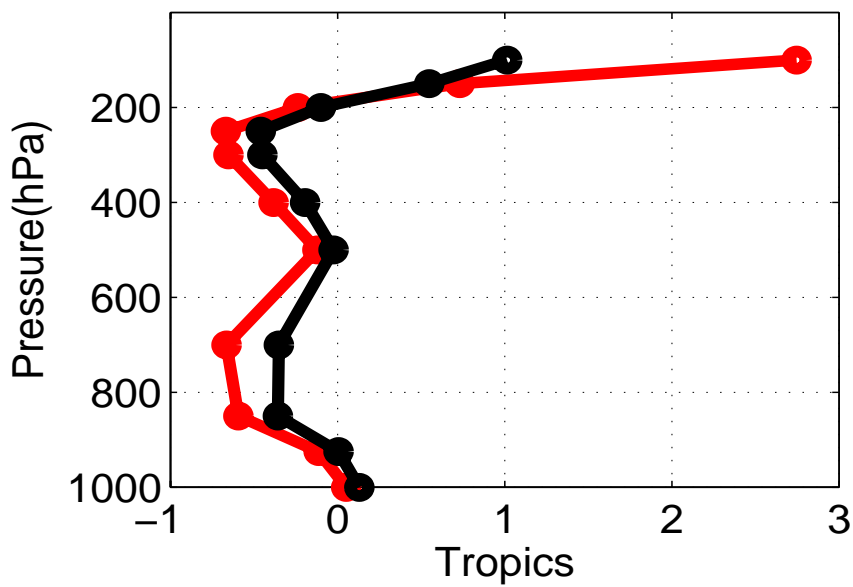
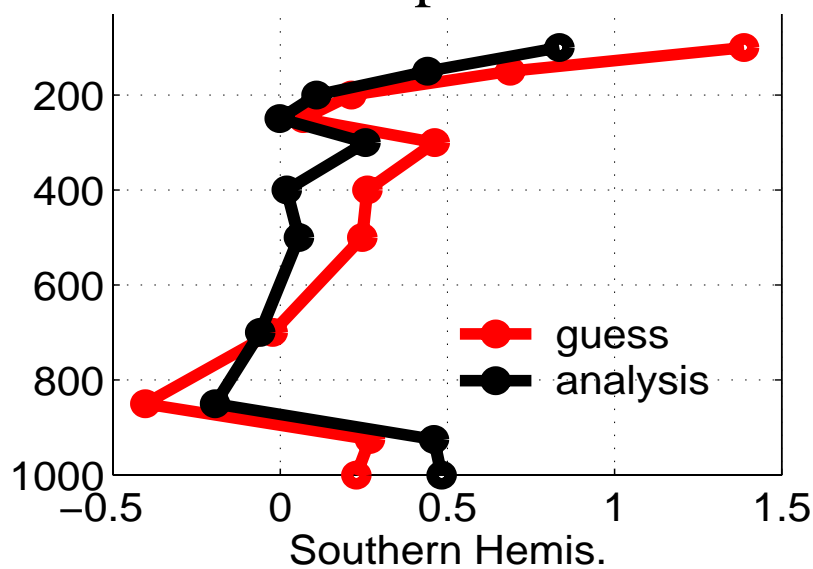
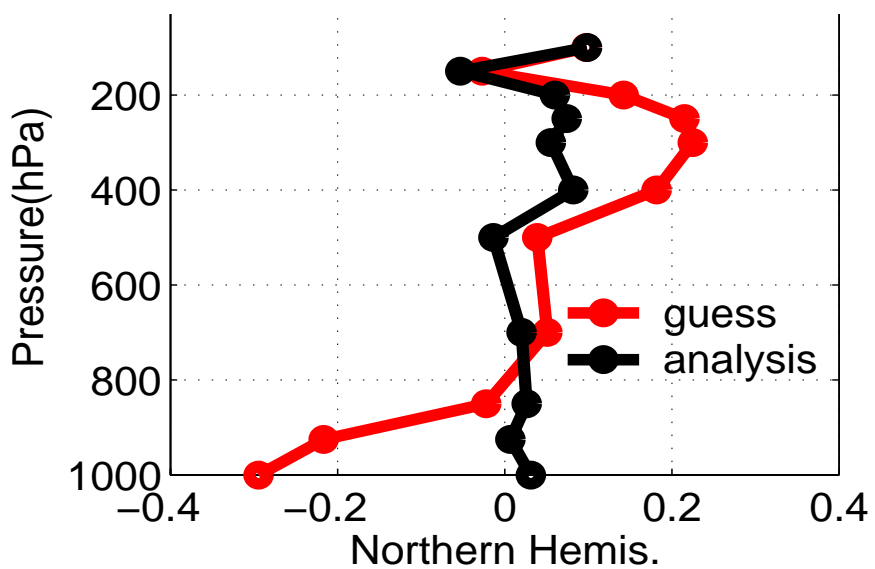
Assimilated every 6 hours

Run on CGD linux cluster Anchorage

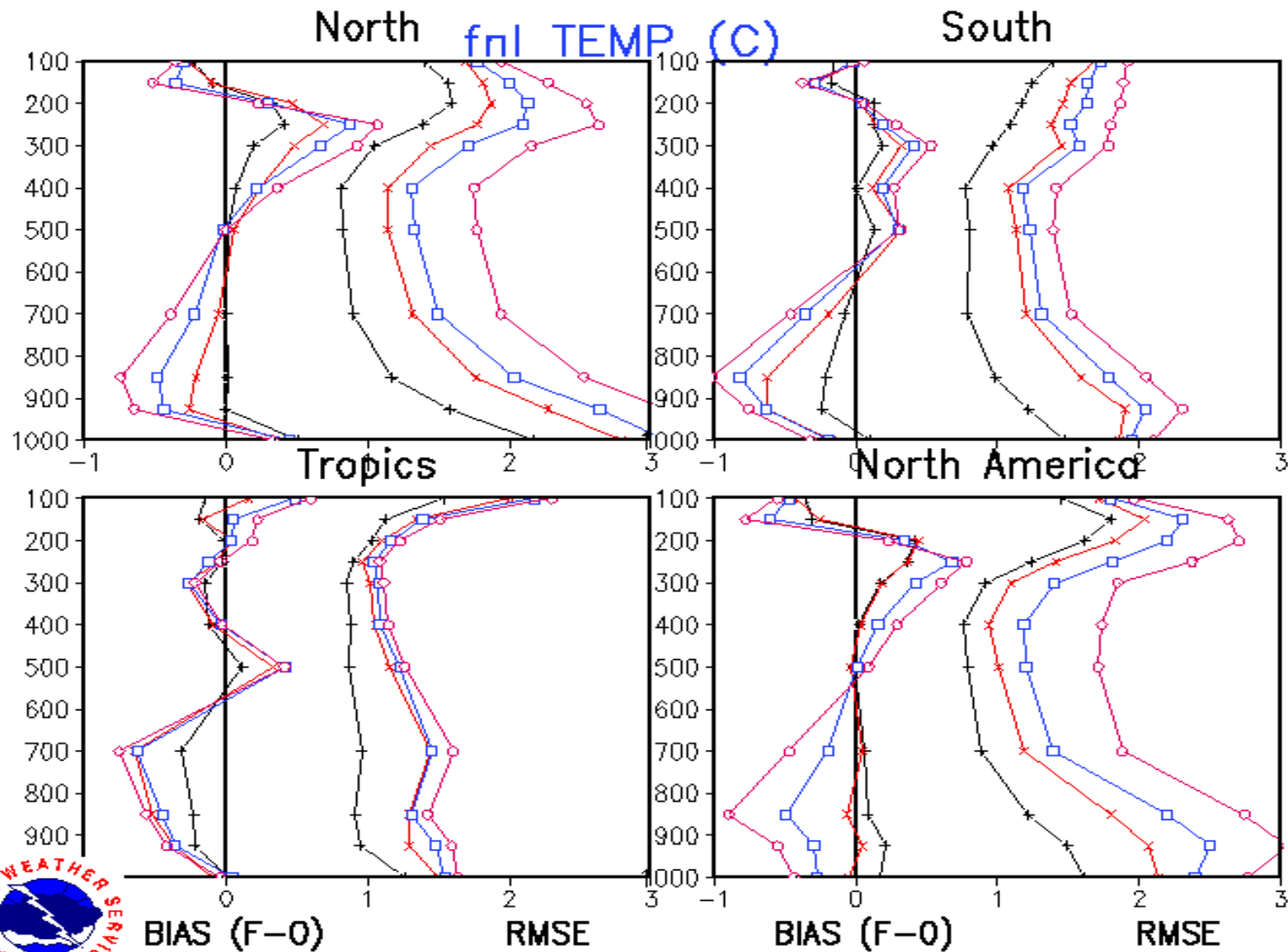
CAM RESULTS: ENSEMBLE MEAN RMS TEMP. ERROR



CAM RESULTS: Ensemble Mean Time Mean Temperature BIAS



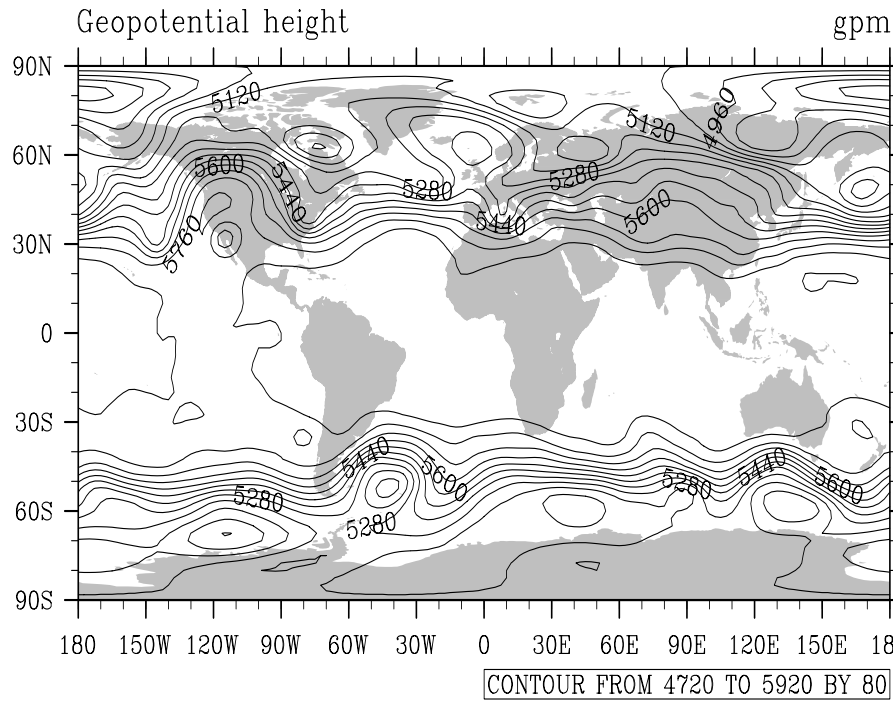
NCEP GFS BIAS (Left), RMS (right): Black Analysis, Red Guess



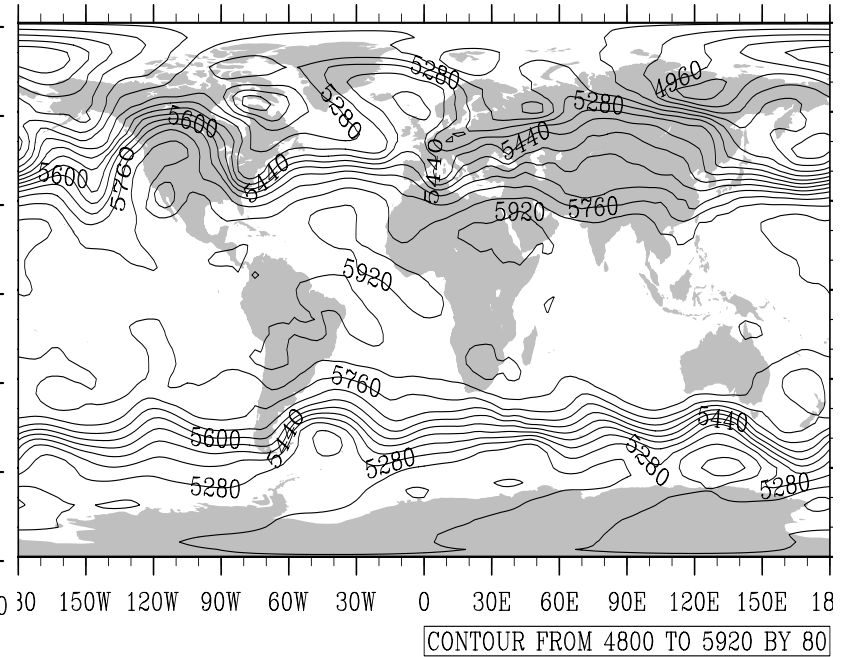
00z01ian2003 - 00z31ian2003

500mb Height Comparison to NCEP CDAS Analysis; Jan. 7, 2003

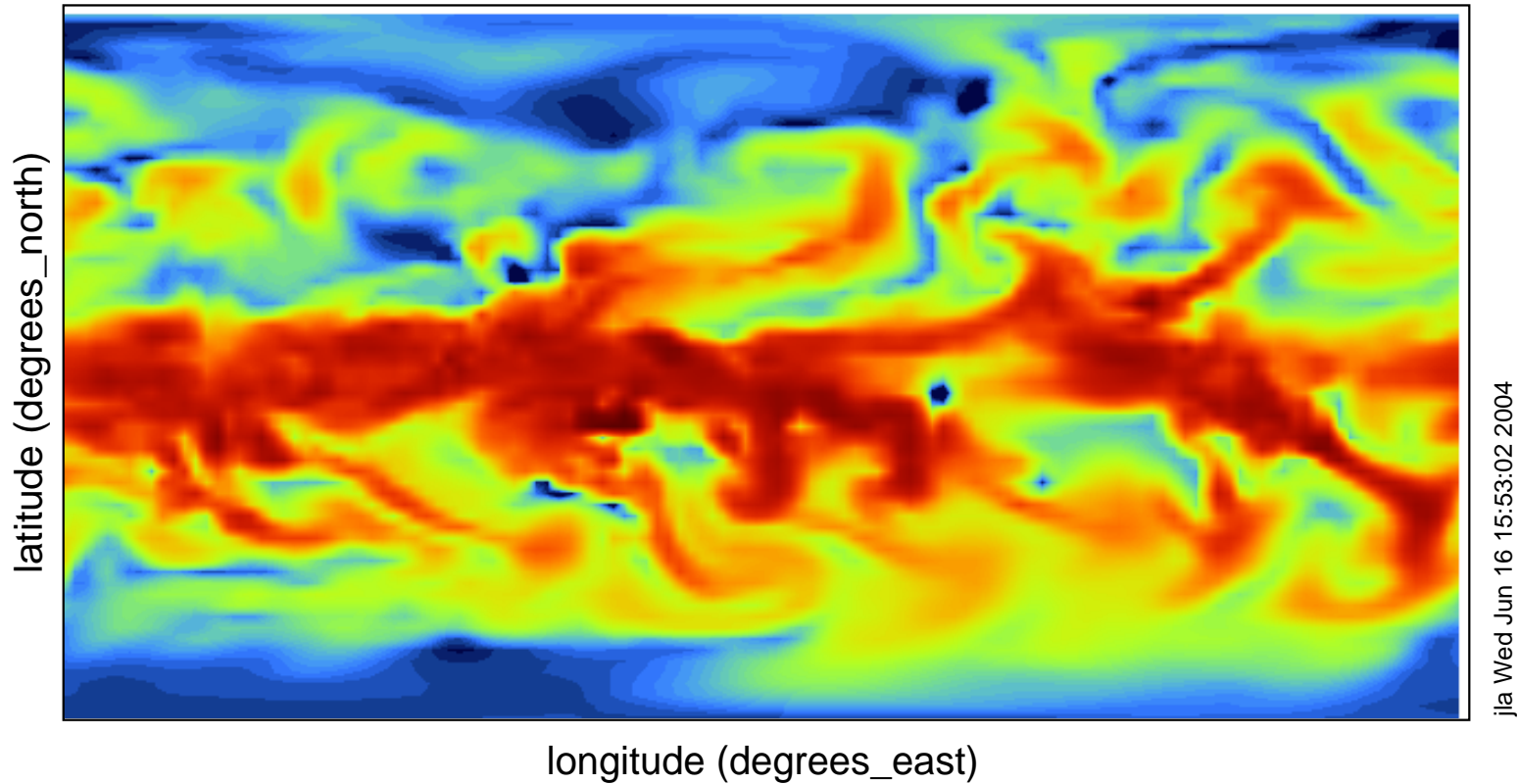
NCEP reanalyses, 500mb GPH, Jan 07 00Z



DART/CAM analyses, 500mb GPH



Captures details of q without q obs; q increments from other obs!
Specific Humidity (kg/kg)



Conclusions

1. Ensemble filters can do complex, real-data assimilation problems
2. Implementing filters is extremely simple
(compared to most assimilation techniques)
3. Filters are powerful in extracting multi-variate relations
4. Filters can deal with tracers, observed or unobserved
5. Assimilation is relatively cheap, but ensembles are required