# Assignments/Dates

- Chapter 3 notes due Feb 15
- <u>http://journals.ametsoc.org/doi/pdf/10.1175/BAMS-88-</u>
  <u>6-853</u> Cerveny Article
- Amazon Drought paper review Due Feb 17
- Odds Are It's Wrong. Due Feb 22
  - <u>http://www.sciencenews.org/view/feature/id/57091/title/Odds</u>
    <u>Are, Its\_Wrong</u>
  - Read and summarize issues about significance testing in a few paragraphs
- Chapter 4 notes due Feb 24
- Exam March 1.

#### Extreme Weather Records Compilation, Adjudication, and Publication BY RANDALL S. CERVENY, JAY LAWRIMORE, ROGER EDWARDS, AND CHRISTOPHER LANDSEA

Weather element	Characteristic	Value	Date	Location	
Temperature	Maximum	56.67°C (134°F)	10 Jul 1913	Greenland Ranch, California	
	Minimum	-62.22°C (-80°F)	23 Jan 1971	Prospect Creek, Alaska	
	Max 24-h change	39.44°C (103°F)	14–15 Jan 1972	Loma, Montana	
Snow	Max 24-h snowfall	1.925 m (75.8 in.)	14-15 Apr 1921	Silver Lake, Colorado	
	Max seasonal snowfall (July–June)	28.956 m (1140 in.)	1998–1999	Mt. Baker Ski Area, Washington	
	Max snow depth	11.455 m (451 in.)	11 Mar 1911	Tamarack, California	
Rain	Max 24 hr	1.092 m (43 in.)	25–26 Jul 1979	Alvin, Texas	
	Least annual	0.0 m	1929	Death Valley, California	
	Max annual	17.903 m (704.83 in.)	1982	Kukui, Hawaii	
	Longest dry period	767 days	3 Oct 1912– 8 Nov 1914	Bagdad, California	
Wind	Max gust	103.3 m s <sup>-1</sup> (231 mph)	12 Apr 1934	Mt. Washington, New Hampshire	
Hail	Largest (diameter/ circumference)	17.78 mm/47.625 mm (7 in./18.75 in.)	22 Jun 2003	Aurora, Nebraska	
	Heaviest	0.7575 kg (1.67 lbs)	3 Sep 1970	Coffeyville, Kansas	
Pressure	Lowest	892.3 mb (26.35 in. Hg)	2 Sep 1935	Matecumbe Key, Florida	
	Highest	1078.6 (31.85 in. Hg)	31 Jan 1989	Northway, Alaska	

TABLE I. U.S. weather elements and characteristics currently within the jurisdiction of the NCEC.

#### US CLIVAR/NCAR ASP Researcher Colloquium (by Invitation/Application) Statistical Assessment of Extreme Weather Phenomena under Climate Change NCAR Foothills Lab, Boulder, Colorado, USA June 1317, 2011

The US CLIVAR/NCAR Research Colloquium will assemble climate researchers, statisticians, decision and policy makers to discuss the state-of-the-art in science of weather and climate extremes and its application to real-world decision-making. Specific objectives:

□ Determine climate and weather extremes that are crucial in resources management and policy making

□ Identify the current state of the science of climate and weather extremes including uncertainties and information gaps in real-world applications

□ Obtain insights into the capabilities of climate models in identifying and modeling such extreme events.

□ Assess efficacy of statistical methods and tools to analyze and model extreme events under climate change

□ Develop interdisciplinary research directions in modeling and application of climate extremes.

The Colloquium organizing committee invites the participation of researchers studying extreme events in observations and climate models; statistical modeling and identification of extremes; use of climate extremes in a suite of decision and policy making context.

If you are interested in participating, please submit an application with your CV and a brief statement of interest via an online application at

http://www.regonline.com/Register/Checkin.aspx?EventID=931739. Travel support is available. You will be asked to identify any travel support needs in your application. The deadline for applications is March 28, 2011.

# Science Magazine

<u>http://www.sciencemag.org/site/special/dat</u>
 <u>a/</u>

# 4. Exploratory Multivariate Data Analysis

- want to relate how one or more phenomena are related to others
- Think of it as a multidimensional problem and the goal is to reduce the dimensionality through exploration of relationships
- Dealing with the dimensionality of environmental data sets in statistical analyses is of general concern (Murphy 1991; Mon. Wea. Rev., 1590-1601).
- Exploratory multivariate data analysis encompasses an array of tools to assess relationships between two or more samples

# **SNOTEL Sites**



### **Ben Lomond Daily Precipitation**











# Estimating Values of One Variable From Another

- X- Ben Lomond Trail
- Y- Ben Lomond Peak
- Want to estimate Peak from Trail
- Use pairs of observations from sample
- Need to determine coefficient b or r
- b- slope of linear estimate
- r- linear correlation

 $\hat{y}_i = \bar{y} + b(\hat{x}_i - \bar{x})$  $\hat{y}_i^* = r \hat{x}_i^*$ 

# Definitions

- Estimate  $\hat{y}_i = \bar{y} + b(\hat{x}_i \bar{x})$
- Error of estimate  $e_i = y'_i \hat{y}'_i$
- Want  $\sum_{i=1}^{n} e_i^2$  to be a minimum
- Need to find the value of b that minimizes that sum

$$\frac{\partial}{\partial b}\sum_{i=1}^{n}e_{i}^{2}=0$$

• The value of b that minimizes the total error in the sample  $b = \overline{x'_i y'_i} / \overline{(x'_i)^2} = \overline{x'_i y'_i} / s_x^2$ 

# Covariance

- Relates how departures of x and y from respective means are related
- Units are the product of the units of the two variables x and y
- Large and positive if sample tendency for:
  - large + anomalies of x occurring when large + anomalies of y AND
  - large anomalies of x occurring when large anomalies of y
- Large and negative if sample tendency for:
  - large + anomalies of x occurring when large anomalies of y AND
  - large anomalies of x occurring when large + anomalies of y
- Near zero when tendency for cancellation
  - large + anomalies of x occurring when both large and + anomalies of y AND
  - large anomalies of x occurring when both large and + anomalies of y

# **Linear Correlation**

$$r^{2} = b^{2} s_{x}^{2} / s_{y}^{2} = (\overline{x'_{i} y'_{i}})^{2} / (s_{x}^{2} s_{y}^{2}) \qquad r = (\overline{x'_{i} y'_{i}}) / \sqrt{x'_{i}^{2} \overline{y'_{i}^{2}}}$$
$$x_{i}^{*} = x'_{i} / s_{x}, y_{i}^{*} = y'_{i} / s_{y}, r = (\overline{x'_{i} y'_{i}})$$

- $1 = r^2 + \frac{e_i^2}{s_y^2}$  y's total sample variance = fraction of variance estimated by x + fraction of variance NOT explained by x
- Dimensionless number relates how departures of x and y from • respective means are related taking into account variance of x and y
- r = 1. Linear fits estimates ALL of the variability of the y anomalies and x and y vary identically
- r = -1 perfect linear estimation but when x is positive, y is negative and vice versa
- r = 0. linear fit explains none of the variability of the y anomalies in the sample. Best estimate of y is the mean value

### Linear Algebra is your friend



$$\overline{x_i'y_i'} = \vec{X}'^T \vec{Y}'/n$$

# Variations on a theme

- Pearson correlation vs. Spearman rank correlation
- Spearman- correlating ranks not values
  - Good for skewed distributions

#### Stop and think before blindly computing correlations

- tendency to use correlation coefficients of 0.5-0.6 to indicate "useful" association.
  - 75%-64% of the total variance is NOT explained by a linear relationship if the correlation is in that range
- linear correlations can be made large by leaving in signals that may be irrelevant to the analysis. Annual and diurnal cyles may need to be removed
- large linear correlations may occur simply at random, especially if we try to correlate one variate with many, many others
- relationships in the data that are inherently nonlinear will not be handled well
- when two time series are in quadrature with one another then the linear correlation is 0
- Linear correlation provides no information on the relative amplitudes of two time series



## **Multivariate Linear Correlations**





## **Multivariate Linear Correlations**

![](_page_19_Figure_1.jpeg)

 $\vec{X}^* = \begin{bmatrix} x^*_{11} & x^*_{12} & \dots & x^*_{17} \\ x^*_{21} & x^*_{22} & \dots & x^*_{27} \\ \dots & \dots & \dots & \dots \\ x^*_{n1} & x^*_{n2} & \dots & x^*_{n7} \end{bmatrix}$ 

 $\vec{R} = \vec{X} *^T \vec{X} * / n$ 

![](_page_19_Figure_4.jpeg)

#### **Linear Correlation Coefficients**

TABLE 1. Matrix of contemporaneous correlation coefficients (×100) between the time series shown in Figs. 2, 3, 4, 7 and 10. The number of winter seasons used in each correlation, if less than the complete 28 seasons (1951-78), is indicated in parentheses.

	SST Index	SLP Index	200 mb Index	PNA Index	WP Index	Tarawa rainfall	Canton rainfall	Christmas rainfall	Fanning rainfall
SST Index									
SLP Index	-83								
200 mb Index	80	-68							
PNA Index	46	-31	57						
WP Index	67	-57	44	-00					
Tarawa rainfall	78	-71	63	32	65				
Canton rainfall	82 (23)	-65 (23)	61 (23)	40 (23)	65 (23)	60 (23)	(23)		
Christmas rainfall	64 (24)	-49 (24)	57 (24)	40 (24)	48 (24)	55 (24)	82 (19)	(24)	
Fanning rainfall	79 (23)	-60 (23)	69 (23)	38 (23)	70 (23)	72 (23)	85 (18)	84 (23)	(23)

#### Teleconnections

![](_page_21_Figure_1.jpeg)

FtG. 9. Correlation coefficients between 700 mb geopotential height at gridpoints poleward of 20°N and (a) the Sea Surface Temperature Index, (b) December-February rainfall at Fanning, (c) our Southern Oscillation Index, and (d) the tropical 200 mb Index. Contour interval 0.2. The locations of the centers of action of the Pacific/North American and West Pacific patterns are denoted, respectively, by dots and open circles in Fig. 9d.

#### Teleconnections

![](_page_22_Figure_1.jpeg)

FIG. 9. Correlation coefficients between 700 mb geopotential height at gridpoints poleward of 20°N and (a) the Sea Surface Temperature Index, (b) December-February rainfall at Fanning, (c) our Southern Oscillation Index, and (d) the tropical 200 mb Index. Contour interval 0.2. The locations of the centers of action of the Pacific/North American and West Pacific patterns are denoted, respectively, by dots and open circles in Fig. 9d.

#### http://www.cdc.noaa.gov/Correlation

![](_page_23_Figure_1.jpeg)

NOAA-CIRES/Climate Diagnostics Center

# **Correlating Maps Rather Than Time Series**

$$\hat{\vec{X}} = \begin{bmatrix} \hat{x}_{1,1} & \hat{x}_{1,2} & \dots & \hat{x}_{1,18} \\ \hat{x}_{2,1} & \hat{x}_{2,2} & \dots & \hat{x}_{2,18} \\ \dots & \dots & \dots & \dots \\ \hat{x}_{7,1} & \hat{x}_{7,2} & \dots & \hat{x}_{7,18} \end{bmatrix}$$

$$\vec{S} = \hat{\vec{X}} *^T \hat{\vec{X}} * /7$$

 Comparing variability in one year over 7 locations to the variability in all of the other n= 18 years

### **Comparing Forecast Anomaly Maps to Analyses**

![](_page_25_Figure_1.jpeg)