

Boundary-Layer Meteorology

Dynamically Induced Displacements of a Persistent Cold-Air Pool

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Abstract:	This study examines the influence of a passing weather system on a persistent cold-air pool (CAP) during the Persistent Cold-Air Pool Study in the Salt Lake Valley, UT. The CAP experiences a sequence of along-valley displacements that temporarily and partially remove the cold air in response to increasing along-valley winds aloft. The displacements are due to the formation of a mountain wave over the upstream topography as well as adjustments to the regional pressure gradient and wind stress acting on the CAP. These processes appear to help establish a balance wherein the depth of the CAP increases to the north. When that balance is disrupted, the CAP depth collapses, which sends a gravity current of cold air back upstream and thereby restores CAP conditions throughout the valley. Intra-valley mixing of momentum, heat, and pollution within the CAP by Kelvin-Helmholtz waves and seiching is also examined.
Suggested Reviewers:	<p>Gunther Zangl, PhD Deutscher Wetterdienst guenther.zaengl@dwd.de Publication of numerous related studies</p> <p>Heather Reeves, PhD National Severe Storms Laboratory heather.reeves@noaa.gov Publication of recent cold-air pool literature</p> <p>Jeilun Sun, PhD National Center for Atmospheric Research jsun@ucar.edu Work related to the stable boundary layer during CASES-99 including gravity current dynamics and antitriptic balance.</p> <p>Bowen Zhou, PhD University of California Berkeley zhoubowen@berkeley.edu Recent publication on simulating katabatic flows including mixing via Kelvin-Helmholtz</p>

waves.

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Recent work on COLPEX, a cold-air pool study in the UK.

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46 **Abstract** This study examines the influence of a passing weather system on a persistent
47 cold-air pool (CAP) during the Persistent Cold-Air Pool Study in the Salt Lake Valley, UT.
48 The CAP experiences a sequence of along-valley displacements that temporarily and partially
49 remove the cold air in response to increasing along-valley winds aloft. The displacements are
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52 appear to help establish a balance wherein the depth of the CAP increases to the north. When
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54 back upstream and thereby restores CAP conditions throughout the valley. Intra-valley mix-
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58 **Keywords** Cold-air Pool, Inversion, Kelvin-Helmholtz Instability, Mountain Wave Turbulent
59 Mixing, Seiche, Stable Boundary Layer

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62 1 Introduction

63

64 The disruption of persistent cold-air pools (CAPs) arising from passing weather systems is
65 examined in this study. CAPs are decoupled air masses that form in mountain valleys and ba-
66 sins due to cooling of the air near the surface, warming of the air aloft, or both (Whiteman et
67 al. 1999). The resulting stable stratification suppresses vertical mixing while the confining
68 topography prevents advection and favors air stagnation. Persistent CAPs are simply CAPs
69 surviving through more than one diurnal cycle (Whiteman et al. 2001).

70 Persistent CAPs are often accompanied by adverse societal impacts. When they occur in
71 densely settled valleys, the emissions from vehicles, home heating, and industrial sources ac-
72 cumulate, leading to unhealthy air quality (Reddy et al. 1995; Pataki et al. 2005; Pataki et al.
73 2006; Malek et al. 2006; Silcox et al. 2012). High particulate concentrations during CAPs
74 have recently been linked to increased risk for cardiovascular disease and asthma and may
75 lead to decreased lifespan (Pope et al. 2009; Beard et al. 2012). Suppressed temperatures
76 within CAPs combined with the presence of snow cover can also increase the likelihood of
77 fog, which affects air and ground transportation (Wolyn and Mckee 1989).

78 The strength and longevity of persistent CAPs is modulated by the synoptic conditions es-
79 tablishing them, the surface energy budget, and subsequent interactions with passing weather
80 systems (Wolyn and Mckee 1989; Whiteman et al. 1999; Whiteman et al. 2001; Reeves and
81 Stensrud 2009; Gillies et al. 2010; Chow et al. 2013). CAPs most often form during the
82 warming aloft accompanying the arrival of high-pressure weather systems. Weak disturb-
83 ances may then temporarily perturb a CAP, whereas more vigorous baroclinic troughs are
84 likely to completely destroy them, especially those accompanied by strong cold-air advection
85 (Whiteman et al. 1999; Whiteman et al. 2001; Zhong et al 2001; Reeves and Stensrud 2009;
86 Chow et al 2013).

87 In the absence of strong cold-air advection, forecasting the demise of CAPs remains a
88 challenge. During such situations, CAP removal may be controlled by interactions among
89 four other mechanisms: (1) internal *convection*, (2) top-down *turbulent erosion*, (3) CAP *dis-*
90 *placement* and (4) *airflow* over the upstream topography (Lee et al. 1989; Petkovšek 1992;
91 Petkovšek and Vrhovec 1994; Gubser and Richner 2001; Zängl 2003; Zängl 2005; Flamant et
92 al. 2006).

93 In contrast to diurnal CAPs that form overnight and are destroyed by daytime heating,
94 *convection* alone is generally insufficient to destroy persistent CAPs due to weak sensible

95 heat flux during the winter (Zhong et al. 2001). However, when other processes are weaken-
 96 ing a CAP, convection may become an important factor in breakup (Whiteman et al. 1999;
 97 Zhong et al. 2001, Chow et al. 2013). For example, Whiteman et al. (1999) show that the fi-
 98 nal removal of persistent CAPs preferentially occurs in the afternoon when sensible heat flux
 99 is strongest.

100 The second mechanism, *turbulent erosion*, is the break down of CAP stratification via ir-
 101 reversible turbulent motions. Petkovšek (1992) proposed a semi-analytic model for this pro-
 102 cess wherein turbulent flow above a CAP progressively erodes downward into the stratified
 103 air. In this scenario, the CAP thins, but also strengthens, in time. The strengthened CAP sub-
 104 sequently suppresses the rate of turbulent encroachment, thus requiring an accelerating wind
 105 aloft for erosion to continue. Zhong et al. (2003) diagnose the time-scale for turbulent CAP
 106 erosion using idealized CAP profiles and steady winds at different strengths. Their results
 107 show that the erosion rate decays in time, consistent with Petkovšek’s hypothesis, and that
 108 turbulent erosion is very slow for typical CAP scales and thus unlikely to cause CAP breakup
 109 independent of other processes.

110 Turbulent erosion of stratification has also been observed in other geophysical flows, such
 111 as mixing across the thermocline in lakes and oceans (Fernando 1991). Strang and Fernando
 112 (2001 a, b) use laboratory tank experiments to examine the deepening rate of a mixed layer
 113 into a stable layer and show that mixed layer deepening progresses via Kelvin-Helmholtz and
 114 other dynamic instabilities, the occurrence of which is controlled by the Richardson number.

115 *CAP displacement*, the third process, is the rearrangement of CAP mass via static and dy-
 116 namic processes. Petkovšek and Vrhovec (1994), and later Zängl (2003), show that CAPs hy-
 117 drostatically adjust to regional pressure gradients by developing a sloping interface and thus
 118 an internal pressure gradient that offsets the pressure gradient aloft. When the CAP slope be-
 119 comes sufficiently large, cold-air spills over the confining topography and the volume of air
 120 within CAP is reduced (Zängl 2003). CAP tilt may also have a component due to wind stress
 121 acting on the CAP (Petkovšek and Vrhovec 1994, Gubser and Richner 2001, Zängl 2003).
 122 This effect can be particularly pronounced when winds are ageostrophic, e.g. acting in the
 123 same sense as the pressure gradient (Zängl 2003). This wind-stress effect is similar to “wind
 124 set-up” or storm surge that displaces water along the downwind fetch within lakes.

125 CAP displacement may also occur due to *airflow* over the upstream topography. Lee et al.
 126 (1989) examine the interaction of a mountain wave with a lee-side CAP in idealized simula-
 127 tions, and show that the CAP is displaced by the mountain wave unless there is an adverse
 128 pressure gradient generating an opposing surface flow toward the mountain. Interestingly,
 129 they also found that turbulent erosion was a minimal factor in CAP evolution despite strong
 130 shear.

131 More generally, the ventilation of valleys containing stratified air masses has been related
 132 to the Froude number (or its inverse, the non-dimensional valley depth):

$$Fr = \frac{U}{NH} \quad (1)$$

133 where U is the mean wind above the valley, N is the Brunt–Väisälä frequency, and H is the
 134 valley depth (Bell and Thompson, 1980; Tampieri and Hunt, 1985; Lee et al. 1987). Bell and
 135 Thompson (1980) found that when $Fr \geq 1.2$, the flow tends to sweep through a valley de-
 136 spite the stratification. Other studies have shown that, in addition to Fr , the terrain geometry,
 137 including ridge spacing, slope angle, and the wavelength of lee waves all affect the character
 138 of the flow into the valley (Tampieri and Hunt, 1985; Lee et al. 1987).

139 Relatively few observational studies have focused on the breakup of CAPs. Whiteman et
140 al. (2001) document the differing destructive processes during two CAPs in the Columbia
141 River Basin, one being affected by strong down slope winds and the other by cold-air advec-
142 tion and internal convection. Rakovec et al. (2002) examined turbulent processes during the
143 breakup of CAPs in a Slovenian mountain valley. Using field observations and numerical ex-
144 periments, they show that turbulent erosion commences above a threshold wind speed and
145 continues if the flow accelerates. Flamant et al. (2006) examined the interaction of foehn
146 winds with a CAP in the Rhine Valley during the Mesoscale Alpine Project. They conclude
147 that CAP displacement along the valley axis is primarily caused by advection within the
148 foehn flow, but also show that Kelvin-Helmholtz and gravity waves affect the CAP to a lesser
149 degree.

150 In this study, we use data collected in the Salt Lake Valley of northern Utah during the
151 Persistent Cold-Air Pool Study (PCAPS, Lareau et al. 2013) to examine the passage of a
152 short wave trough during a multi-day CAP. This trough-CAP interaction produced a variety
153 of waves, displacement and fronts that disrupted the otherwise quiescent CAP. In the follow-
154 ing sections we analyze the observed changes in CAP structure and develop a simple concep-
155 tual model for the trough-CAP interaction based on the observations and an idealized numer-
156 ical simulation using a Large-Eddy Simulation version of the Weather Research and Fore-
157 casting (WRF-LES) model (Skamarock et al. 2008).

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159

160 2 The Salt Lake Valley and Meteorological Data

161

162 2.1 The Salt Lake Valley

163

164 The Salt Lake Valley (SLV) is located in northern Utah, USA at the eastern edge of the semi-
165 arid intermountain west, which is the region between the Sierra Nevada and Rocky Moun-
166 tains. CAPs are common in the SLV during winter, affecting the nearly 1 million residents.
167 The meridionally-oriented valley is confined to the east and west by the Wasatch (~2800 m)
168 and Oquirrh (~2400 m) Mountains, respectively (Fig. 1). To the south, the Traverse Moun-
169 tains (~1800 m), which have ~500 m of relief, act as a partial barrier separating the SLV from
170 the neighboring Utah Valley. The SLV opens to the northwest into the Great Salt Lake Basin.
171 The lowest elevations in the SLV are found along the Jordan River, which slopes downward
172 from ~1400 m as it enters the SLV through the Jordan Narrows, a gap through the Traverse
173 Mountains, to ~1280 m at the shore of the Great Salt Lake. East-west asymmetries in the
174 SLV have large impacts during CAPs: (1) there is more landmass at a given elevation to the
175 west of the Jordan River, and (2) north-south flow is blocked more to the east of the River
176 than to its west.

177

178 2.2 Meteorological Data

179

180 The meteorological data used in this study were collected during the PCAPS Intensive Ob-
181 serving Period 1 (IOP-1). IOP-1 examined a multi-day CAP that formed on 1 December and
182 lasted through late on 6 December 2010. We describe here the key observational resources
183 that are used in this study, the locations of which are shown in Fig. 1. An overview of PCAPS
184 and all available data resources are provided by Lareau et al. (2013).

185 To diagnose the evolution of the IOP-1 CAP, we construct time-height profiles of tem-
186 perature, potential temperature, relative humidity, and wind intended to be representative of
187 the conditions within the central core of the SLV. For this purpose, we rely most heavily on

188 the data collected at the Integrated Sounding System (ISS) sites labeled by blue dots in Fig. 1,
189 which are on bluffs immediately to the west of the Jordan River. A 915 MHz radar wind
190 profiler (RWP) and Radio Acoustic Sounding System (RASS) were operated continuously at
191 ISS-N, while radiosondes were launched at 3-12 h intervals from ISS-S, ~1 km to the south,
192 depending on the operational plan for the field program. We constrain these vertical profiles
193 near the surface by automated weather observations at ISS-S and also use radiosonde data
194 from the Salt Lake International Airport (KSLC; black dot in Fig. 1) above the boundary lay-
195 er to improve the temporal coverage for periods when sondes were not launched at ISS-S.
196 Gaps in the remote sensor data due to low signal-to-noise ratios are filled objectively using an
197 “inpainting” analysis technique (Schönlieb 2012) and bounded by surface and radiosonde da-
198 ta at the gap boundaries. The resulting time-height profiles are quality controlled to remove
199 spurious unphysical values and gradients and then averaged linearly with interpolated time-
200 height profiles from the radiosonde data alone. The final set of time-height profiles reflect an
201 effective blend of the remote sensor and in situ observations at a temporal interval of 30
202 minutes and a vertical resolution of ~50 m. These profiles are representative of the conditions
203 throughout most of the SLV during this CAP except during the Disturbance Phase, described
204 later, when these profiles reflect conditions near the ISS sites only.

205 A laser ceilometer located at ISS-S is used to characterize the mixing depth of aerosol, the
206 presence of hydrometeors, and fine-scale structures within the boundary layer at 16 s tem-
207 poral resolution (Young 2013). Two pseudo-vertical transects along the confining topography
208 are created based on lines of near-surface sensors running up the sidewalls. The first transect
209 is composed of 6 automatic weather stations ascending the Traverse Mountains in the south-
210 east corner of the valley (yellow dots in Fig. 1 with SM6 located on the valley floor at an ele-
211 vation of 1370 m while SM1 is on the Traverse Mountain ridgeline at an elevation of 1930
212 m). These stations were equipped with wind, temperature, humidity and pressure sensors and
213 recorded data every 5 minutes. The second transect uses HOBOTM temperature data loggers
214 aligned along Harker’s Ridge, which is a sub-ridge along the east slope of the Oquirrh Moun-
215 tains (northern string of green dots in Fig. 1). The HOBOS also report temperature every 5
216 minutes and are spaced vertically at ~50 m intervals from 1350 to 2500 m.

217 Data from over fifty surface weather stations within the SLV with diverse suites of sensors
218 are used from the Mesowest archive (Horel et al. 2002). In addition, seven 10-m Integrated
219 Surface Flux System (ISFS) stations providing radiation, kinematic flux, and ground probe
220 sensors as well as standard weather variables were deployed around the Salt Lake Valley as
221 part of PCAPS (numbered in purple dots in Fig. 1).

222

223

224 3 Results

225

226 3.1 IOP-1 Overview

227

228 Wei et al. (2013) describe the conditions from 30 November – to 7 December 2010 that
229 encompass IOP-1 without relying on the PCAPS field campaign data, i.e., they examined
230 KSLC radiosonde and Mesowest surface observations in combination with a WRF model
231 simulation. Based on all the PCAPS data now available, we show that the IOP-1 CAP
232 progressed through 4 stages in its life cycle: formation, disturbance, persistence, and break-up
233 (Fig. 2). This paper primarily examines the disturbance phase, but here we briefly summarize
234 the event in its entirety.

235

236 3.1.1 Formation

237
238 The IOP-1 CAP followed the passage of a strong shortwave trough, which brought snow and
239 cold temperatures to the SLV. The CAP was then initiated by mid-tropospheric ridging and
240 warming, which formed a capping layer of strong static stability that decoupled the cold val-
241 ley atmosphere from the flow above crest level (Wei et al. 2013).

242 The strength of the nascent CAP was subsequently augmented by a surface based radiation
243 inversion forming during clear skies overnight on 2 December (see Fig. 2a, b). Averaged over
244 the seven ISFS stations, the net radiative cooling in the valley on that night is the strongest
245 during the CAP episode (Fig. 2a). Combined, the warming aloft and cooling at the surface
246 yielded a ~ 700 m deep CAP with a surface potential temperature deficit (relative to that near
247 the top of the CAP) in excess of 15 K at 12 UTC 2 December. Weak winter insolation, high
248 albedo due to snow cover, and the strong stability suppressed the growth of the convective
249 boundary layer the following afternoon, which allowed the CAP to persist and for aerosol to
250 accumulate rapidly (Fig. 2b). Concentrations of small particulates surpassed the National
251 Ambient Air Quality Standard (U.S. EPA 2013) of $35\text{-}\mu\text{g m}^{-3}$ after just the second day of the
252 cold pool (Fig. 2c).

253 254 *3.1.2 Disturbance*

255
256 The disturbance phase of IOP-1 occurred on 3 December as the initial ridge broke down and
257 a weak shortwave trough accompanied with mid-level clouds moved across the Intermoun-
258 tain West (Fig 3). The approaching trough generated a compact regional pressure gradient
259 that accelerated southerly winds above the CAP, reaching a peak approaching $\sim 20\text{ m s}^{-1}$ dur-
260 ing the early morning of 3 December (Fig. 4). Terrain channeling controlled the orientation of
261 the flow in the SLV, leading to ageostrophic south winds blowing along the valley axis and
262 down the regional pressure gradient (not shown).

263 As the winds increased aloft, the CAP thinned from ~ 700 m at 00 UTC 2 December to
264 ~ 150 m at 06 UTC 3 December (Fig. 4). The downward slope of the isentropes within the
265 capping layer of strong static stability is partially due to increased warm air advection associ-
266 ated with the strengthening southerly flow and, as we show later, also due to tilting and dis-
267 placement of the CAP.

268 Surface conditions at station SM6 on the valley floor at the extreme southern end of the
269 SLV and immediately in the lee of the Traverse Mountains (Fig. 5) remained quiescent
270 (speeds less than 3 m s^{-1}) and were similar to those observed throughout most of the SLV un-
271 til 00 UTC 3 December at which time the first burst of warm ($>10\text{ }^\circ\text{C}$), dry (dew point tem-
272 peratures $< -5\text{ }^\circ\text{C}$), and windy (speeds greater than 7.5 m s^{-1}) conditions penetrated for a brief
273 time to the surface. CAP conditions resumed at this location until 03 UTC followed by a se-
274 cond intrusion of warm, dry, windy conditions through 0830 UTC (Fig. 5). Another short pe-
275 riod of CAP conditions was followed by the third warm, windy burst from 10-13 UTC. The
276 causes for these abrupt changes in surface conditions are explored throughout this paper.

277 The disturbance period in the valley concludes after ~ 15 UTC 3 December as the trough
278 axis passes over the region bringing a sharp reduction in the winds aloft and surface condi-
279 tions at the south end of the valley return roughly to those observed the day before (Fig. 5).
280 Hence, the disturbance period is more complicated than the hypothesis provided by Wei et al.
281 (2013) that it was due to the passage of a weak cold front.

282 283 *3.1.3 Persistence*

284

285 Following the trough's departure, the CAP returns to a quiescent state, providing continued
286 cold temperatures and high levels of pollution as ridging builds over the intermountain west
287 on 4-6 December (Fig. 2). During this phase, the CAP eventually developed a stratocumulus-
288 capped boundary layer and periods of surface fog (red shading Fig. 2b) leading to travel de-
289 lays and, unfortunately, contributing to the crash of a small aircraft to the north of the SLV
290 near Ogden, UT on 6 December.

291

292 *3.1.4 Breakup*

293

294 The long-lived IOP-1 CAP was finally destroyed late on 6 December by cold-air advection
295 aloft, internal convection, and enhanced winds associated with a much stronger shortwave
296 trough moving into the region (Wei et al. 2013). The breakup of the valley stratification was
297 accompanied by a reduction in the particulate pollution and a return to healthier air quality
298 (Fig. 2).

299

300 *3.1.5 Forecast Uncertainty*

301

302 During this CAP event, forecasting the extent of the trough-CAP interaction on 3 December
303 was particularly difficult. Operational and research numerical weather prediction guidance
304 did not resolve the details associated with this weak trough passage and the limited impact it
305 had on improving air quality in the valley. For example, while the retrospective research sim-
306 ulations completed by Wei et al. (2013) captured many of the general features associated with
307 IOP-1, their simulation fared poorly during the Disturbance Phase with wind speed and direc-
308 tion errors as large as 10 m s^{-1} and 90° respectively, and temperature errors greater than 2.5°
309 C below 700 hPa. To better understand the unresolved processes that contributed to the CAP
310 evolution during the Disturbance phase, we now turn to detailed analyses of PCAPS observa-
311 tions.

312

313 3.2 Surface Temporal Evolution

314

315 The abrupt changes in surface meteorological conditions evident in Fig. 5 are caused by a se-
316 quence of displacements of the CAP along the valley axis. To better understand these dis-
317 placements, hourly surface temperature gridded analyses at $\sim 100 \text{ m}$ horizontal resolution are
318 created from all available surface temperature observations using a Barnes horizontal dis-
319 tance weighting (Barnes 1964) of the departures of the observed temperatures from the tem-
320 perature estimated for that elevation from the hourly vertical profiles of temperature de-
321 scribed in Section 2b (Figs. 6-9). The relatively dense network of temperature observations
322 available in the SLV during this IOP reduces the sensitivity of the resulting analyses to the
323 technique, e.g., very similar temperature analyses have been obtained for this period using a
324 two-dimensional variational analysis technique (Tyndall and Horel 2012).

325 The overall dependence of temperature on elevation is immediately apparent from the sur-
326 face temperature observations and analyses in Figs. 6-9. For example, the string of HOBO
327 temperature sensors along Harker's Ridge (Fig. 1) at 0000 UTC (Fig. 6a) transitions from low
328 temperatures (blue shades) in the valley to much higher temperatures on the western slopes of
329 the valley (yellow and orange shades) before again dropping at the upper reaches of the
330 Oquirrh Mountains (blue shades). Prior to 0000 UTC, the temperatures in the lowest eleva-
331 tions of the SLC were nearly uniform (not shown).

332 The first CAP displacement in the valley is evident at 0000 UTC, where the leading edge
333 of the CAP is shifted northward, forming a roughly east-west frontal zone (Fig. 6a). Warm air

334 (5-10° C) and southerly winds penetrate to the surface to the south of the front, while cold air
335 (~0° C) and northerly winds are present to the north. This initial CAP displacement is re-
336 versed over the next two hours (Fig. 6 b, c) as the CAP edge advances southward at the low-
337 est elevations, eventually abutting the Traverse Mountains to the east of the Jordan Narrows.
338 The southwest corner of the valley remains out of the CAP at that time with southerly flow
339 continuing over the Traverse Mountains in that region.

340 A second northward CAP displacement is initiated at ~0300 UTC as strong winds and
341 warm temperatures again surface along the southeastern portions of the valley (Fig. 5 and
342 Fig. 6d). The southerly flow is particularly strong and warm along the lee slopes of the Trav-
343 erse Mountains. The edge of the CAP then moves progressively northward through the val-
344 ley, reaching its northernmost excursion at ~0600 UTC (Fig. 7 a,b,c). At that time high tem-
345 peratures (~10° C) and strong southerly winds (7-10 m s⁻¹) are reported throughout the south-
346 ern 2/3 of the valley, while light winds and temperatures around 0° C persist within the dis-
347 placed CAP. The temperature gradient across the leading edge of the CAP is ~10° C over 2
348 km. The pronounced tendency for the displacement of the CAP to be enhanced over the west-
349 ern portion of the SLV arises in part from its higher elevation as well as the unimpeded flow
350 towards the Great Salt Lake on that side of the Valley.

351 Despite continued strong southerly flow aloft, the leading edge of the CAP again reverses
352 course between 0700 and 0800 UTC, returning southward through the valley (Fig 7d and 8a).
353 As the cold air advances, winds to the north of the front become coherent in strength and di-
354 rection, flowing from the NW to SE then turning south along the valley axis (Fig. 8a).
355 Meanwhile, strong south winds continue to the south of the front indicating convergence
356 along the leading edge of the cold air. As the CAP subsumes observing sites throughout the
357 valley, the cold frontal temperature drop is nearly identical in magnitude to the previous
358 warm frontal rise, which produces the step changes apparent in individual time series (e.g.,
359 Fig. 5). By 0900 UTC (Fig. 8b), the cold front encroaches on the Traverse Mountains in the
360 southeastern sections of the SLV. As before, high temperatures and strong winds continue
361 along the southwestern portion of the valley and near the crest of the Traverse Mountains.

362 The third and final CAP displacement commences between 1000 and 1200 UTC as the
363 frontal boundary again moves northward re-establishing a position across the valley center
364 (Fig. 8c,d and Fig. 9a). This third displacement is shorter lived, and as the winds aloft dimin-
365 ish after 1200 UTC (Fig. 4), the cold front mobilizes southward for the final time (Fig. 9b).
366 By 1500 UTC (Fig. 9d), the CAP has returned throughout the valley and penetrates south
367 through the Jordan Narrows into the neighboring Utah Valley. This reversal in the gap flow
368 effectively marks the end of the disturbed CAP conditions and a return to the quiescent and
369 horizontally homogenous CAP ensues.

370 3.3 Mountain Wave

371
372
373 The north-south displacements of the CAP evident in the hourly surface temperature analyses
374 and other earlier figures result in part from the southerly flow crossing over the Traverse
375 Mountains into the SLV. The vertical profiles of potential temperature and wind speed up-
376 stream of the Traverse Mountains are shown at 0600 UTC 3 December in Fig. 10a, which
377 corresponds to the furthest northward displacement of the CAP. Disregarding the sharp sur-
378 face-based radiational inversion, the profiles suggest upstream conditions can be character-
379 ized at that time as a two-layer stably-stratified fluid: nearly constant wind speed and poten-
380 tial temperature above 1750 m with 6K lower potential temperature below 1650 m with in-
381 creasing wind speeds through the lower layer and extending into the intervening strong stable
382 layer.

383 Ignoring the surface based inversion, it is possible to compute the internal Froude number
 384 from this profile as
 385

$$Fr = \frac{U}{g'h} \quad (2)$$

386 where U is the mean wind speed ($\sim 6 \text{ m s}^{-1}$), h is the height of the interface ($\sim 300 \text{ m}$),
 387
 388

$$g' = \frac{\Delta\theta}{\theta} g \quad (3)$$

389 is the reduced gravity where $\Delta\theta$ is the change in temperature across the capping layer ($\sim 6 \text{ K}$)
 390 and θ is the mean profile temperature ($\sim 297 \text{ K}$). With these approximations $Fr \approx 0.8$, indicat-
 391 ing that the upstream mean flow is slightly slower than the fastest linear shallow water gravi-
 392 ty waves. It is likely, then, that as the flow passes over the crest of the Traverse Mountains
 393 and thins (e.g., h reduced to $\sim 100 \text{ m}$) it transitions to a super-critical state ($Fr > 1$). Following
 394 the hydraulic flow analogy, such a flow is expected to produce a mountain wave with strong
 395 downslope winds with non-linear effects including a downstream hydraulic jump (Durrant
 396 1986). Similar flows have previously been documented over the Traverse Mountains during
 397 diurnal CAPs by Chen et al (2004).
 398

399 The impact of the mountain wave along the fall line of the Traverse Mountains is shown in
 400 Fig. 10c. Consider first the conditions at the time of the upstream sounding (0600 UTC). All
 401 stations from the ridge crest (SM1) to the valley floor in the lee (SM6) report the same poten-
 402 tial temperature, $\sim 297 \text{ K}$, which is consistent with air in the upstream stable layer at $\sim 1700 \text{ m}$
 403 being lifted up and over the ridge while the lower upstream layers are blocked by the barrier.
 404 Wind speeds at the crest (SM1- black curve) and near the valley floor (SM5- red; SM6- dark
 405 blue respectively) are equally strong at this time and occasionally the winds at the base of the
 406 slope are stronger, reflecting acceleration of the flow. (Consistently weaker winds at interven-
 407 ing sites, such as SM4, light blue curve, reflect siting more than atmospheric conditions.)

408 The pulsing of mountain-waves throughout the Disturbance phase causes the along-slope
 409 potential temperature profile to abruptly switch between stratified and adiabatic states (Fig.
 410 10c). For example, the ridge-to-valley potential temperature difference is $\sim 12 \text{ K}$ at 0250
 411 UTC, whereas just 20 minutes later it is nearly zero (a reminder that Fig. 5 is the blue curve
 412 in Fig. 10 c, d). Periods of along-slope adiabatic flow are accompanied by the penetration of
 413 strong southerly winds to the valley floor, whereas weak northerly flow near the valley floor
 414 coincides with stratification. The restratification of the CAP once the southerly flow lessens
 415 is clearly evident after 1300 UTC with no change in the conditions at the top (SM1) and pro-
 416 gressively lower potential temperatures down the lee slope into the valley.

417 To visualize in greater detail the impact of the flow across the Traverse Mountains, an ide-
 418 alized quasi-two dimensional Large-Eddy-Simulation is shown in Fig. 11. The simulation is
 419 initialized from temperature and wind profiles similar to those shown in Fig. 10a and uses a
 420 50 km cross section of the SLV beginning south of the Traverse Mountains, extending north
 421 across the ISS sites, and terminating at the Salt Lake International Airport. The domain is 1
 422 km wide to allow 3-D turbulence and uses open boundary conditions at the downwind (north-
 423 ern) boundary and a Rayleigh damping layer at the southern boundary that maintains a con-
 424 stant inflow profile. The near-surface inversion in the upstream sounding is extrapolated to

425 match the observed surface temperature ISS-S within the SLV, which was 285 K. Radiation
 426 is neglected, as are sensible heat fluxes at the surface, and friction is parameterized using a
 427 Monin-Obukov surface layer scheme. The horizontal grid spacing is 50 m and there are 100
 428 vertical levels stretched over 10 km. The vertical resolution is nominally 30-50 m within the
 429 valley. The simulation is run for 1-hr to capture the immediate response of the downstream
 430 CAP to the upstream stratified flow over the topography.

431 After 1 h, a pronounced mountain wave, hydraulic jump, and CAP displacement are ap-
 432 parent (Fig 11b). The low-level upstream flow is partially blocked such that the depth of the
 433 cold lower layer increases until it surmounts the ridge and spills down the lee-slopes. As we
 434 speculated above, the Froude number at the mountain crest exceeds the critical value within
 435 the overtopping flow. The flow aloft behaves similarly, represented by perturbations in the
 436 height of the 300 K isentrope. Accompanying the thermal perturbation of the wave is a
 437 marked increase in wind speed above the ridge crest and extending down the lee slope. The
 438 lee-side along-slope flow is ostensibly adiabatic with constant speed in excess of 10 m s^{-1} ,
 439 consistent with observations in Fig. 10c,d.

440 The flow separates from the surface near the base of the lee slope in a pronounced hydrau-
 441 lic jump. The presence of the upstream inversion layer is well known to favor such hydraulic
 442 jumps, lee waves, and boundary layer separation (Vosper 2004; Jiang et al. 2007). The sur-
 443 face flow within the jump region is reversed and the air becomes turbulently mixed, reducing
 444 the stratification and eroding the surface based inversion. Consequently a front forms separ-
 445 ating the comparatively quiescent near-surface CAP conditions to the north from the better-
 446 mixed and windier conditions to the south.

447 The front shown in the numerical simulations suggests a link between the strength of the
 448 mountain wave and the timing of the CAP advance and retreat throughout the valley. For ex-
 449 ample, the northward displacement of the CAP between 0300 and 0600 UTC correspond to a
 450 time of increased downslope flow, whereas the frontal reversal is linked with a modest de-
 451 crease in the strength of the downslope winds.

452

453 3.4 Advance and Retreat of the CAP

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455 While the mountain waves caused the CAP to retreat and advance in the extreme southeastern
 456 end of the SLV three times on 3 December, a single disruption of the CAP was centered near
 457 0600 UTC 3 December at the ISS sites (Fig. 2). Figure 12 shows in more detail this ~ 3 h pe-
 458 riod when the CAP retreated northward past the ISS sites temporarily providing clean air
 459 (low aerosol backscatter). The retreat of the CAP is synonymous with the passage of a warm
 460 front, which is marked by a gradual reduction in the height of the aerosol layer followed by
 461 rapid reduction in aerosol concentration, a 7 K temperature rise, and a burst of strong souther-
 462 ly winds (Fig. 12). As the front continues northward past ISS-S, there is a ~ 12 minute lag be-
 463 fore its passage at ISS-N, which is one kilometer away, giving a propagation speed in the
 464 along valley direction of $\sim 1.5 \text{ m s}^{-1}$. Using these values, the width of the frontal zone is ~ 1
 465 km and the front-normal temperature gradient is $\sim 7 \text{ K km}^{-1}$. The winds on the warm side of
 466 the front are around 8 m s^{-1} from the south while those within the CAP are nearly zero.

467 Figure 13 shows a radiosonde launched at ISS-S just 5 minutes before the warm front
 468 passes. The sounding ascends through a sharp surface inversion and a strongly stable capping
 469 layer. The depth of the stable layer has clearly diminished leading up to this launch (cf. Fig.
 470 2). As the front passes and the surface potential temperature increases by 7 K, the thin sur-
 471 face-based inversion layer is removed and replaced by a shallow well-mixed layer beneath
 472 the still present capping layer. Based on the model simulation shown in Fig. 11 and dynam-
 473 ical reasoning associated with mountain lee waves, it is likely that the sharply higher poten-

474 tial temperature and cleaner air behind the warm front is associated with the air flowing from
475 aloft upstream of the Traverse Mountains descending into the SLV and mixing with the much
476 colder air within the CAP.

477 In contrast to the gradual thinning and quiescent prefrontal conditions associated with the
478 warm front, the cold front arrives with strong northerly winds ($4\text{-}5\text{ m s}^{-1}$) and an abrupt 200 m
479 increase in the depth of the aerosol layer (Fig. 12). This frontal “head” is shown in more de-
480 tail in Fig. 14 and moves much more quickly than the warm front, advancing between the ISS
481 sites in just 5 minutes, giving a propagation speed of $\sim 3.5\text{ m s}^{-1}$, which is more than twice
482 that of the warm front. The northerly flow within the cold air behind the front combined with
483 the opposing southerly flow of $\sim 5\text{-}7\text{ m s}^{-1}$ implies strong convergence.

484 In the wake of the frontal head, the aerosol layer depth decreases and high amplitude
485 waves develop (Fig 14). This morphology is consistent with the characteristics of an advanc-
486 ing gravity current, e.g. an elevated head, convergent opposing flow, and mixing via Kelvin-
487 Helmholtz waves behind the front (Simpson 1997). Moreover, the ceilometer data suggest
488 that the upstream two layered air mass (Fig 14) is lifted over the gravity current head (high
489 aerosol backscatter), with evidence of the frontal disturbance as much as 300 m AGL. This
490 evolution closely resembles laboratory and numerical simulations of gravity currents propa-
491 gating into a two layer stratified environment (Simpson 1997; White and Helfrich 2012).

492 The differences between the retreat and advance of the CAP likely relates to differences in
493 the front-relative shear profiles, which profoundly influence gravity current dynamics (Mar-
494 kowski and Richardson 2010). During the warm frontal passage, the CAP advances in the
495 same direction as the upstream wind and opposite to the shear vector. Such sheared profiles
496 generally produce low amplitude gravity current heads. In contrast, the cold front has strong
497 flow within the lowest layers of the cold-air and propagates against the ambient flow such
498 that the front-relative shear vector is reduced, which leads to a taller frontal head, stronger
499 updraft, and more vigorous mixing behind the front (Simpson 1997; Markowski and Richard-
500 son 2010). Previous investigations of gravity currents have found that the mixing behind the
501 frontal nose can strongly impact heat and momentum fluxes within the stable boundary layer
502 (Sun et al. 2002).

503 504 3.5 CAP Tilt

506 The model simulation in Fig. 11 suggests that the displaced CAP may be inclined to the north
507 such that the depth of the cold air increases over the span of the SLV, particularly considering
508 that the valley is sloping downwards as well. Fig. 15 contrasts the vertical profiles of poten-
509 tial temperature and wind over a distance of 19.2 km between ISS-S and KSLC near the end
510 of the Displacement Phase. The depth of the CAP at KSLC is clearly 200 m deeper than at
511 ISS-S when the leading edge of the CAP is located ~ 3 km to the south of ISS-S.

512 CAPs are known to develop such sloping surfaces in response to both static and dynamic
513 forcing. The static response is the CAP adjustment to the regional pressure gradient
514 (Petkovšek and Vrhovec 1994, Zängl 2003) while the dynamic response relates to the wind
515 stress across the top of the CAP (Petkovšek and Vrhovec 1994, Gubser and Richner 2001).
516 Following Zängl (2003), the magnitude and shape of the static displacement can be approxi-
517 mated by

$$\Delta z = T \frac{\overline{\frac{dP}{dx}}}{Pg\Delta\gamma} \overline{\Delta x} \quad (4)$$

518 where T , P , and $\frac{dP}{dx}$ are representative values for the temperature, pressure, and pressure gra-
 519 dient immediately above the CAP and $\Delta\gamma$ is the difference between the CAP and ambient
 520 lapse rates. The expression indicates that the depth of the cold-air is proportional to the
 521 square root of the distance from the leading edge of the cold air and that the smaller the lapse
 522 rate differences, the greater inclination of the CAP required to balance the regional pressure
 523 gradient (Zängl 2003).

524 Using values derived from the soundings shown in Fig. 15 and an estimate of the large-
 525 scale pressure gradient from ERA-interim reanalyses at 12 UTC ($\sim 1.25 \times 10^{-3} \text{ Pa m}^{-1}$) we su-
 526 perimpose onto Fig. 15 (blue triangle) the estimated depth of the CAP at KSLC from (4).
 527 This approximation underestimates the depth of the cold-air by $\sim 150 \text{ m}$ at KSLC. It is likely
 528 then that dynamical wind stresses impact the CAP structure as well.

529 To account for the dynamic component of the displacement, we consider an antitriptic bal-
 530 ance (Sun et al. 2013) between the perturbation pressure gradient within the CAP and the
 531 momentum flux convergence due to Reynolds shear stress across the cold-pool top
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$$\frac{1}{\rho} \frac{\partial P'}{\partial x} = \frac{\partial u'w'}{\partial z} \quad (5)$$

533 Following Li et al. (2009), the pressure perturbation at the surface can be determined from
 534 the vertically integrated temperature anomalies
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 536

$$\begin{aligned} P' \Big|_{z=0} &\approx \frac{\rho g}{T} \int_{z=0}^{z=\Delta z} T' \Big|_z dz \\ &\approx \frac{\rho g \gamma}{T} \frac{\Delta z^2}{2} \end{aligned} \quad (6)$$

537 Where ρ and T are reference values for density and temperature, Δz is the vertical CAP dis-
 538 placement away from horizontal, and γ is the lapse rate, which is assumed to be constant. In-
 539 tegrating (6) once within the CAP and once within the warm air, the internal pressure gradi-
 540 ent is then approximated as
 541

$$\frac{1}{\rho} \frac{\Delta P'}{\Delta x} \approx \frac{g\Delta\gamma}{2T} \frac{\Delta z^2}{\Delta x} \quad (7)$$

542
 543 Where $\Delta\gamma$ is again the difference in lapse rates. Next, we approximate the momentum flux
 544 divergence as
 545

$$\begin{aligned} \frac{\partial u'w'}{\partial z} &\approx \frac{u'w'_{top} - u'w'_{bot}}{H} \\ &\approx \frac{k_m \frac{\partial u}{\partial z}}{H} \approx k_m \frac{\Delta u}{H^2} \end{aligned} \quad (8)$$

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where we assume that the momentum flux at the top of the layer is much greater than at the surface, H is the depth of the shear layer, and ΔU is the wind speed difference across H . The eddy diffusivity for momentum, k_m , is itself a function of the flow, and can be approximated for the ‘‘upside boundary layer’’ based on the Richardson number (Kim and Mahrt 1992).

Combining (7) and (8) and then solving for the dynamic displacement yields

$$\Delta z_{dyn} = \frac{2T}{g} \frac{k_m \Delta u}{H^2 \Delta \gamma} \overline{\Delta x}. \quad (9)$$

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Again using values from the soundings in Fig. 15 ($H = 400$ m, $T = 280$ K, $\Delta u = 17$ m s⁻¹, $k_m = 3$ m² s⁻¹, $\Delta \gamma = 2.98 \times 10^{-2}$ K m⁻¹) we compute Δz_{dyn} and add the result to the static displacement. The resulting approximation for the idealized CAP top matches more closely the elevation difference of the CAP at ISS-S and KSLC (cyan triangle, Fig. 15).

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We conclude, then, that the observed CAP geometry reflects a three-way balance between the perturbation pressure gradient, the pressure gradient aloft, and the wind stress. This balance can, however, be easily disrupted by changes in the wind speed. For example a sudden decrease in the wind shear would cause the internal pressure gradient to be out of balance, and prompt a southward rush of cold-air until a new balance is established. This may help explain the advance and retreat of the CAP that was described in the above sections as well as the gravity current characteristics of the advancing cold air.

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3.6 Kelvin-Helmholtz Instability

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Many high frequency (order minutes) waves are observed during IOP-1 (cf. Fig. 11). Amongst these waves we are particularly interested in those resulting from Kelvin-Helmholtz instability, which is a dynamic instability occurring in stratified shear flows when the kinetic energy available from shear exceeds the work required to move a parcel against the stratification. When this condition is met, Kelvin-Helmholtz waves (KHW) develop, evolving from small perturbations into breaking waves that mix properties across the stratification (Nappo 2002). Formally this condition is given by the gradient Richardson number,

$$Ri = \frac{N^2}{\frac{\partial u}{\partial z}^2 + \frac{\partial v}{\partial z}^2} \quad (10)$$

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where N is the Brunt–Väisälä frequency, and the terms in the denominator are the components of the vertical shear. KHW are an important mixing mechanism in stratified geophysical flows (Fernando 1991) and have been regularly documented in the stable boundary layer and CAPs, often associated with low-level jets (Newsom and Banta 2003; Pinto et al. 2006; Flamant et al. 2006).

583 During IOP-1, KHW are first observed during the onset of the accelerating winds aloft.
 584 For example, Fig. 16a shows a sequence of high frequency (~ 1 cycle per minute) waves that
 585 culminate in a pronounced KHW billow that inverts the aerosol gradient within the wave
 586 crest. The folding of low aerosol air beneath high aerosol air suggests that these waves mix
 587 pollution from near the surface into the layers aloft, and presumably act similarly on the tem-
 588 perature profile.

589 A contemporaneous sounding at KSLC shows that the KHW are centered within a weakly
 590 stable layer between the surface-based inversion and the capping layer aloft. The wind shear
 591 across this layer is modest, but the Richardson number is nonetheless near the critical value
 592 for KHI ($Ri < 0.25$) due to the reduced static stability in that layer

593 At ~ 0400 UTC 3 December, winds aloft increase to $\sim 10 \text{ m s}^{-1}$ and KHW become a domi-
 594 nant feature in the aerosol backscatter profiles at ISS-S. Figure 16b shows a sequence of these
 595 KHW wherein 100 m amplitude waves occur once every 3 minutes. The first three waves
 596 successively grow in amplitude, and the 4th and 5th waves appear to have broken down into
 597 turbulence or smaller scale waves. The Richardson number, here evaluated from our time-
 598 height data, is near critical over a deep layer. However, since the time-height temperature and
 599 wind data lack the vertical and temporal resolution to resolve fine scale structures in the CAP,
 600 it is likely that the minimum values for Ri are lower than those calculated here.

601 Later, at ~ 1100 UTC 3 December (Fig. 16c), the winds aloft reach their peak strength of
 602 $\sim 15 \text{ m s}^{-1}$ and strong shear extends over the depth of the CAP. In fact, the shear is now en-
 603 hanced by a counter current of northerly flow near the surface associated with the southward
 604 motion of the CAP. Correspondingly, Ri is reduced to near its critical value over most of the
 605 CAP depth. The KHW now have amplitudes upwards of 200 m, and appear to loft aerosols
 606 deep into the clear air above. The dominant period of these waves remains ~ 3 minutes.

607 As evident in earlier results as well, it is interesting to note that the CAP is not destroyed
 608 despite the strong wind shear, near critical Ri , and active KHW. Competing processes must
 609 offset the turbulent heat fluxes arising from the KHW, which would tend to remove the CAP
 610 stratification over time. We suspect that the vertical differential temperature advection across
 611 the CAP is responsible for maintaining its strength. For example, the northerly flow at the
 612 surface is continually feeding cold-air from deeper portions of the CAP into the region sur-
 613 rounding ISS, where these waves are active.

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616 3.7 Basin-Scale Internal Waves

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618 A noticeable feature of the Disturbance Phase of IOP-1 is the presence of SLV-scale internal
 619 waves. Relatively low frequency, long (basin-scale) wavelength phenomena such as
 620 baroclinic seiches are known to occur within stratified lakes (Csanady 1972; Monismith
 621 1985), but have not been thoroughly documented in atmospheric CAPs (Largeron et al. 2013).

622 Such basin-scale internal waves (BSIW) appear to be manifest during IOP-1 as oscillations
 623 in the depth of the CAP superimposed upon the broader trends associated with the passage of
 624 the short-wave trough (Fig. 17). Visual inspection of the potential temperature and aerosol
 625 backscatter profiles suggests that the waves have a period of ~ 3 hrs., and arrive with a steep
 626 increase in depth but then depart with a more gradual thinning. We attempt to isolate the
 627 properties of these BSIW by applying a 1-5 hr band-pass filter to independent time series of
 628 surface pressure at ISS-S (1-min resolution) as well as the 1500-1800 m layer-averaged me-
 629 ridional wind and potential temperature at ISS (Fig. 17b). This filter removes lower frequen-
 630 cy variations associated with synoptic-scale and diurnal fluctuations, high frequency varia-

631 tions due to micro-scale processes (e.g. KHW), and preserves the frequencies associated with
632 the waves of interest.

633 The filtered data show that increases in the depth of the aerosol layer tend to correspond to
634 increases in the surface pressure and decreases in layer mean temperature (Fig. 17b, i.e., a
635 deeper CAP with higher aerosol concentration is accompanied by higher pressure and lower
636 temperature). The meridional component of the wind generally reverses during the wave cy-
637 cle, oscillating between more northerly and southerly along valley flow. This wind reversal is
638 important in redistributing pollution within the CAP.

639 These oscillations are coherent over the scale of the SLV, appearing with comparable ampli-
640 tude (~ 1 hPa) at each of the 7 ISFS sites (Fig. 17c). There is an ~ 1 hr time lag between
641 ISFS1 and ISFS7, which are at the north and south ends of the valley, respectively, and sepa-
642 rated by about 31.4 km (see Fig. 2). Spectral analysis of these time-series confirms that the
643 dominant BSIW period is between 3 and 4 hrs (not shown).

644 To further demonstrate the link between surface pressure and CAP structure, we examine
645 one of these waves as it passes over the Harker's ridge transect between 0515 and 0845 UTC
646 2 December (Fig. 18a). From these profiles it is apparent that the oscillation takes the form of
647 rises and falls in the depth of the surface-based layer of cold air relative to a mean state. The
648 maximum amplitude in temperature variations occur within the layer between 1500 and 1800
649 m, which coincides with the transition layer that separates the surface-based nocturnal inver-
650 sion from the capping layer aloft. This residual layer is apparent in the individual profiles as a
651 nearly adiabatic lapse rate generally centered at about 1600 m.

652 We associate surface pressure perturbations with the temperature perturbations by integrat-
653 ing Eq. 6 over the height of the transect in Fig. 18a. Figure 18b shows the computed perturba-
654 tions as the wave passes and confirms that as the CAP rises (falls) the surface pressure in-
655 creases (decreases) by ~ 0.4 hPa, giving a total amplitude of ~ 0.8 hPa which is consistent with
656 the pressure perturbations measured throughout the valley (Fig 17c). The computed perturba-
657 tions also capture the steep initial rise followed by the more gradual thinning seen in the aero-
658 sol backscatter (Fig. 17a).

659 The exact causal mechanism and nature of these BSIW is as of yet unknown. They may
660 arise due to any of a number of forcings acting upon the stably stratified CAP. For example,
661 it is possible that they are a response to an external forcing, such as the increasing winds
662 aloft, or an internal forcing, such as katabatic flows or lake breezes that are known to occur
663 within the SLV during CAPs. Regardless of their source, these BSIW are an important factor
664 in local changes in the CAP. For example it is possible that these waves alter the CAP inter-
665 nal force balance and contribute to the advance and retreat of the cold air. Interestingly such
666 phenomena do not appear to be previously documented in CAP literature.

667 4 Summary and Conclusions

668 In this paper we have documented the complex evolution of a CAP that was disturbed by a
669 passing short-wave trough. We show that the initially horizontally homogenous stratified air
670 mass was disrupted by a series of along valley displacements, frontal passages, internal
671 waves, and turbulent mixing. To synthesize these elements of the trough-CAP interaction we
672 present here a schematic of the CAP evolution (Fig. 19) using insights from the observational
673 data and the numerical simulation.

674 The stages of the CAP disruption are as follows:

675 (a) At the onset, a quiescent and horizontally homogenous two-layered CAP resides in the
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680 valley. Synoptic scale warming aloft modulates the upper stable layer, while the surface based
 681 inversion is affected by diurnally varying sensible heat fluxes. The layers are partially
 682 separated by a residual layer of weaker stability (Fig. 19a).

683

684 (b) Winds above the CAP increase as a disturbance approaches. A mountain wave develops in
 685 the stratified cross barrier flow over the upstream topography, generating downslope warming
 686 and accelerated winds. The plunging flow displaces and erodes the surface inversion, forming
 687 a frontal interface. Increased shear leads to KHW, especially at the top of the surface
 688 inversion layer (Fig. 19b).

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690 (c) The CAP tilts upward in the down wind direction, establishing a force balance between
 691 the internal hydrostatic pressure gradient, the external pressure gradient, and the wind stress
 692 acting on the CAP. As the CAP tilts, its southern edge advances through the valley as a warm
 693 front, providing warmer, windier, and cleaner air to southern locales (Fig. 19c, note that in
 694 this panel the schematic includes observed potential temperatures from soundings and surface
 695 stations at ~1100 UTC 3 December).

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697 (d) Some perturbation, such as a temporary reduction in wind stress or a wave modulated
 698 change in depth, disrupts the CAP force balance. The CAP tilt partially collapses due to the
 699 unbalanced internal pressure gradient, sending a shallow density current propagating upwind
 700 through the valley and restoring the surface based inversion. Enhanced KHW mixing occurs
 701 in the wake of the density current (Fig. 19d).

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703 Stages b-d repeat as the force balance is restored leading to a sequence of frontal advances
 704 and retreats over upwind portions of the valley. Meanwhile northern locales remain within the
 705 CAP throughout the evolution. Finally, the winds aloft diminish and the CAP tilt collapses for
 706 a final time, restoring horizontally homogenous and quiescent CAP conditions throughout the
 707 valley.

708 While this simple schematic summary relies primarily on data from IOP-1, it nonetheless
 709 fits well with observations from many other CAPs, which are common in the SLV. For ex-
 710 ample, a similar sequence of step-like frontal temperature changes was observed at ISS-S
 711 during PCAPS IOP-4 (not shown). Moreover, many of the details of the IOP-1 CAP are simi-
 712 lar to the evolution of the CAPs described by Whiteman et al. (2001) and Flamant et al.
 713 (2006). Namely, a CAP is displaced in strong pre-frontal downslope winds leading to a warm
 714 front that provides partial or complete valley ventilation. In the present case, the CAP dis-
 715 placement is reversible, and CAP conditions are restored after winds abate. In other instances,
 716 however, a CAP may be completely removed, suggesting that irreversible turbulent mixing
 717 and spillover at the downwind end of the basin play an important role in CAP destruction.

718 We conclude by noting that many of the key features in the trough-CAP interaction are
 719 meso- and micro-scale processes that are typically either poorly resolved or altogether unre-
 720 solved in numerical forecast guidance. These unresolved processes strongly impact the CAP,
 721 and thus the forecasts for air quality. To further address the sensitivity of CAP removal to
 722 mountain waves, hydraulic jumps, KHW, and BSIW a companion study using a larger set of
 723 idealized large-eddy simulations than the single simulation used to generate Fig. 11 will be
 724 forthcoming.

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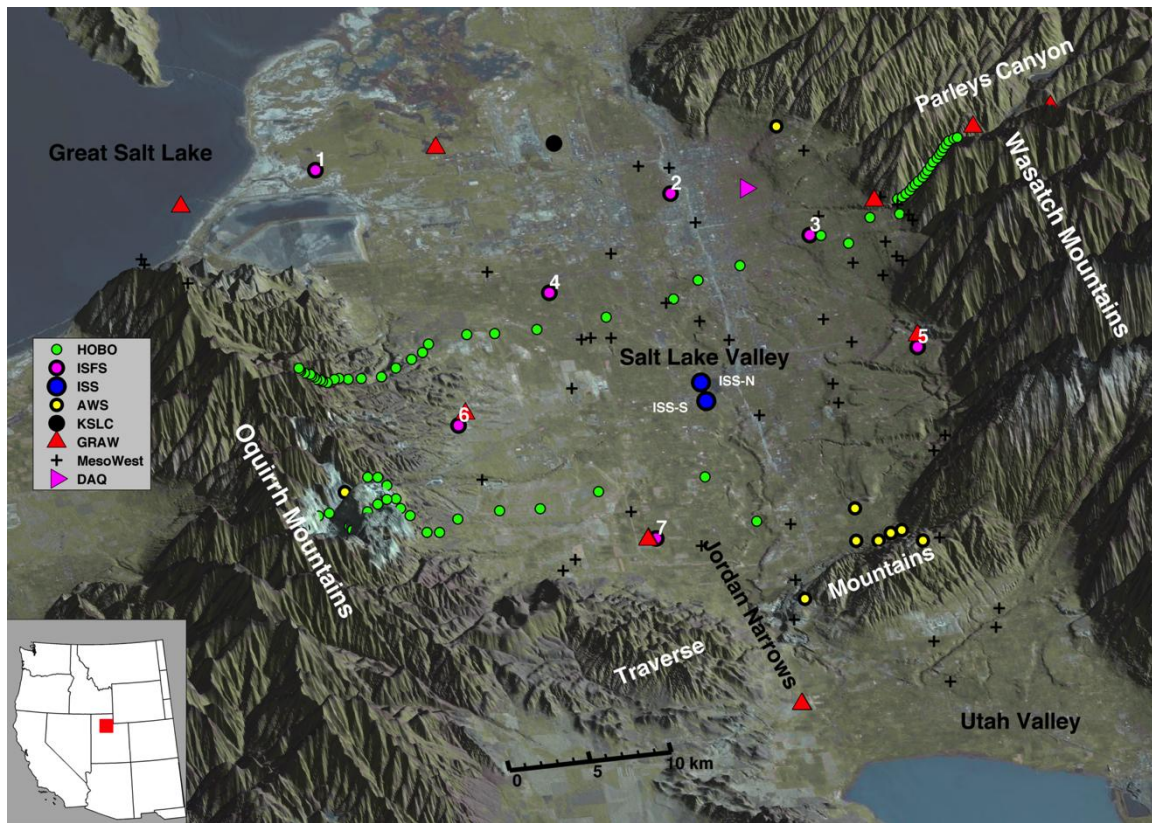


Fig. 1 Perspective view of the Salt Lake Valley showing PCAPS instrument locations and major topographic features (for further details see text and Lareau et al. 2013)

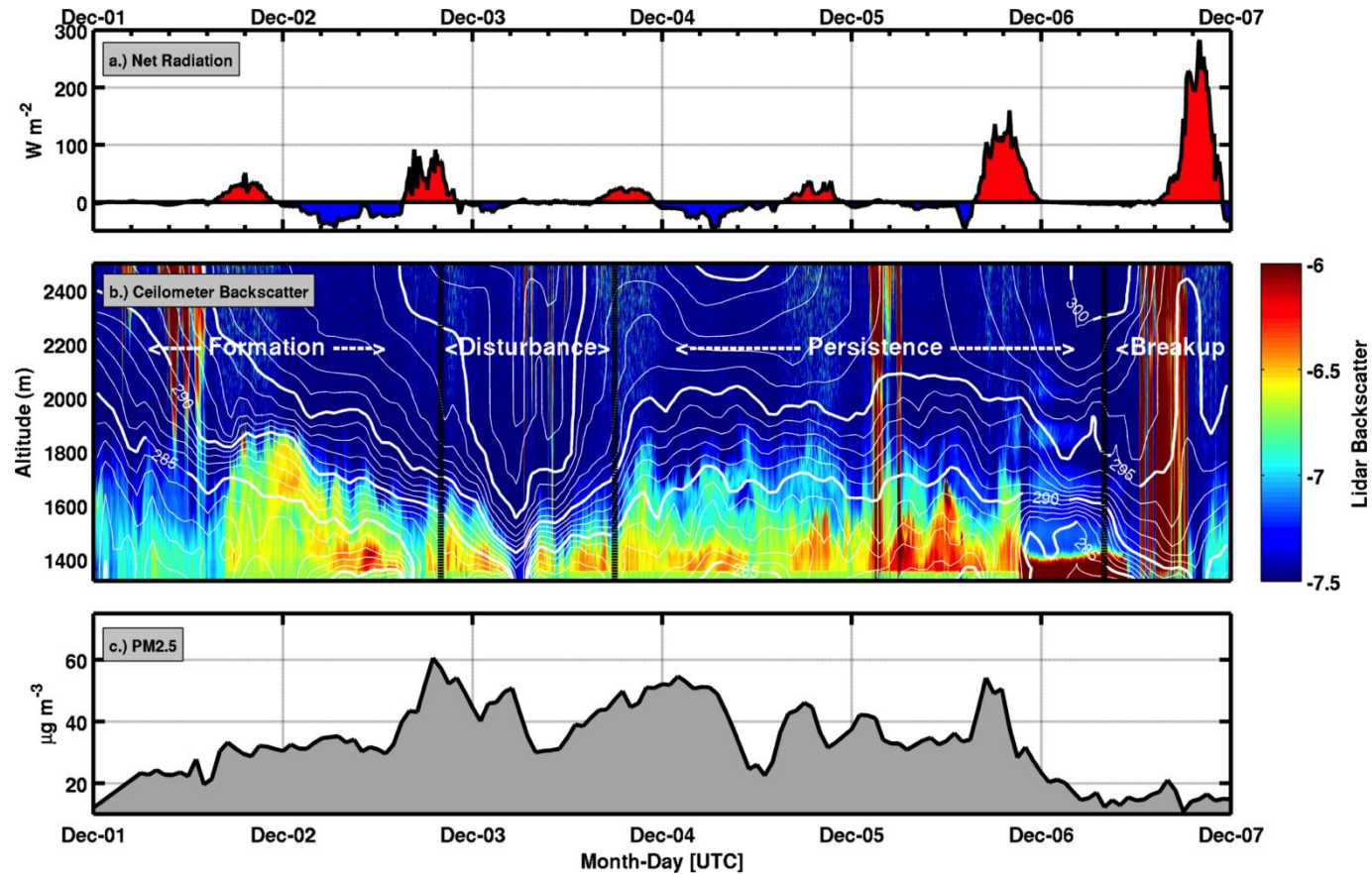


Fig. 2. Overview of PCAPS IOP-1. (a) Net radiation averaged over the seven ISFS stations in the SLV, (b) Time-height profile at ISS of potential temperature (contours at 1 K interval) and aerosol backscatter (shading) where yellow-orange (blue) shades reflect high (low) aerosol concentrations and dark red shades denote hydrometeors, (c) PM 2.5 concentration ($\mu g m^{-3}$) at DAQ site.

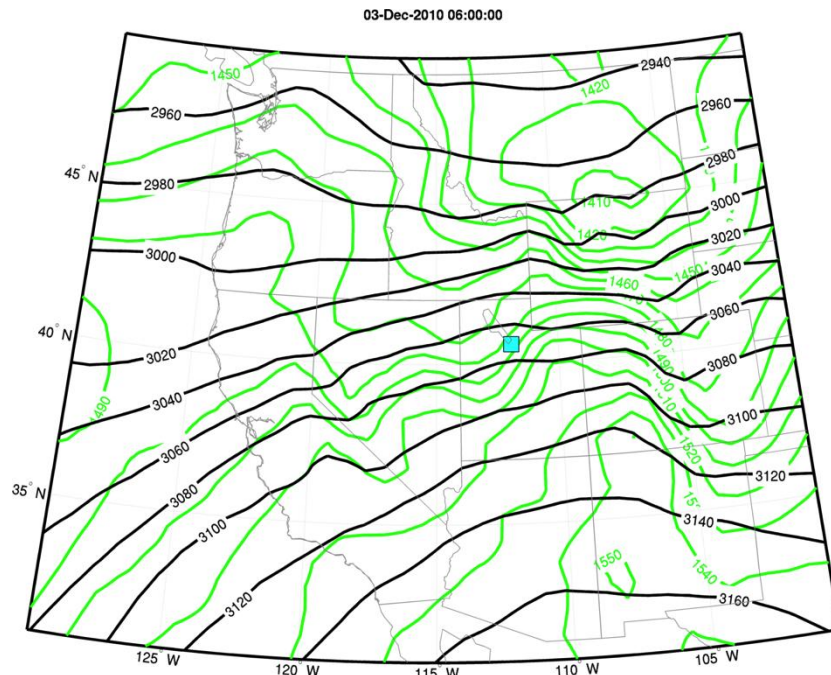


Fig. 3. European Centre for Medium-Range Weather Forecasts ERA-Interim reanalysis of the weak trough approaching Utah at 0600 UTC 3 December 2010. 700 hPa height (black contours at 20-m intervals) and 800 hPa height (green contours at 10-m intervals).

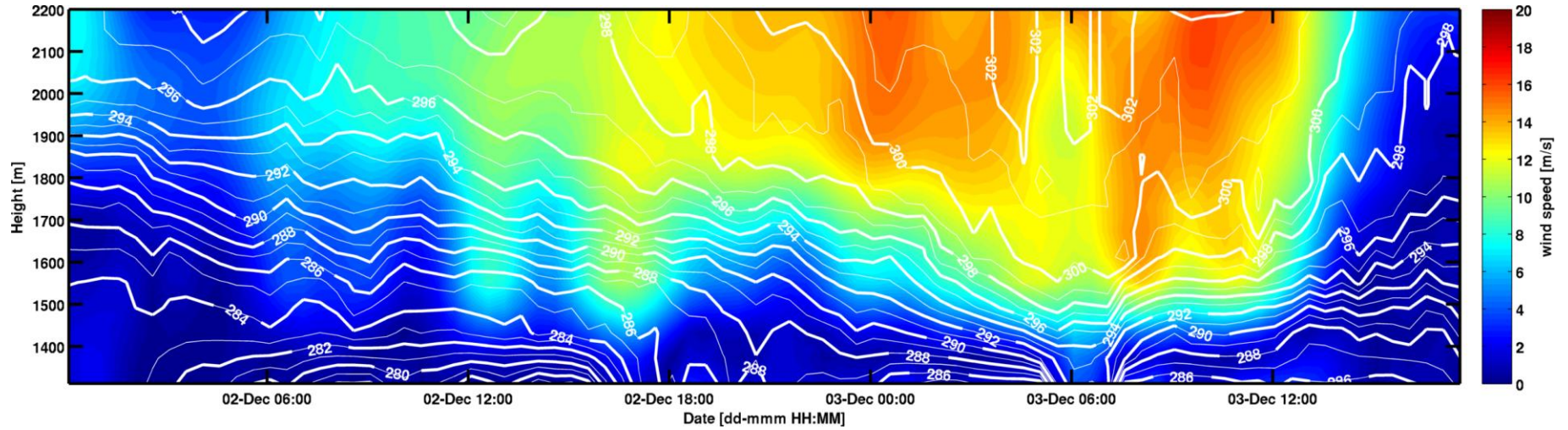


Fig. 4. Time height profile at ISS from 0000 UTC 2 – 1800 UTC 3 December of potential temperature (contours with heavy white lines every 2 K) and wind speed (shaded).

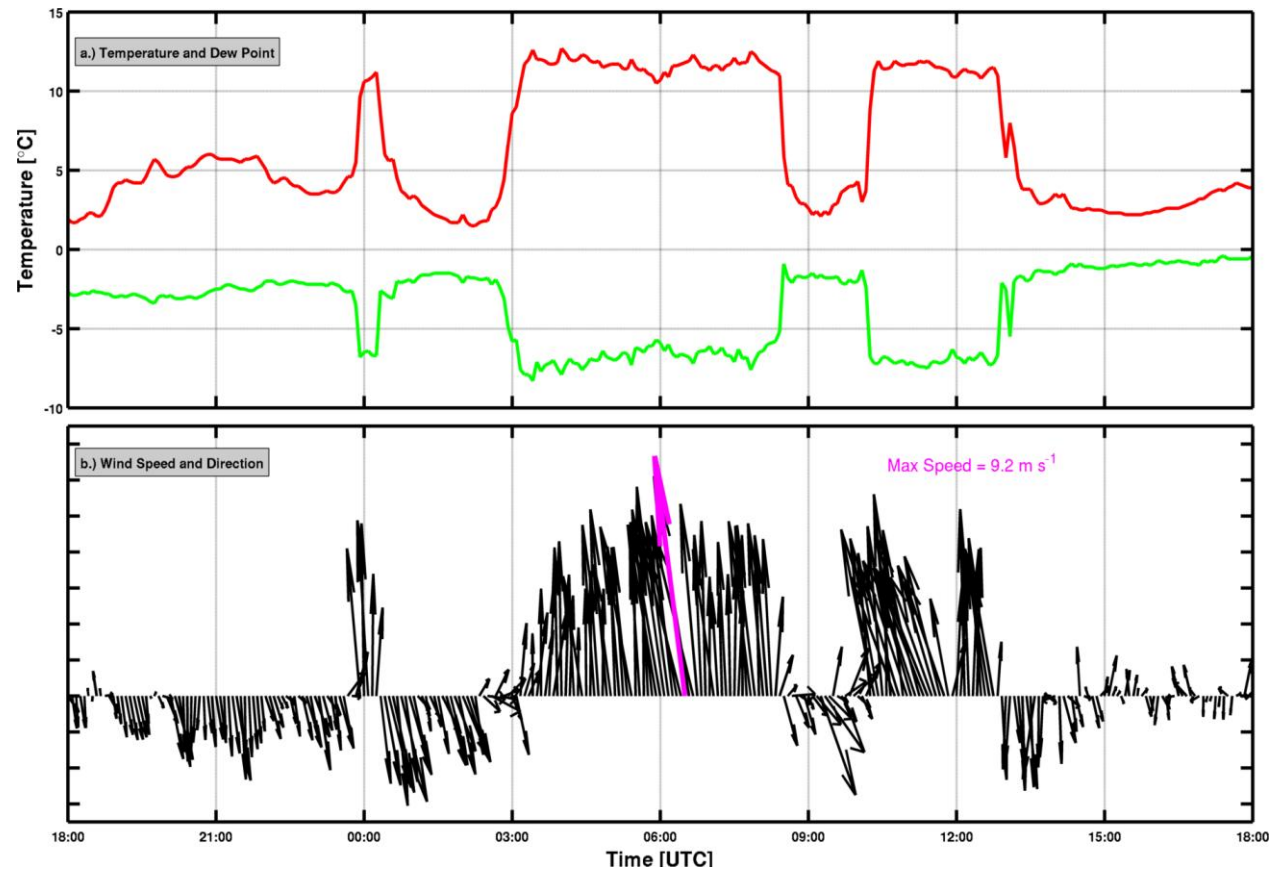


Fig. 5. Time series of (a) temperature (red line) and dew point temperature (green line) and (b) vector winds with the maximum speed shown in magenta for reference.

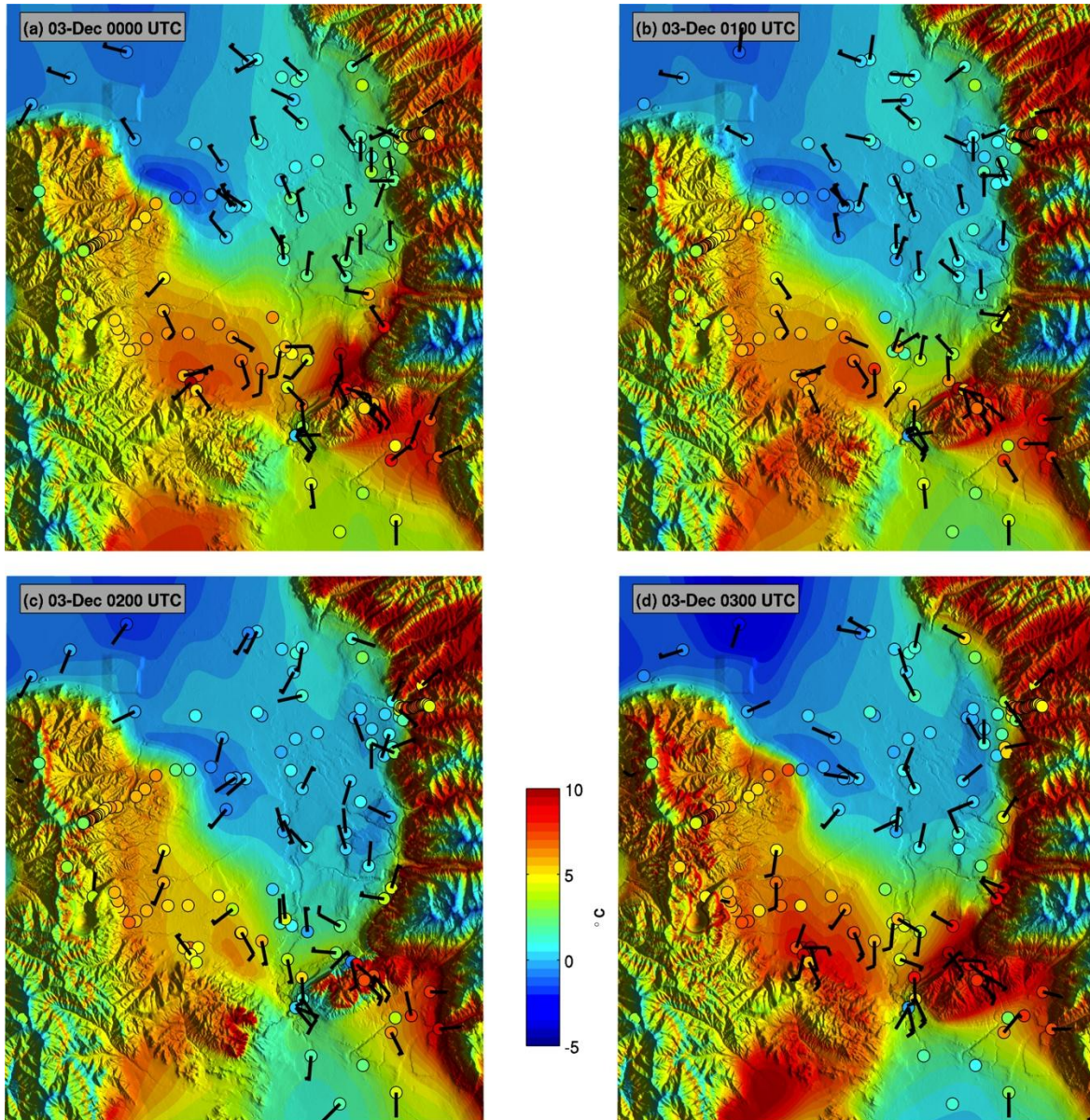


Fig 6. Hourly surface temperature analyses (colour shaded) from 0000-0300 UTC 3 December 2010. Surface temperature observations (filled circles shaded according to the scale) and vector wind (wind barbs in m/s where a full barb denotes 5 m/s).

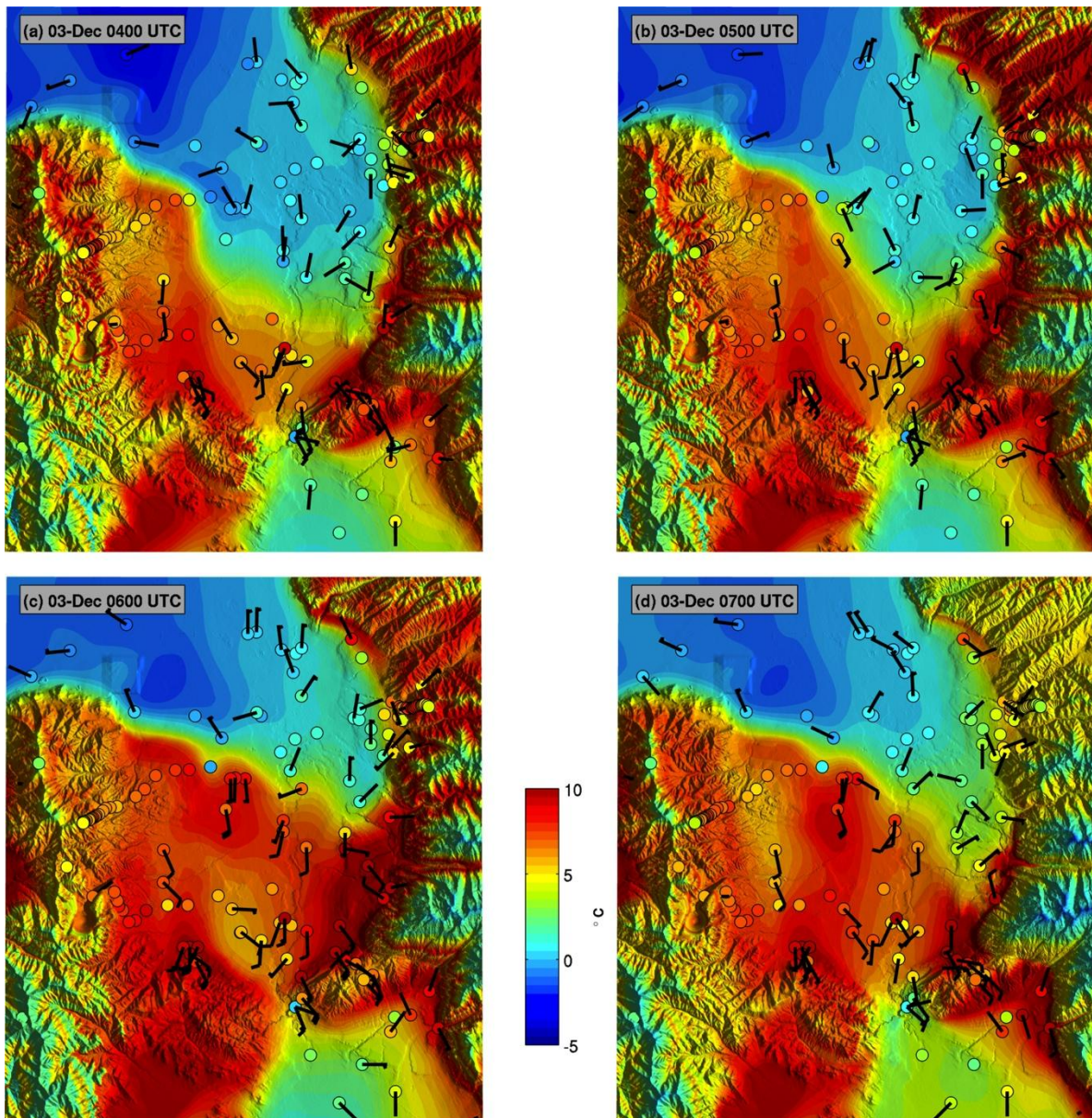


Fig 7. As in Fig. 6 except for 0400-0700 UTC 3 December.

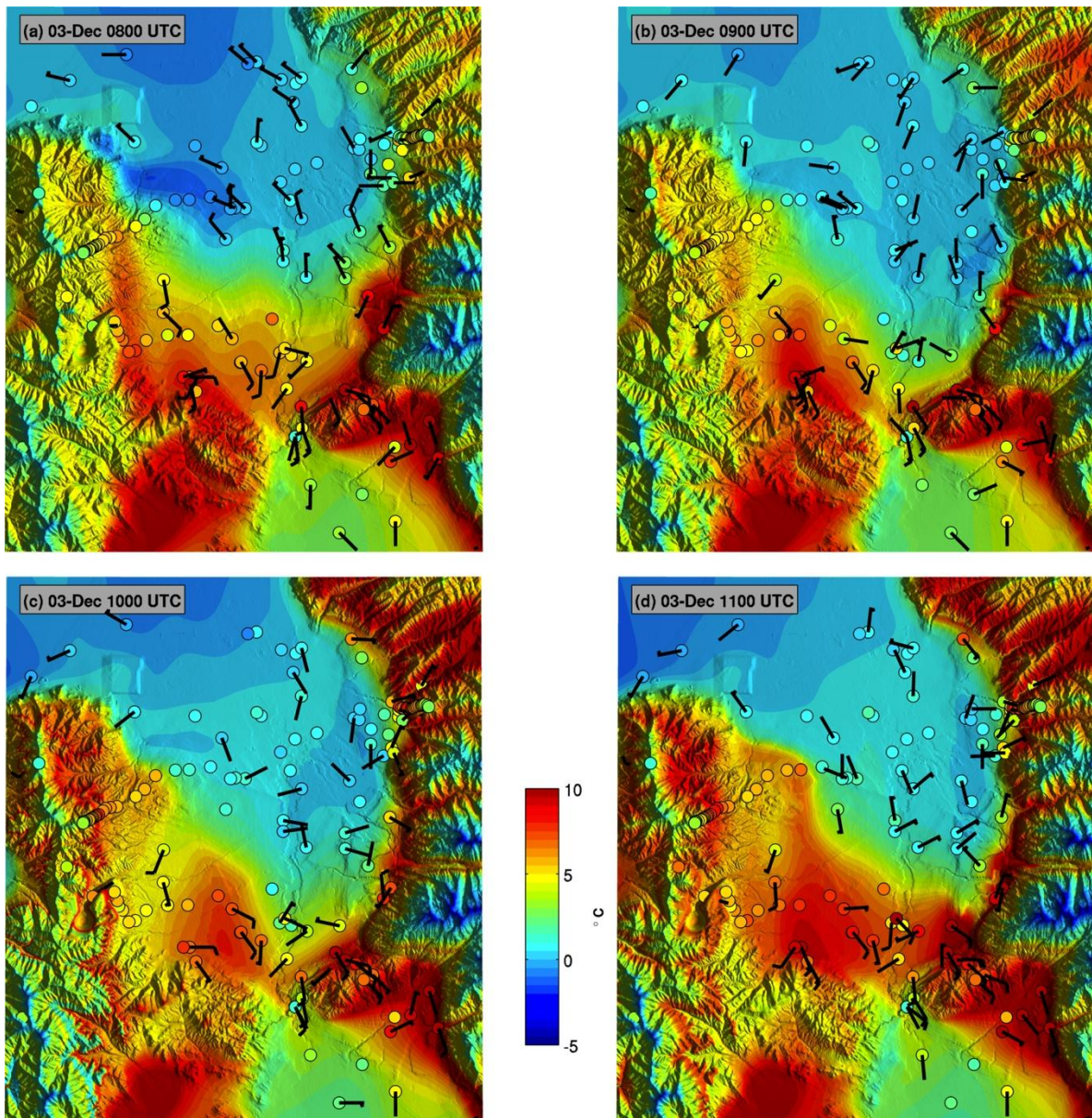


Fig. 8. As in Fig. 6 except for 0800-1100 UTC 3 December.

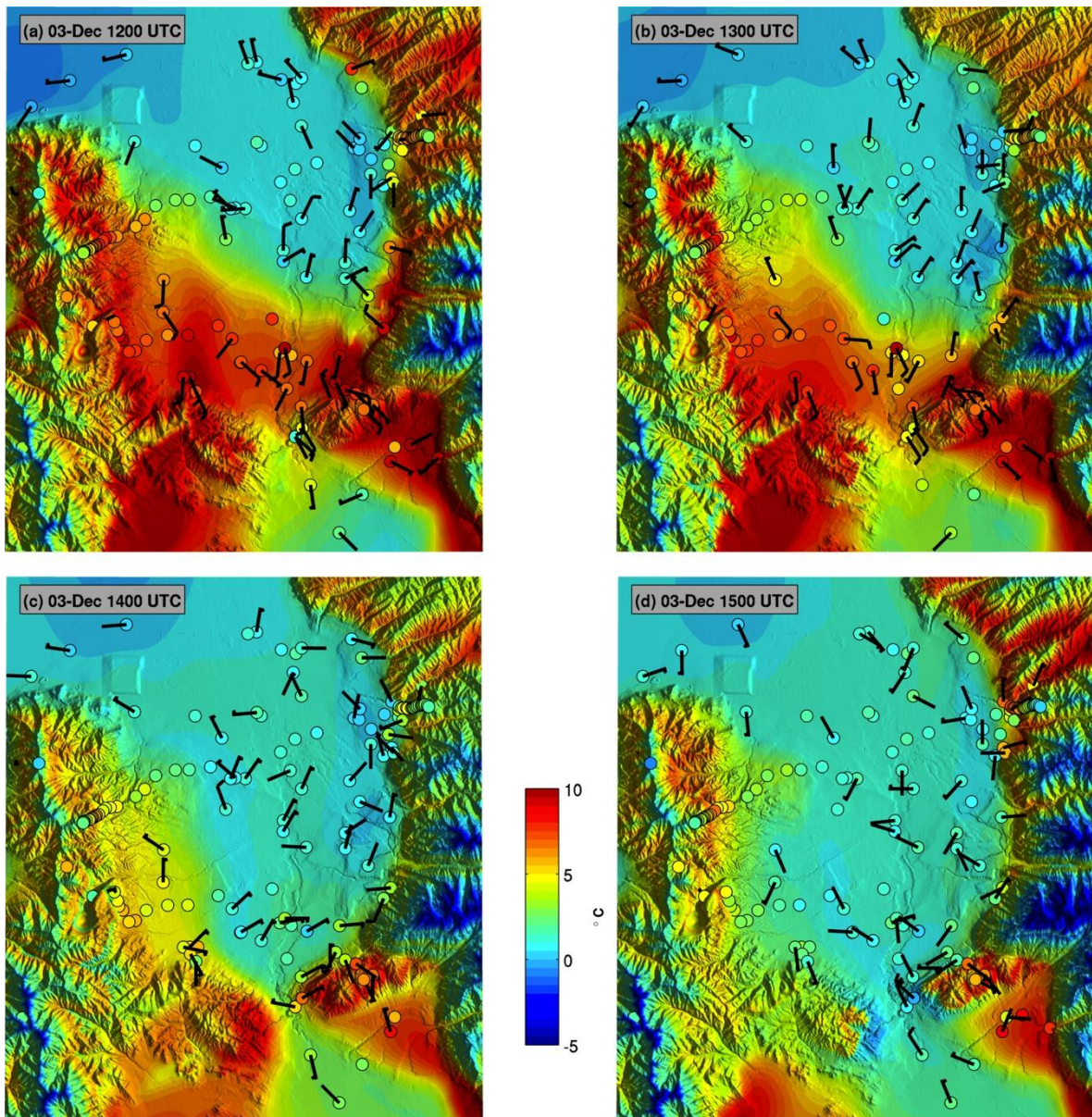


Fig 9. As in Fig. 6 except for 1200-1500 UTC 3 December.

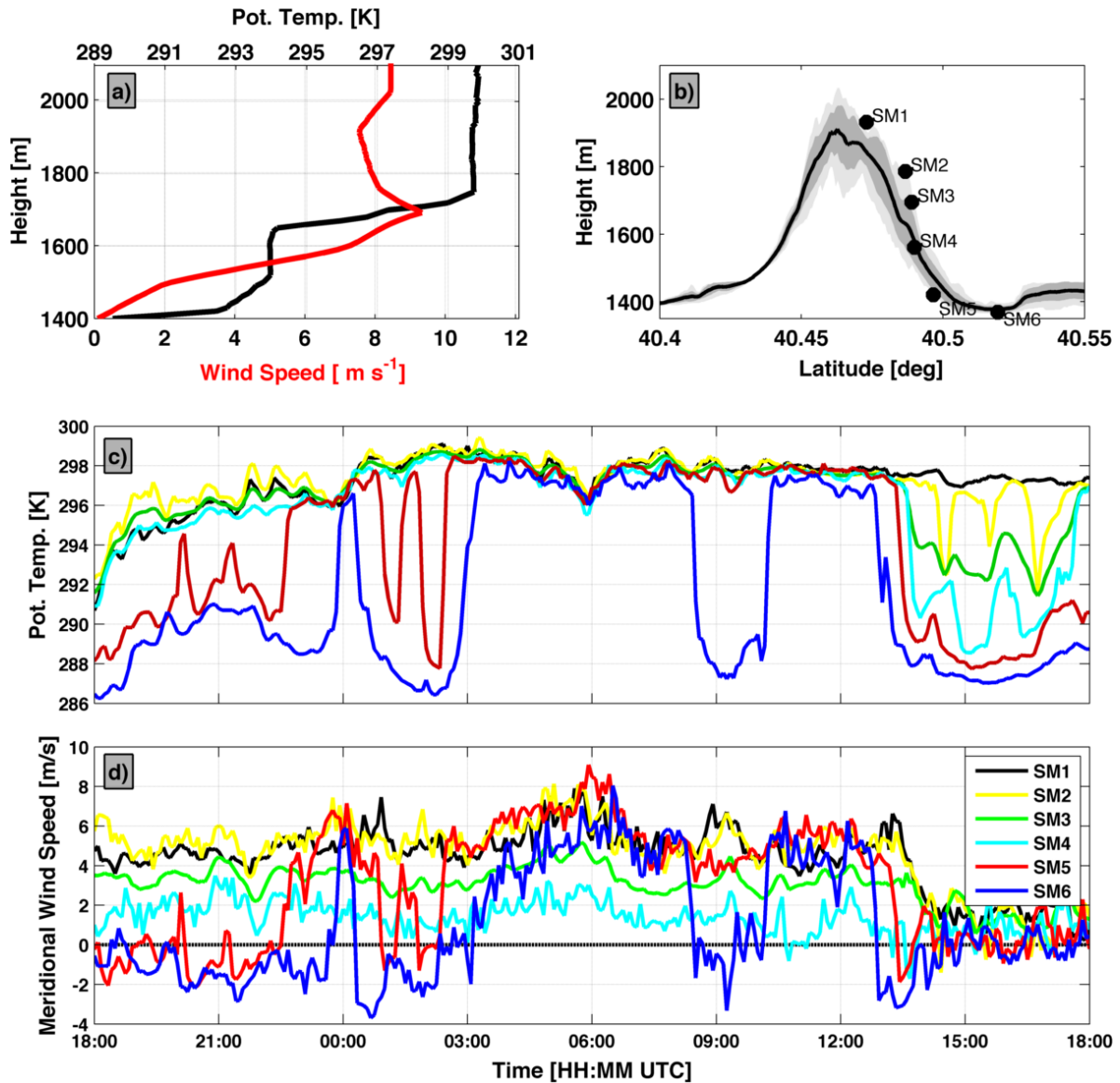


Fig. 10. Properties of the mountain wave forming over the Traverse Mountains. (a) Sounding upstream of the SLV at 0600 UTC 3 December showing potential temperature (black) and meridional wind (red). (b) Traverse Mountain cross-section showing station locations and the terrain variability (shading). (c) Potential temperature and (d) meridional wind time series for each of the 6 SM stations.

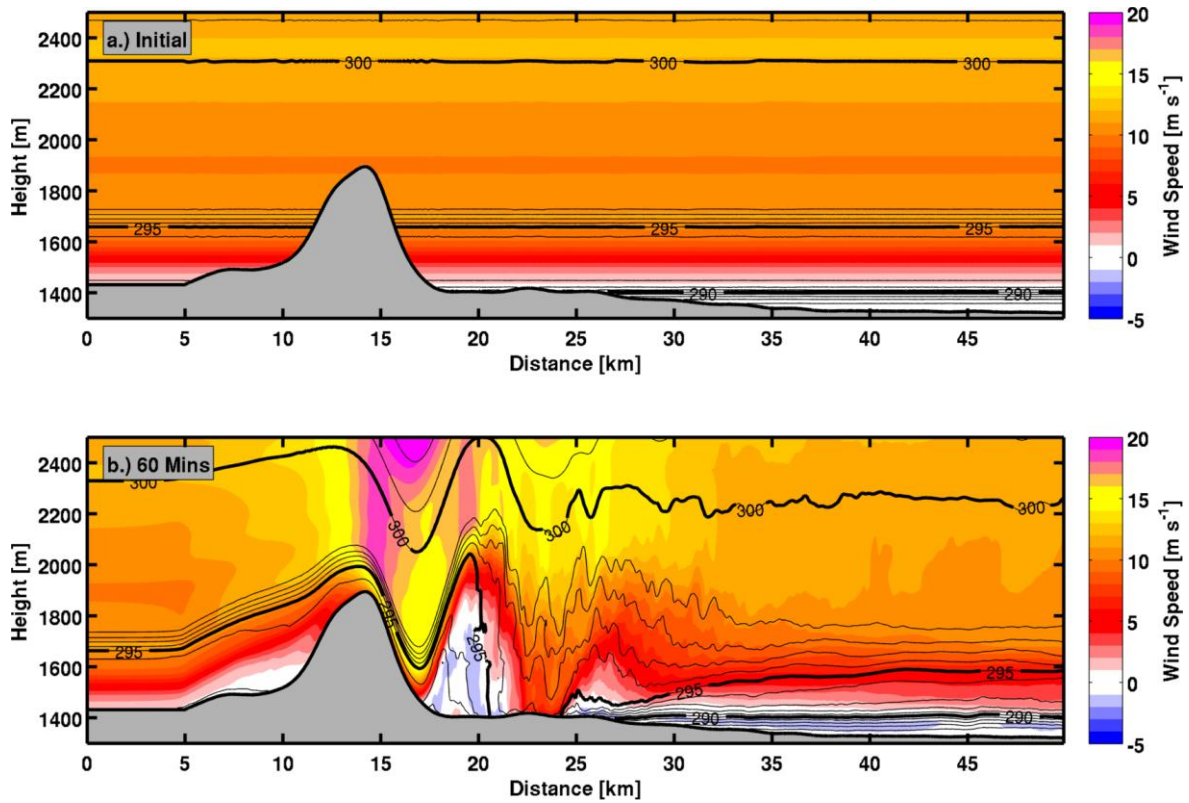


Fig. 11. Large-Eddy Simulation of a mountain wave disrupting the two-layered CAP. Panels show wind speed (colours) and potential temperature (contours, bold every 5 K) at (a) the initialization and (b) after 1-h of simulation.

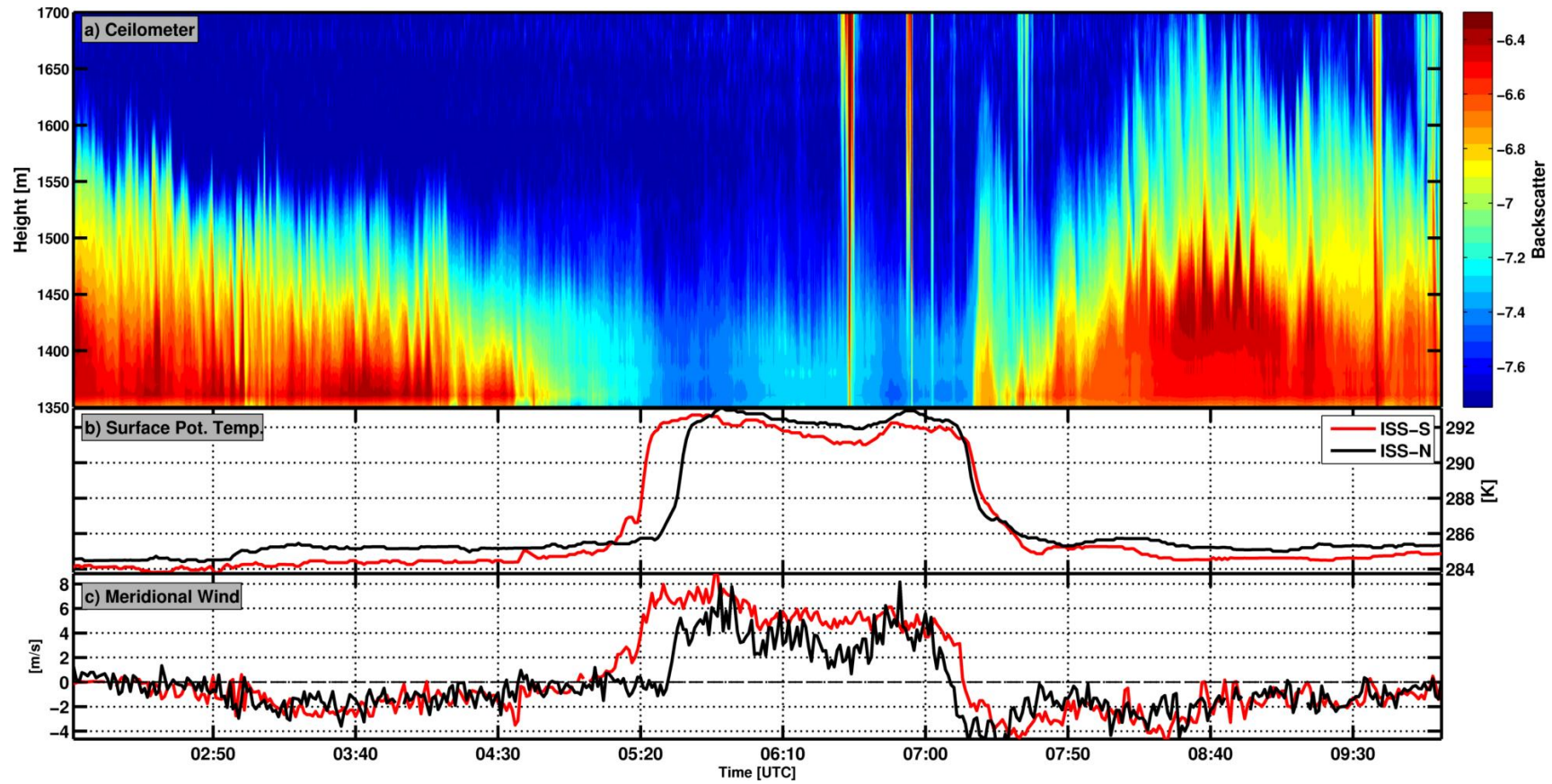


Fig. 12. Time series data during the warm and cold frontal passages at ISS-S and ISS-N on 3 December 2010. (a) Laser ceilometer backscatter, (b) potential temperature, and (c) meridional wind.

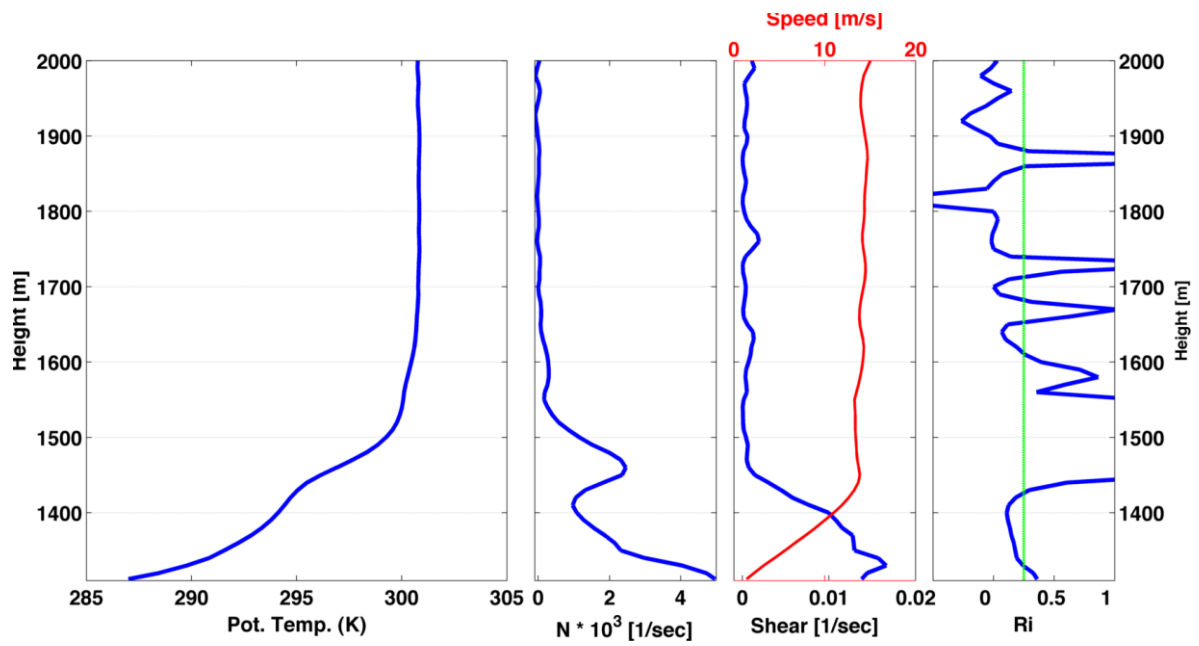


Fig. 13. Sounding from ISS-S at 05:14 UTC 3 December. (a) Potential temperature, (b) Brunt-Vaisala frequency, (c) wind speed and wind shear, and (d) the gradient Richardson number with the critical value marked in green.

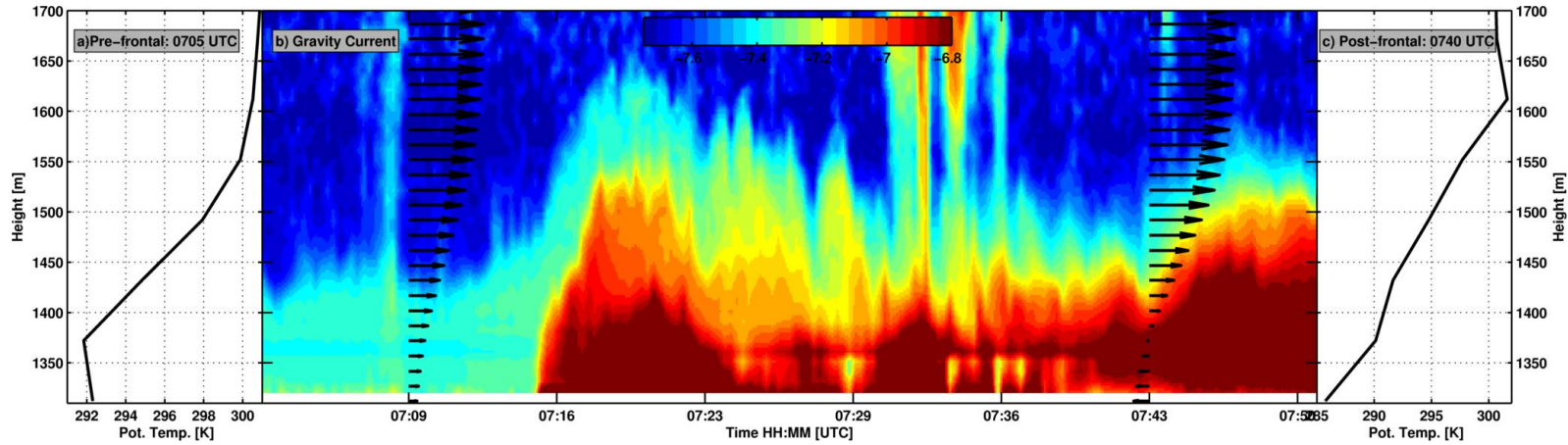


Fig. 14. Detail of the gravity current passage at ISS-S. (a) Prefrontal potential temperature profile at 0705 UTC, (b) ceilometer backscatter and meridional wind profiles from the radar wind profiler, and (c) post-frontal potential temperature profile at 0740 UTC. Profile data is retrieved from the time-height data set.

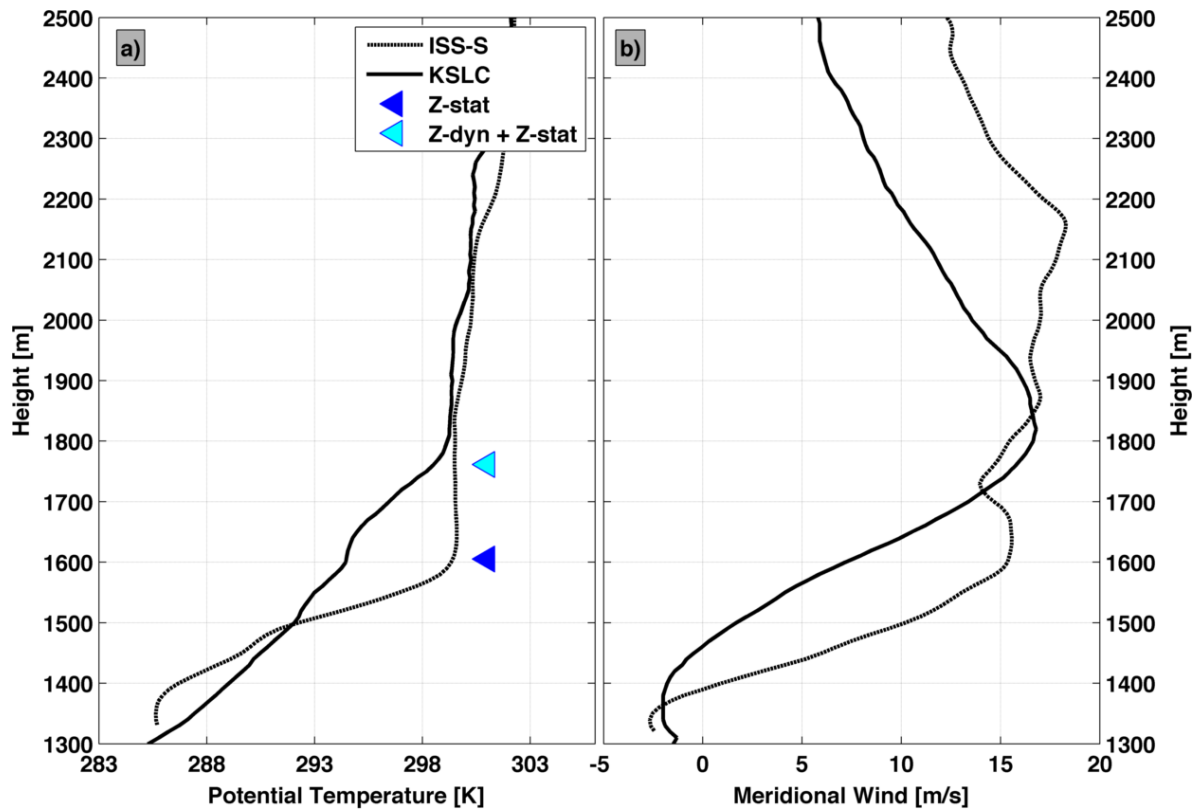


Fig. 15. Vertical profiles of (a) potential temperature and (b) meridional wind launched at 1115 UTC at KSLC (solid lines) and ISS-S (dashed lines). The shaded triangles are estimates of the CAP depth at KSLC from the static and dynamic + static forcing.

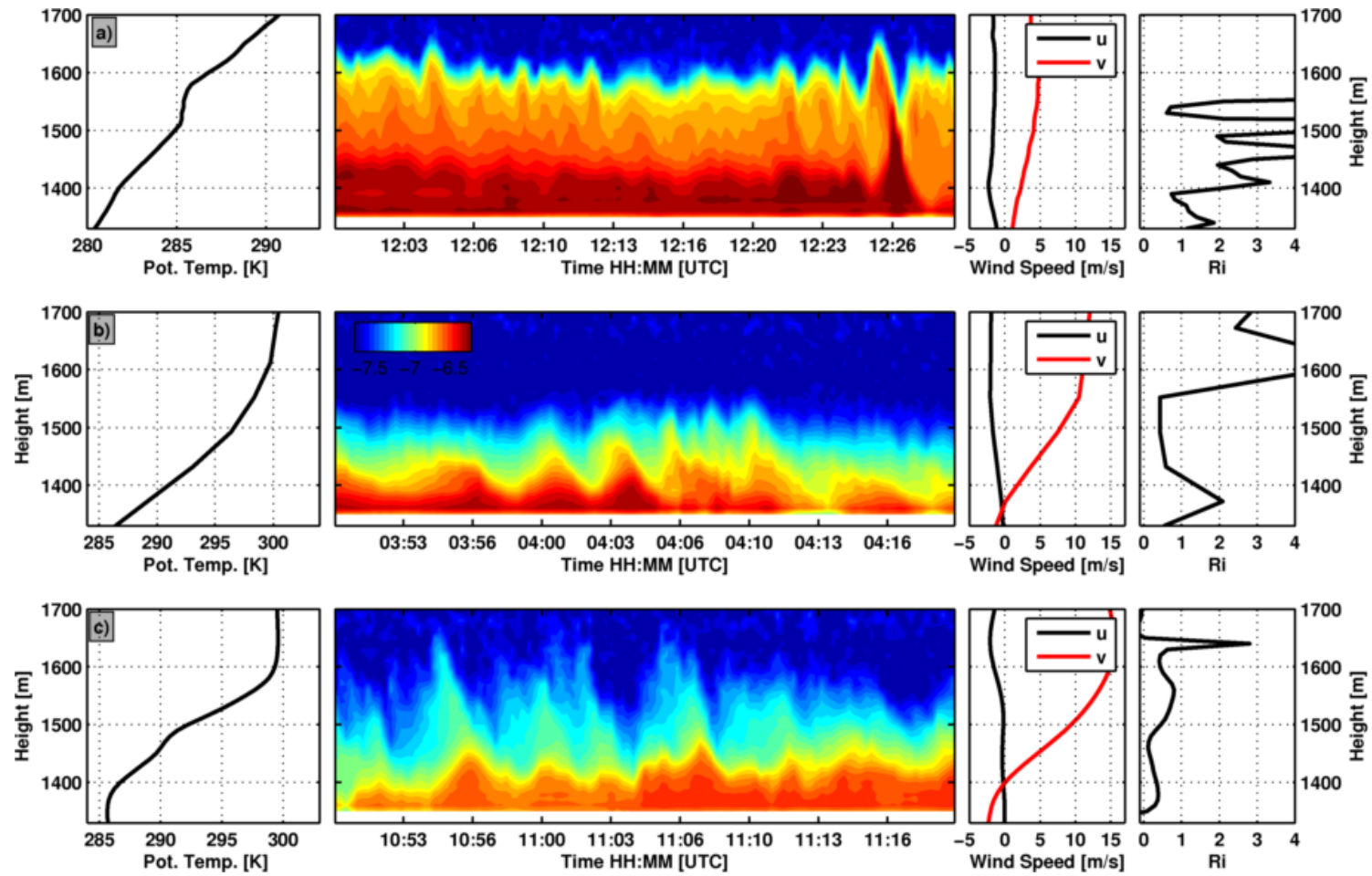


Fig. 16. Kelvin Helmholtz waves at: (a) ~1200 UTC 2 December, (b) ~0400 UTC 3 December, and (c) ~1100 UTC 3 December. First column: potential temperature. Second column: aerosol backscatter. Third column: wind speed. Last column: gradient Richardson number.

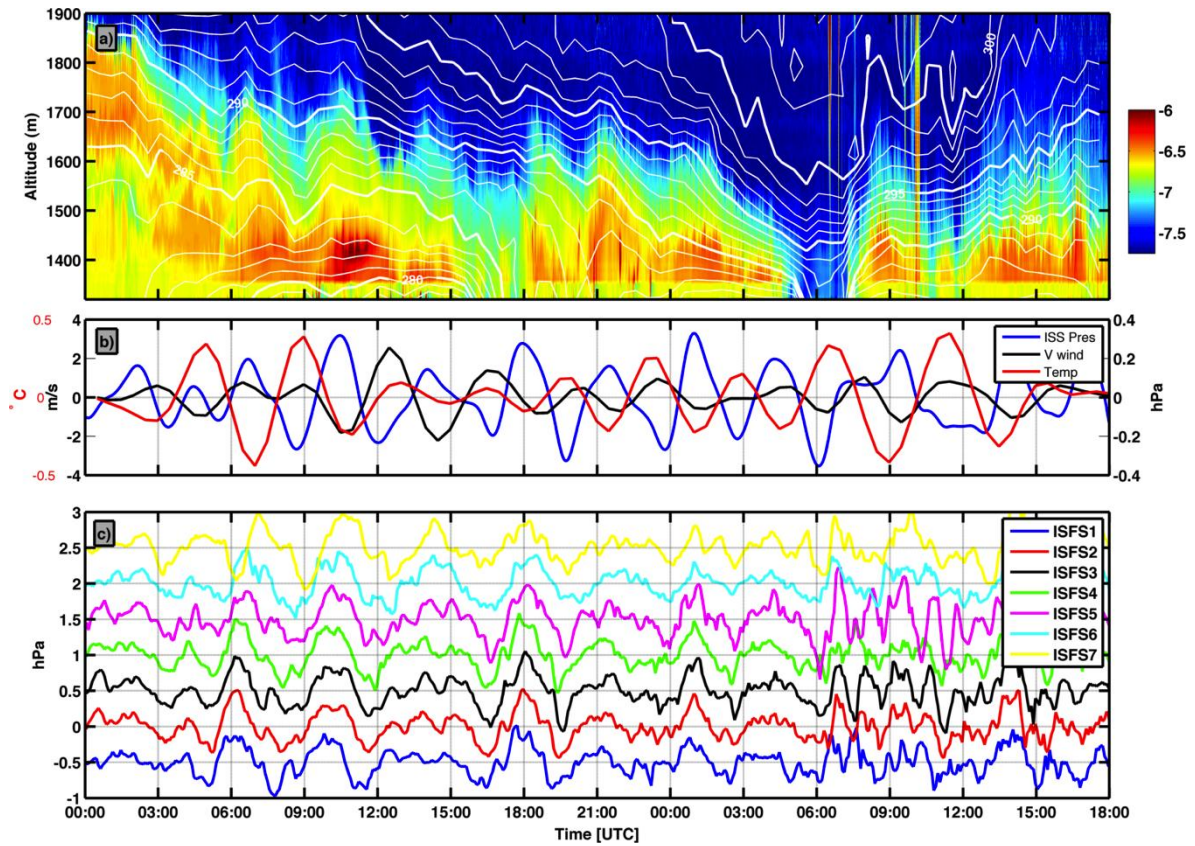


Fig. 17. Conditions at ISS-S from 0000 UTC 2 December to 1800 3 December of: (a) aerosol backscatter (shaded) with potential temperature (contours), (b) Band-pass filtered perturbations of ISS-S surface pressure (blue), and 1500-1800 m mean meridional wind (black), and potential temperature (red). (c) High-pass filtered surface pressure perturbations at each ISFS site. Curves are offset by 0.5 hPa.

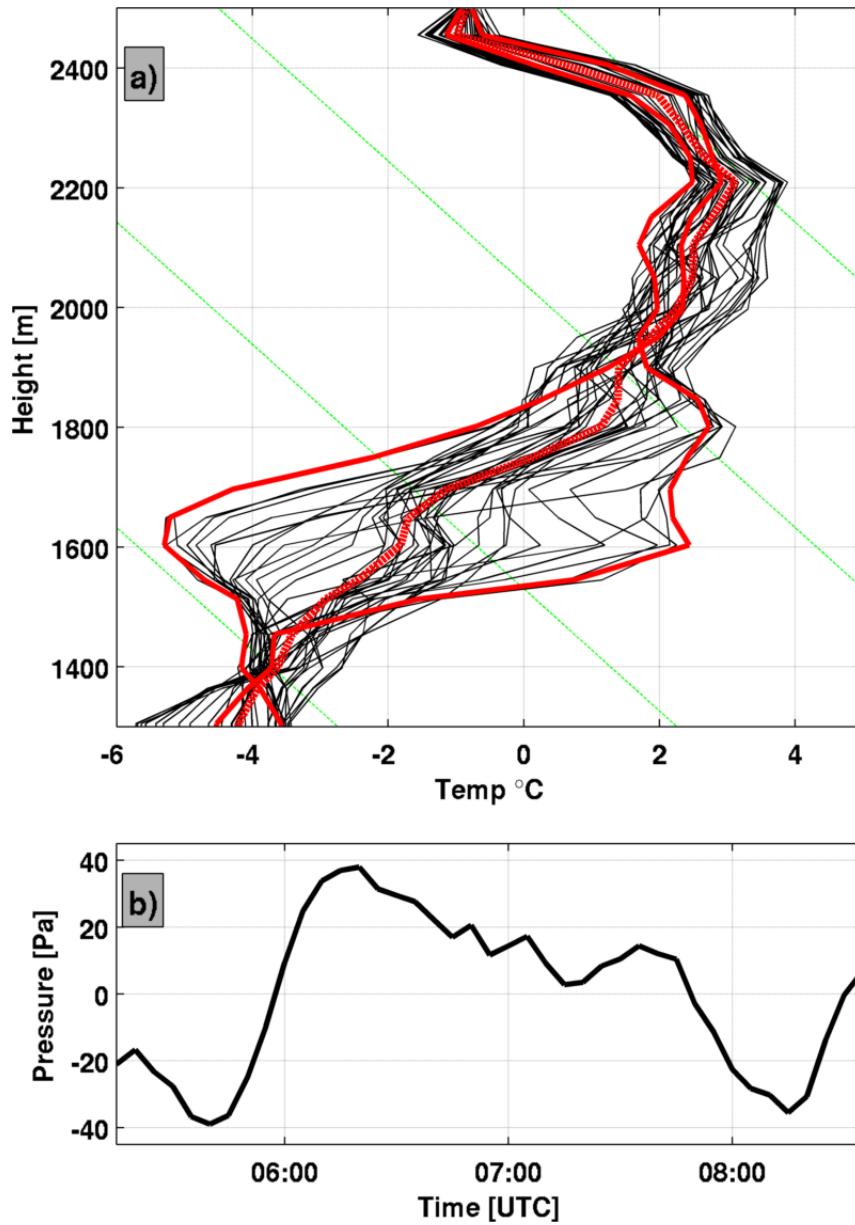


Fig. 18. (a) Harker's Ridge temperature profiles every 5 minutes between 0525 and 0830 UTC during the passage of one BSIW. Red lines indicate the mean and extreme profiles and the dashed green lines are adiabats. (b) The surface pressure perturbation computed from temperature anomalies.

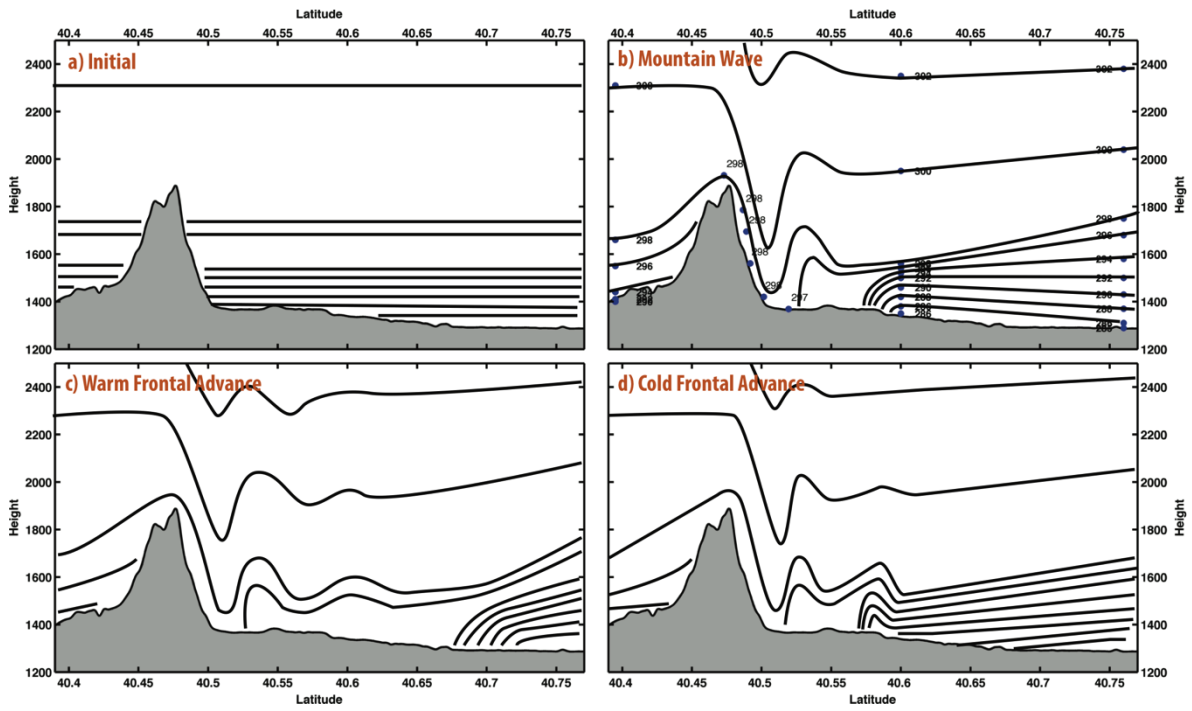
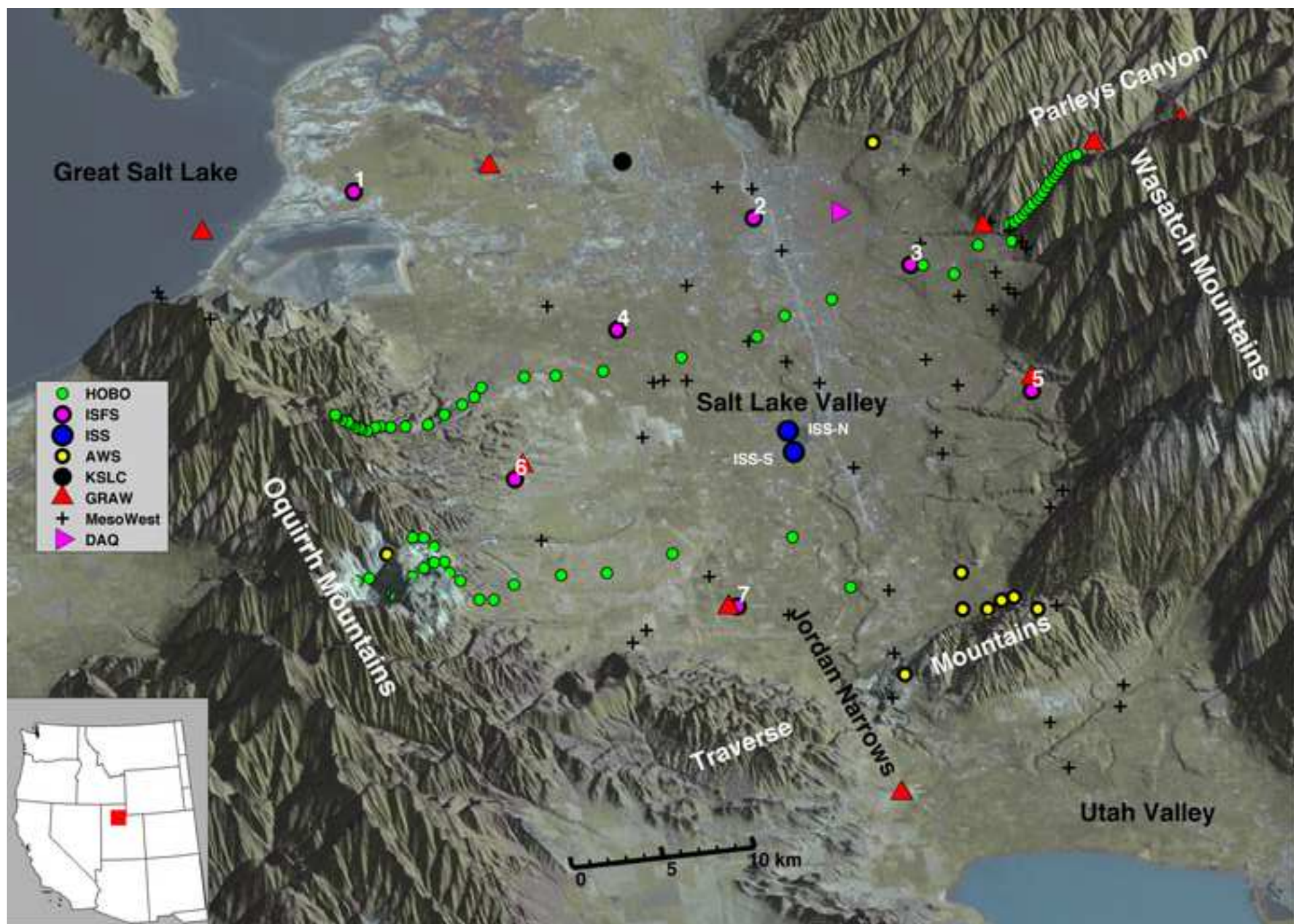
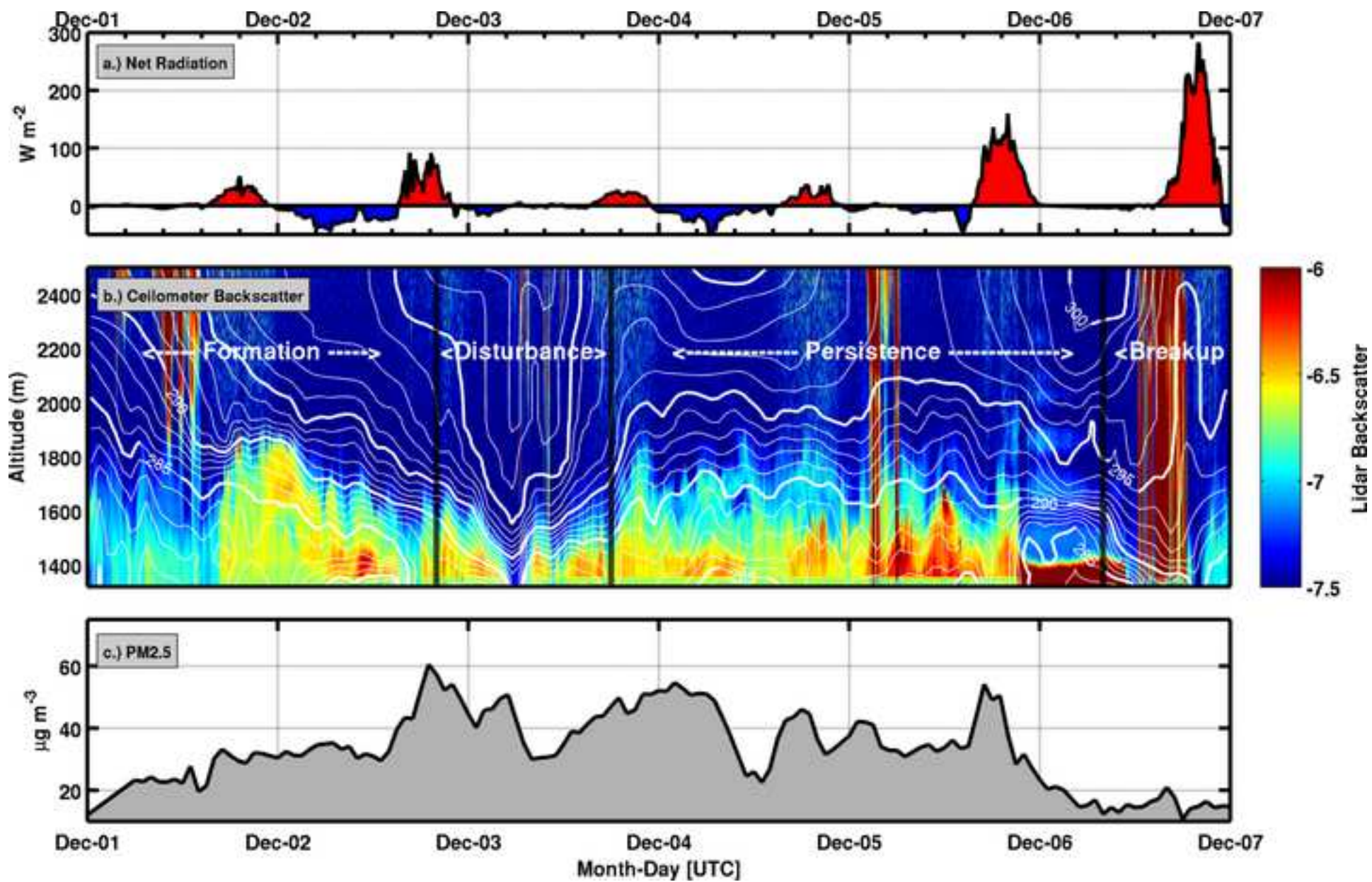


Fig. 19. Schematic of CAP displacement. Stages described in the text.

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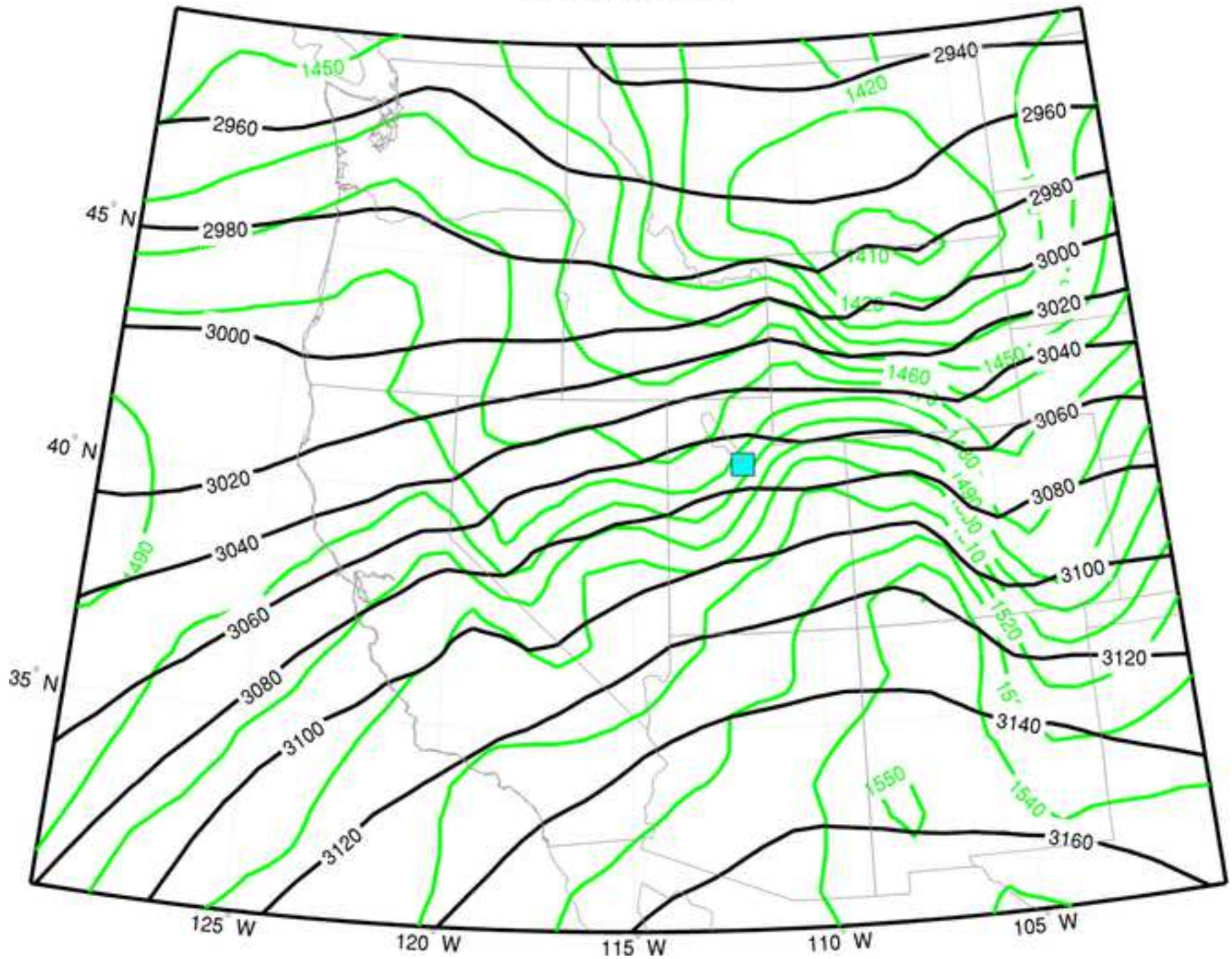


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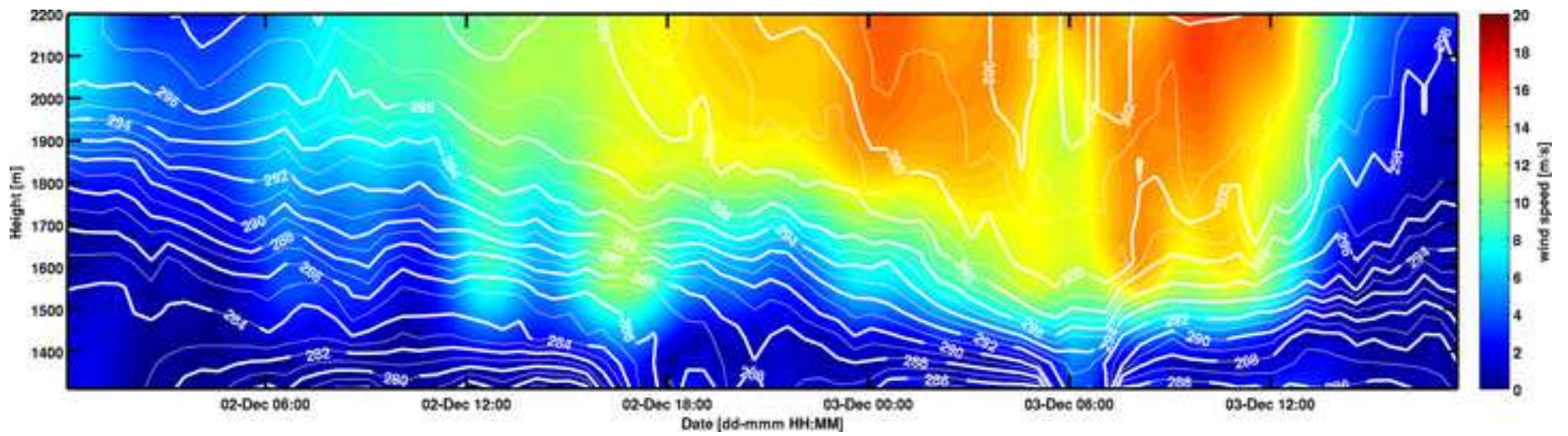


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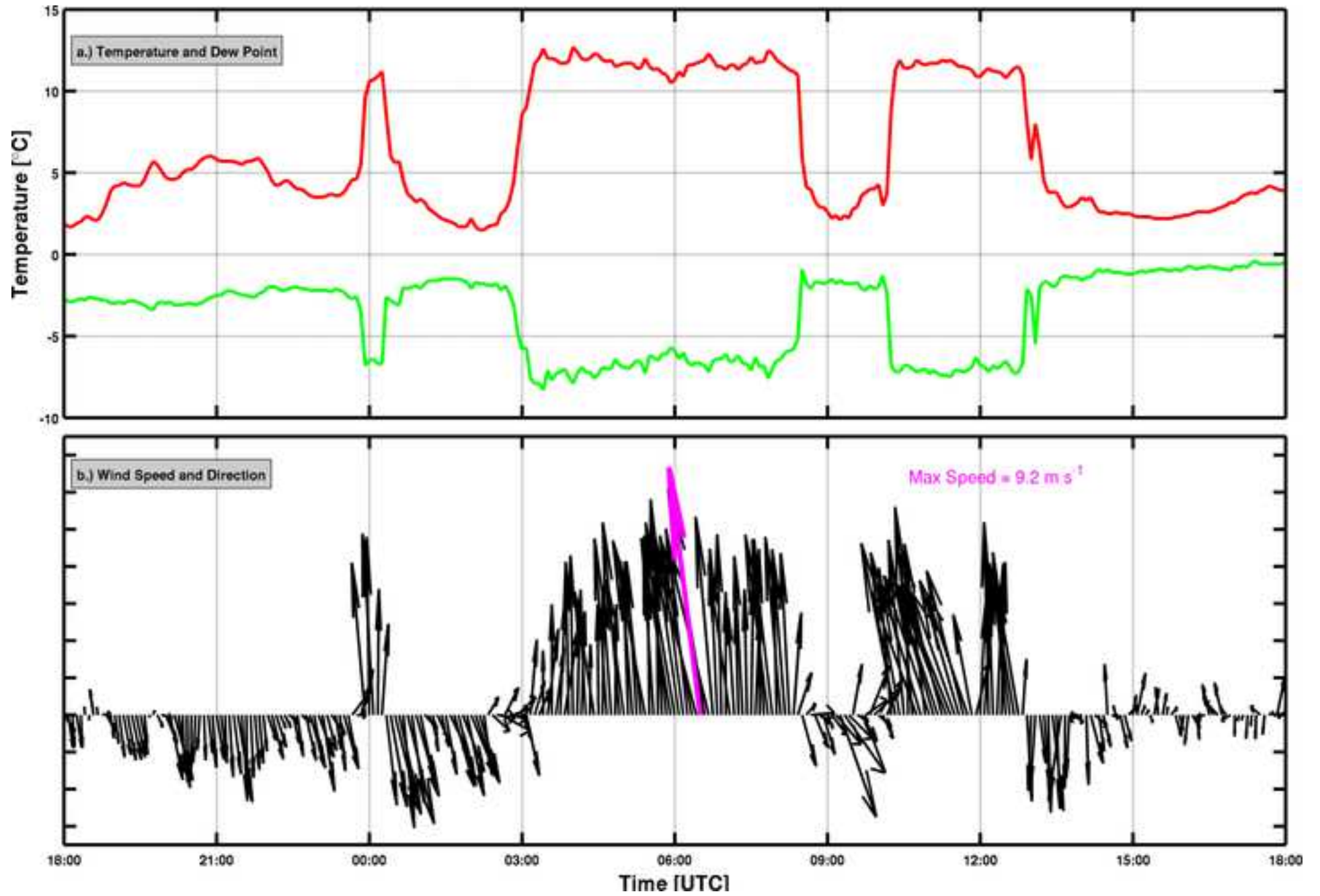
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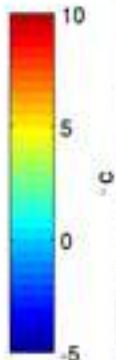
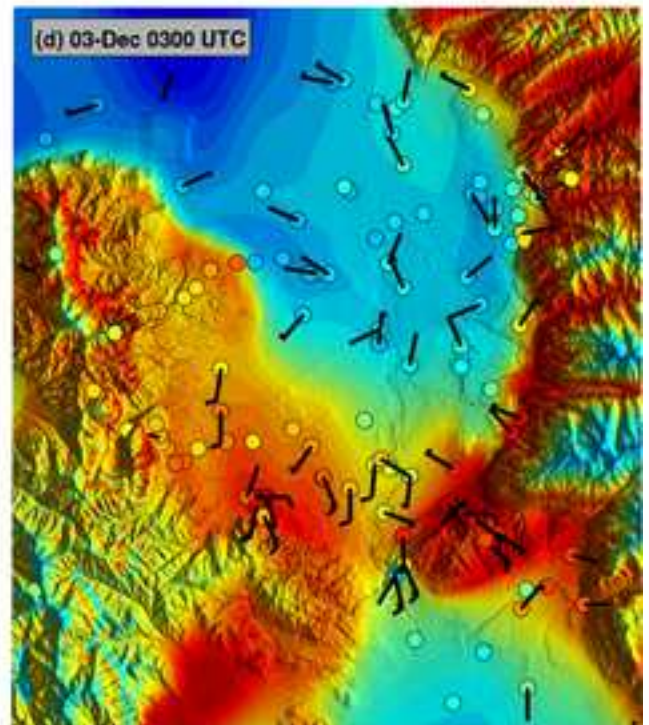
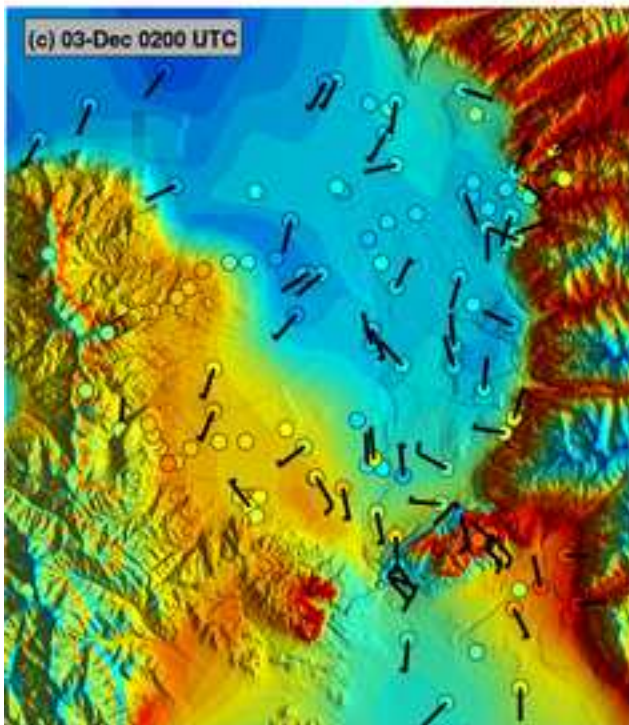
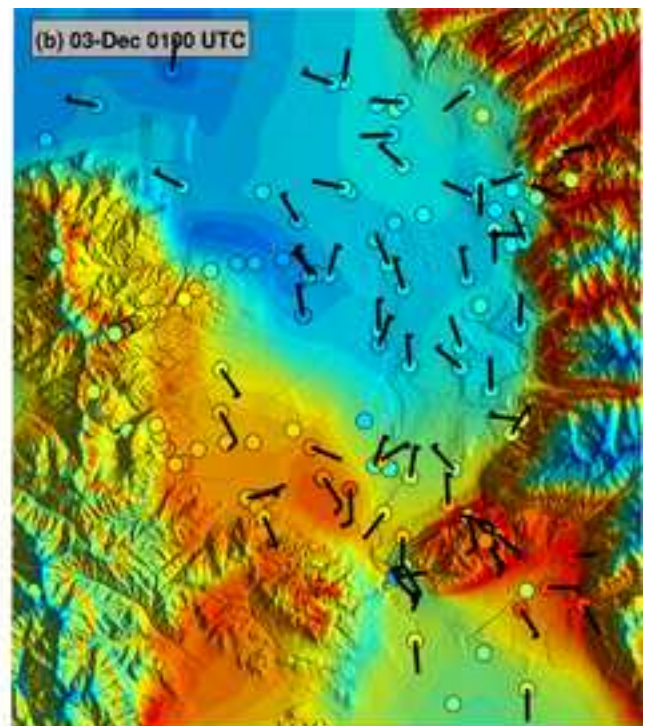
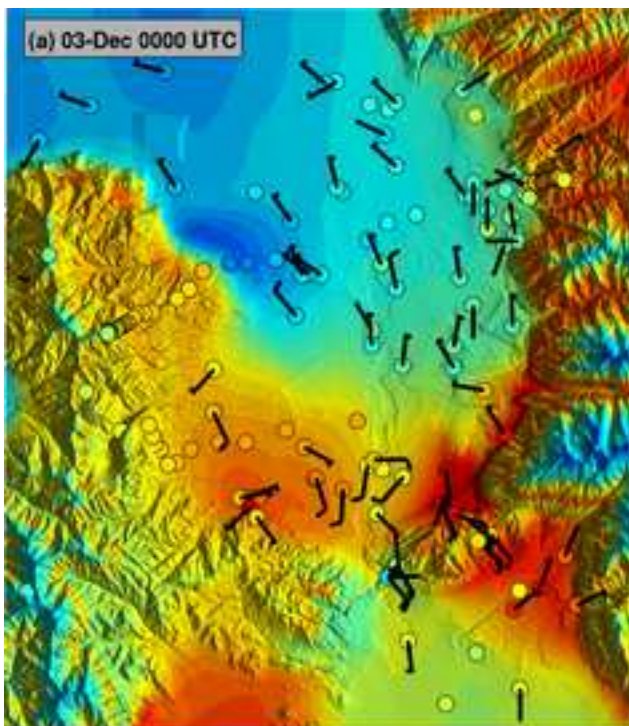
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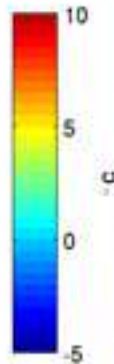
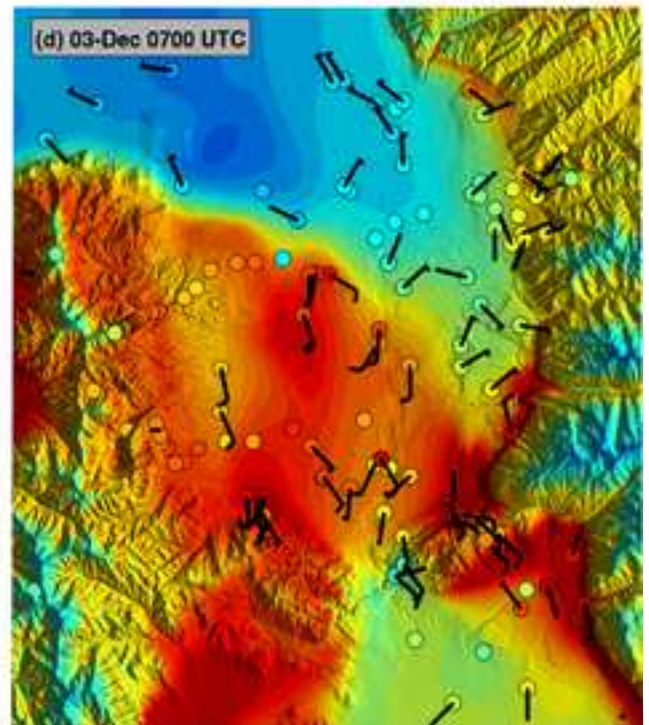
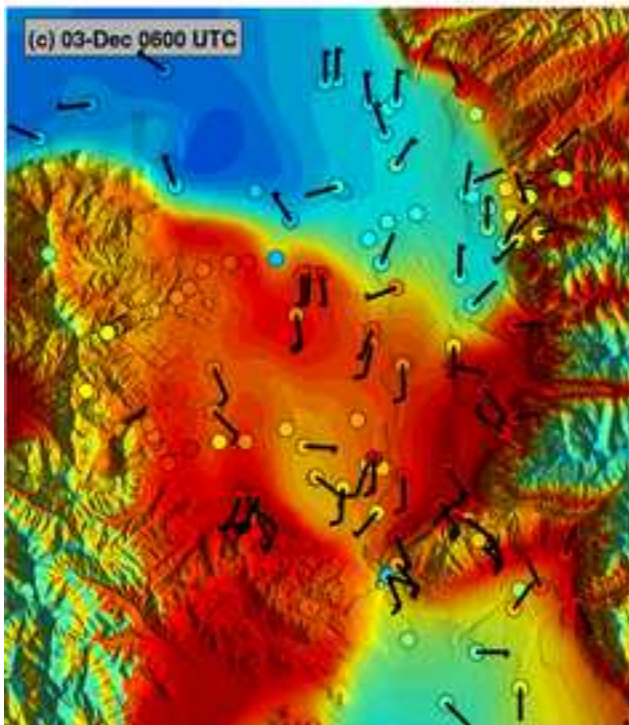
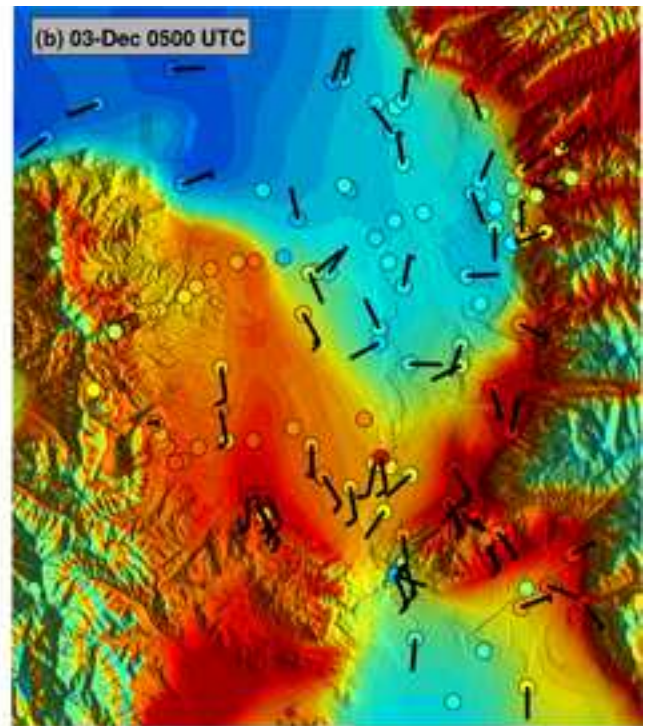
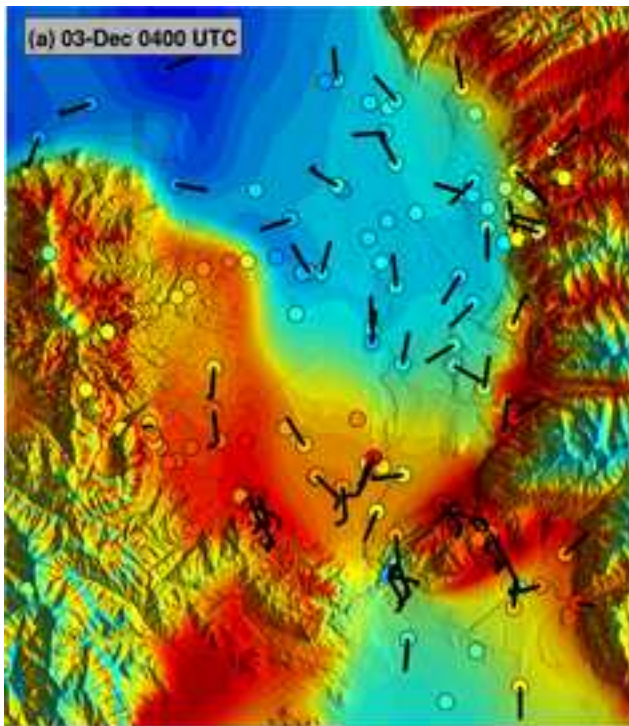
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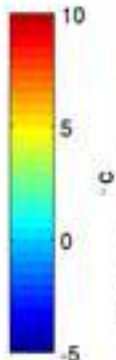
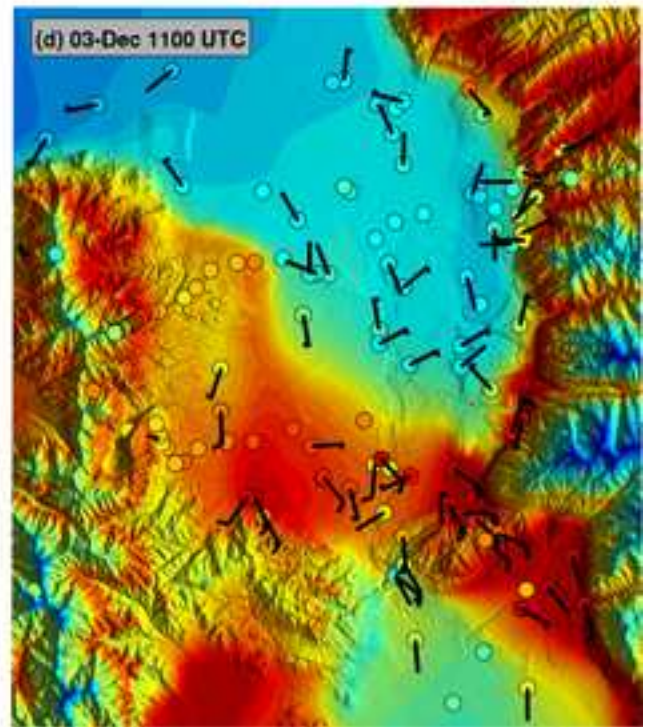
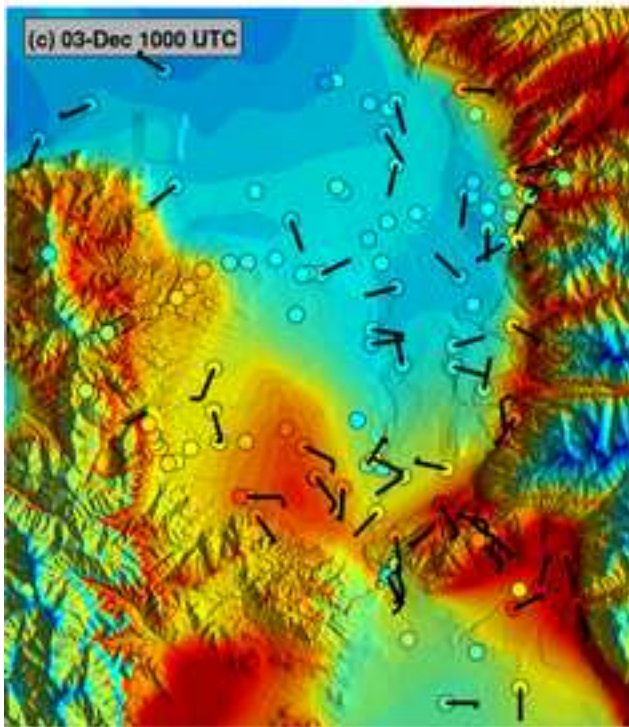
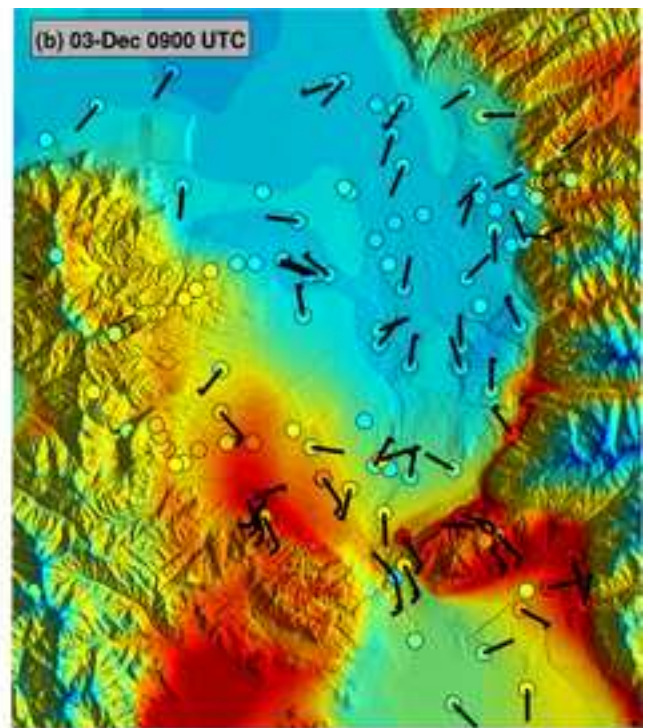
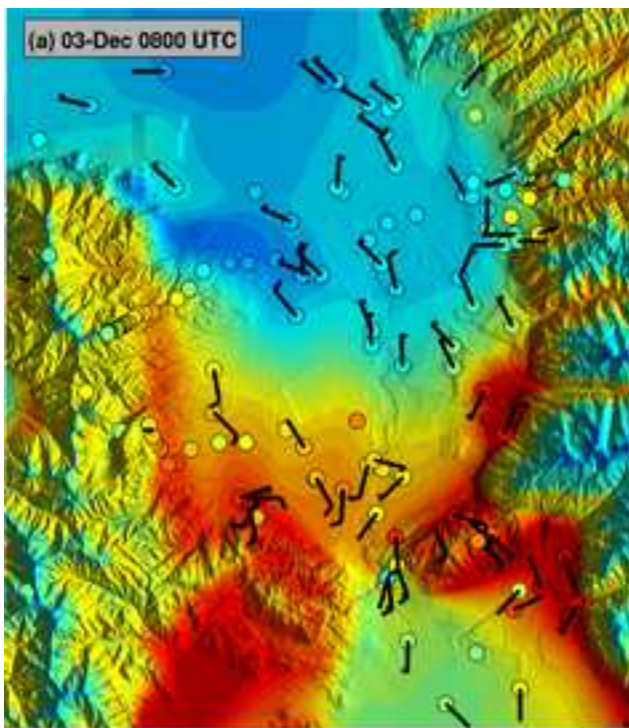
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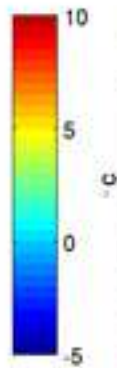
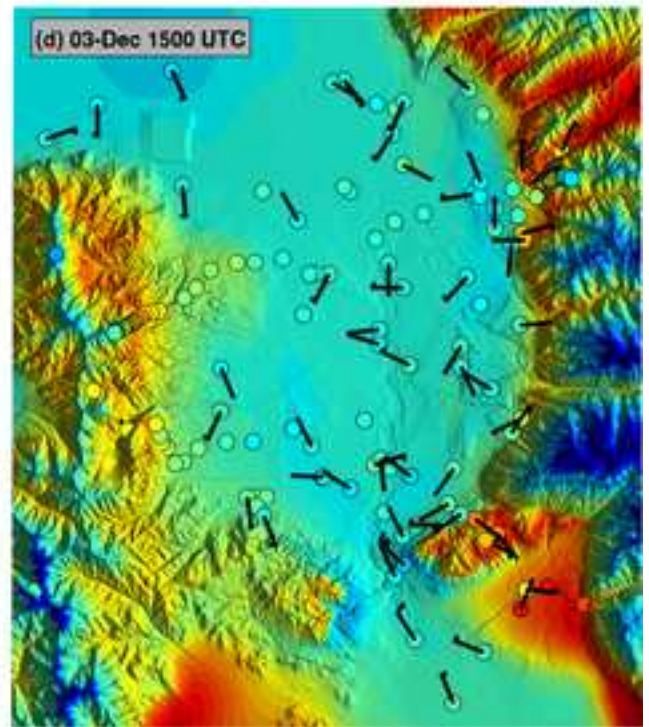
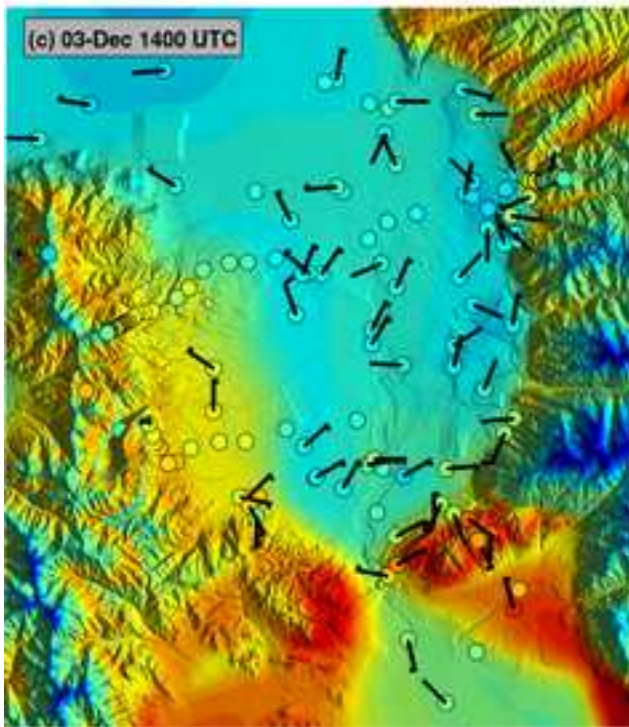
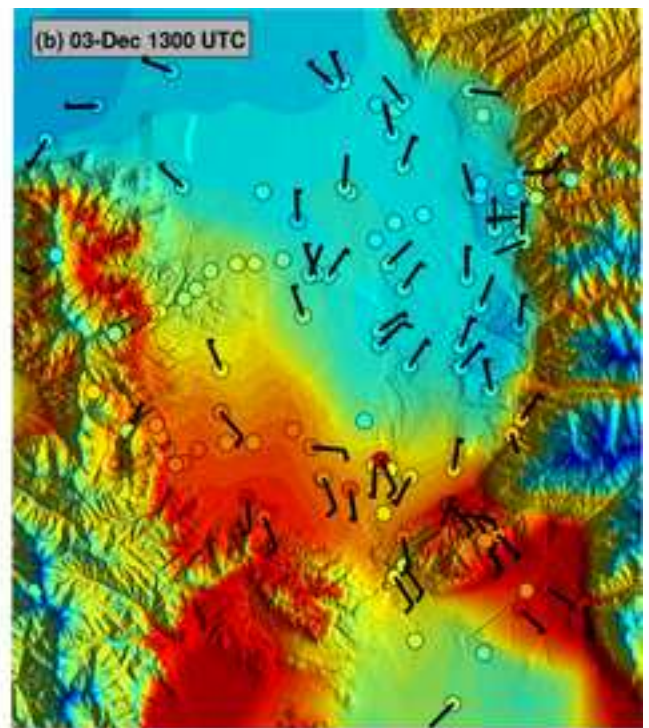
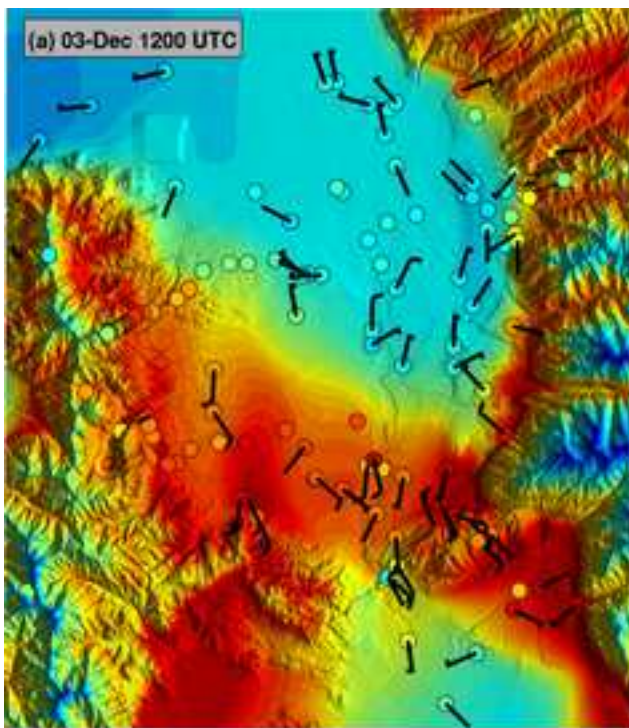
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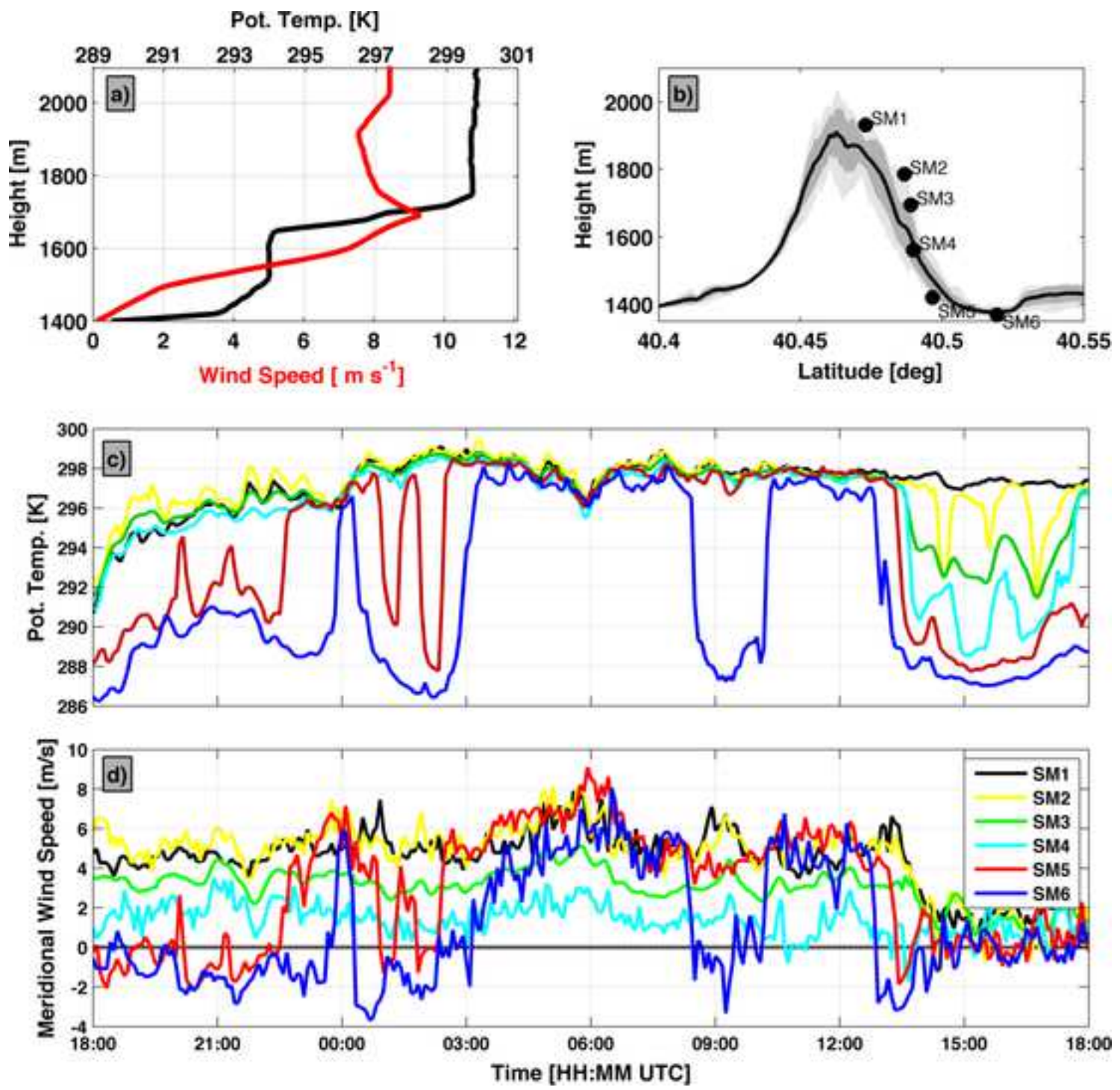
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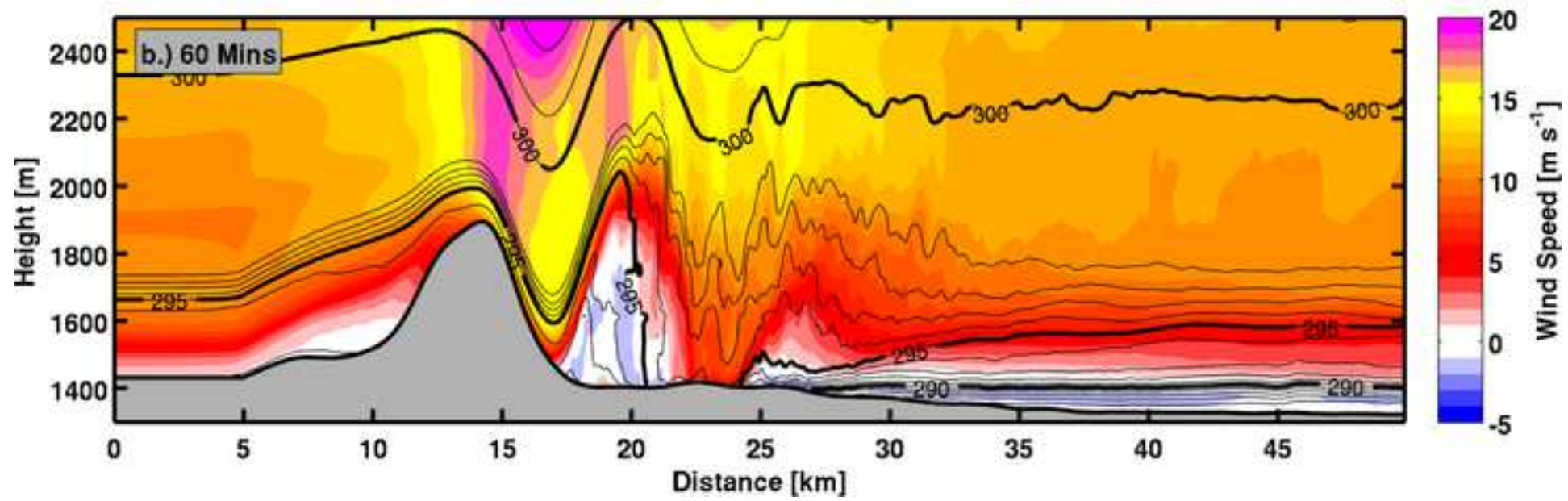
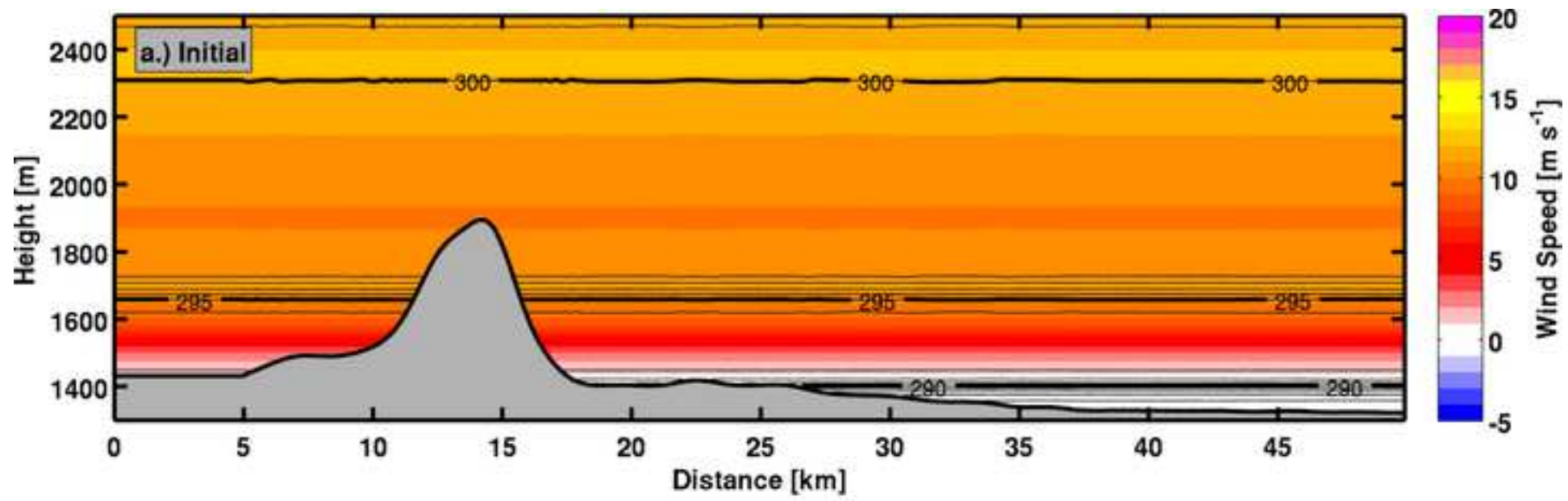
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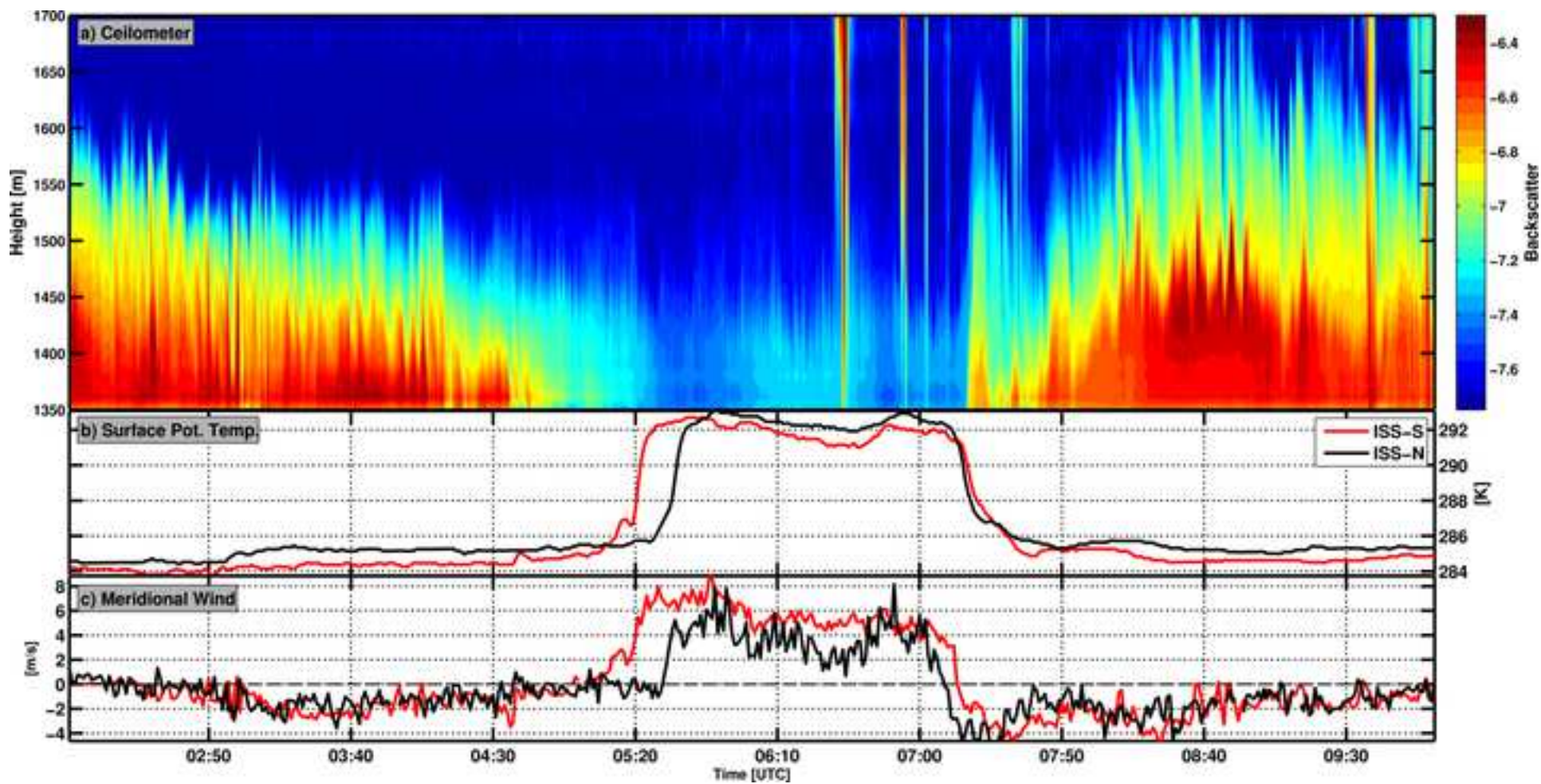
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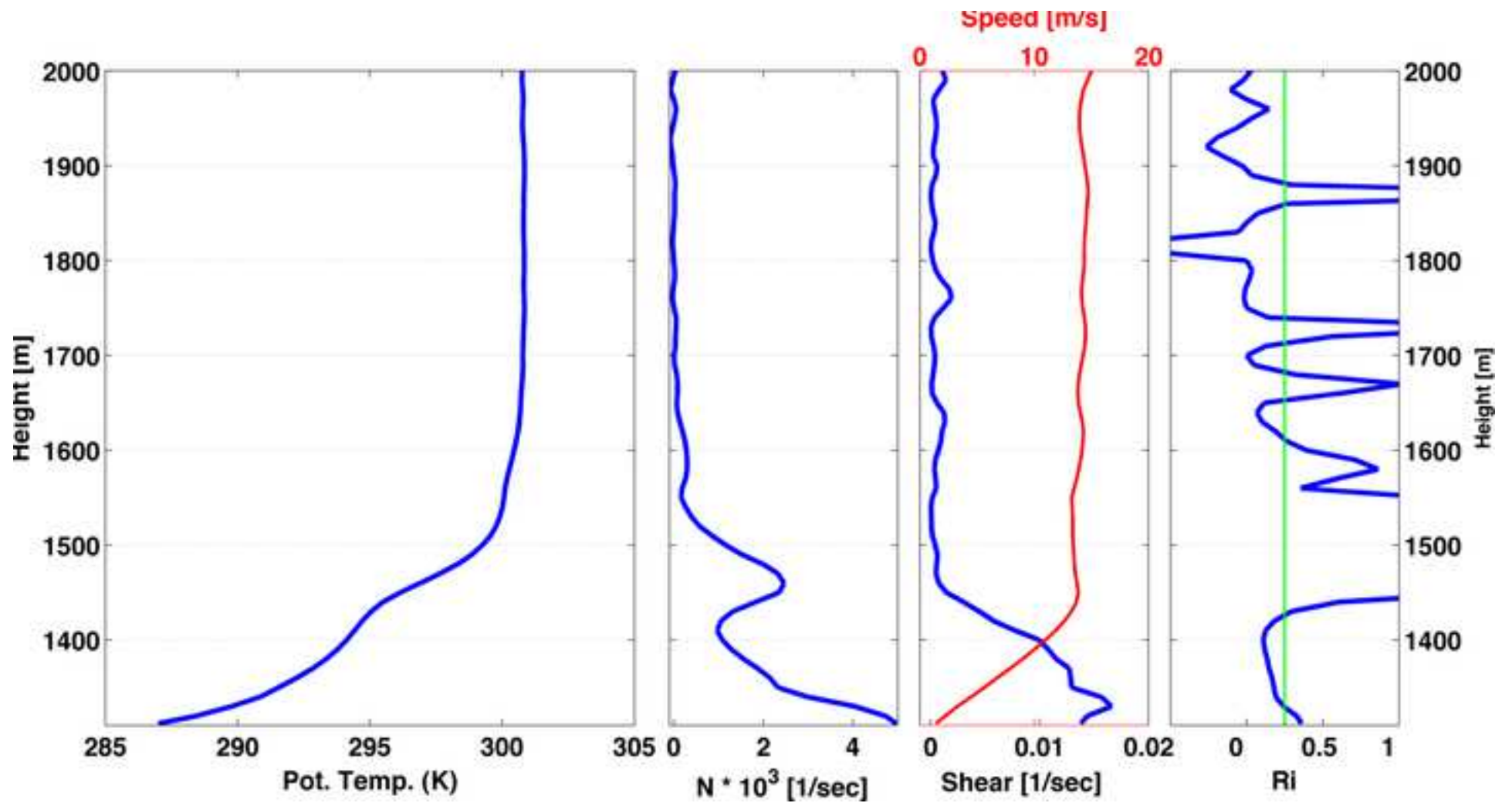
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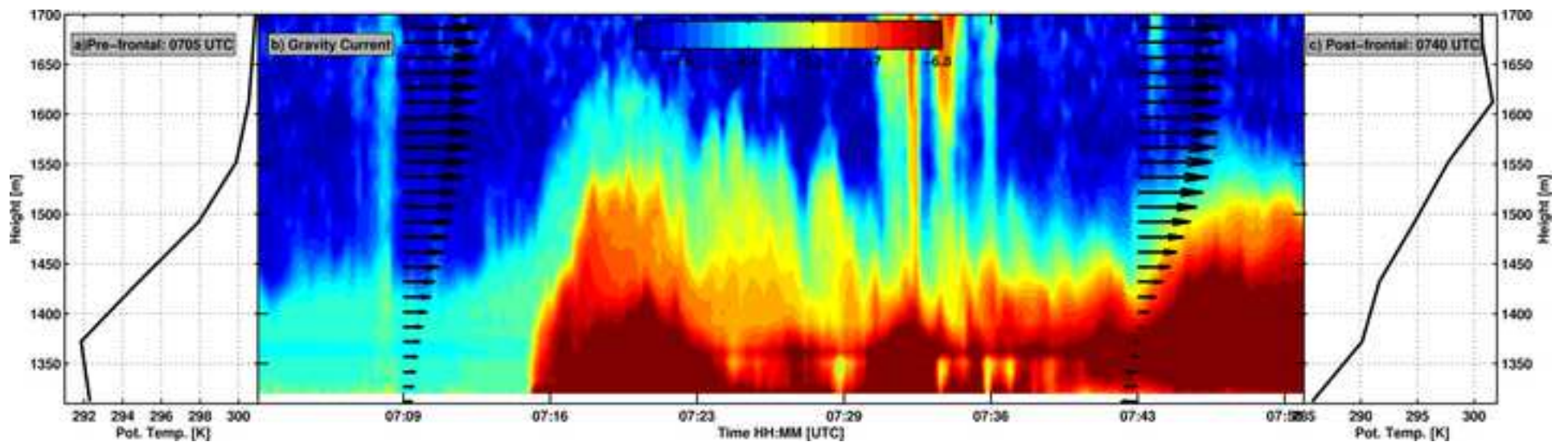
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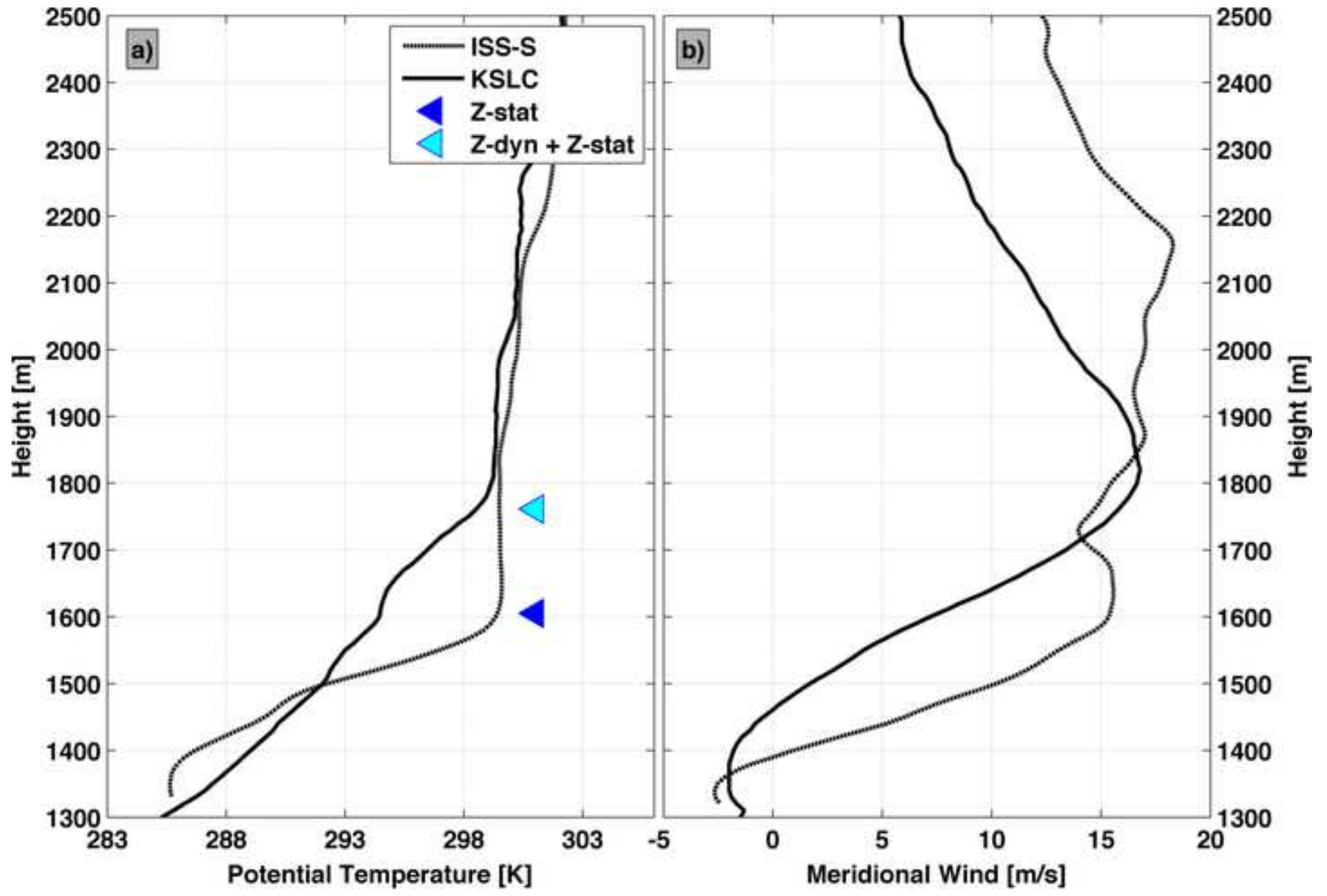
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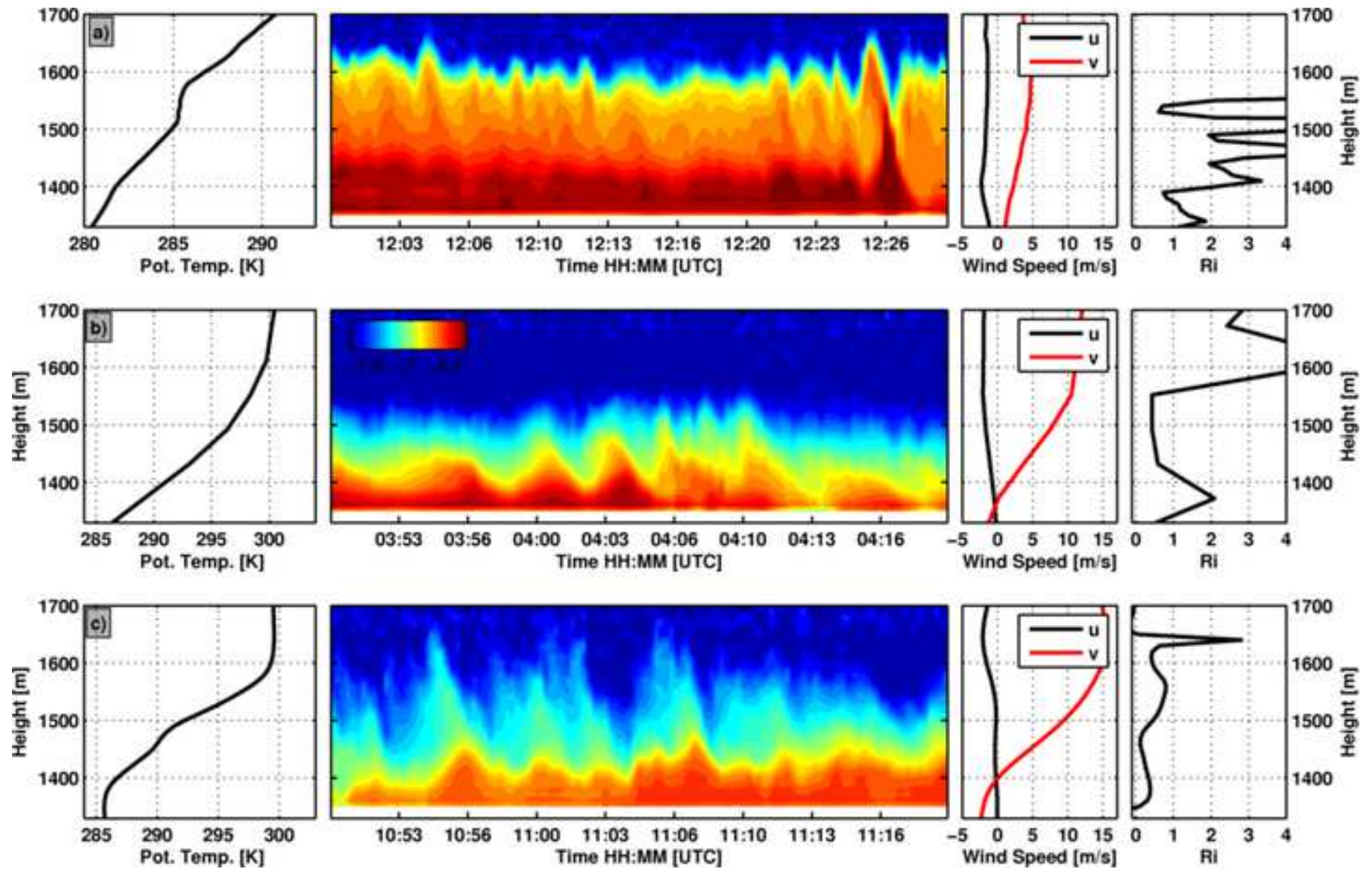
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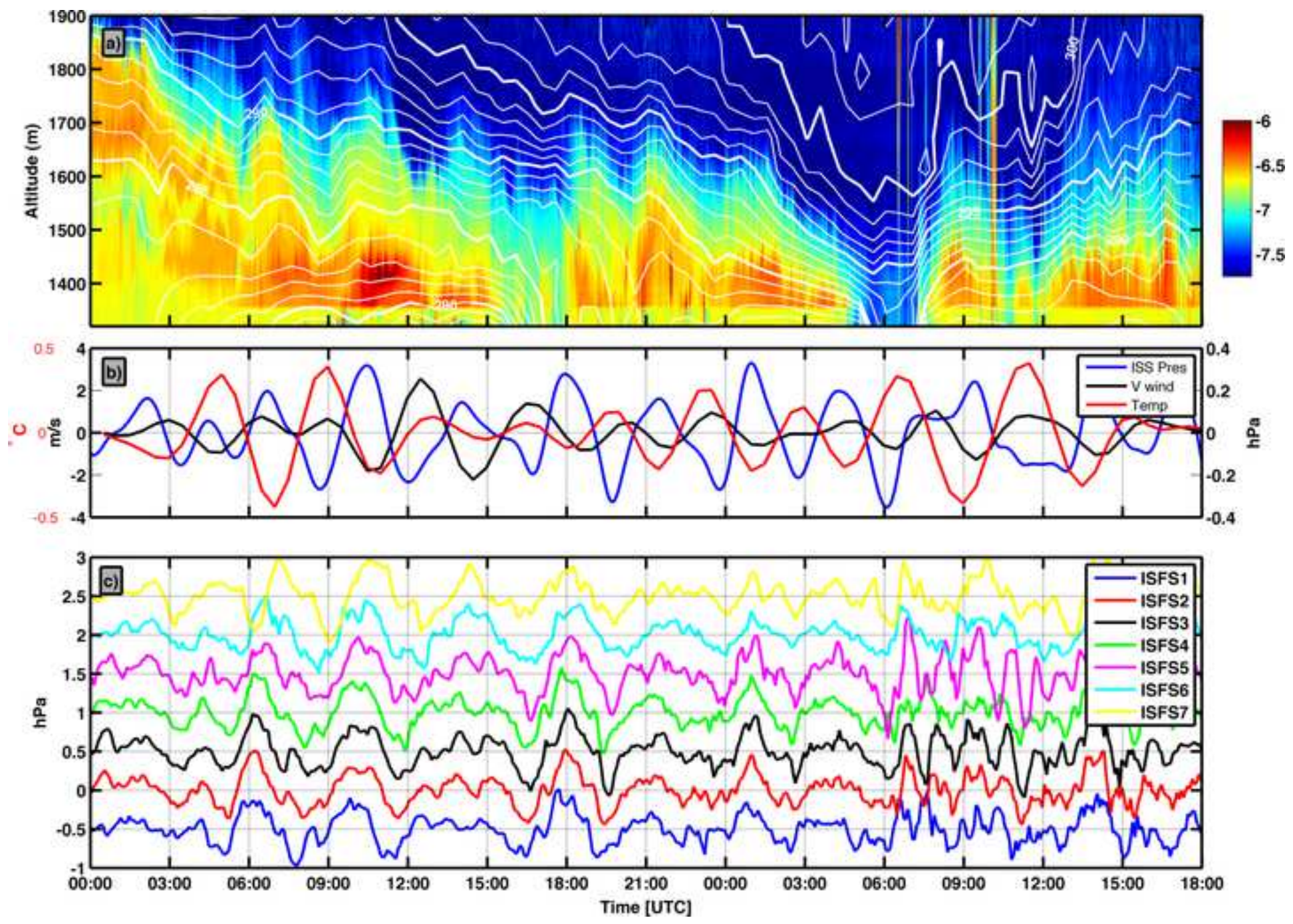
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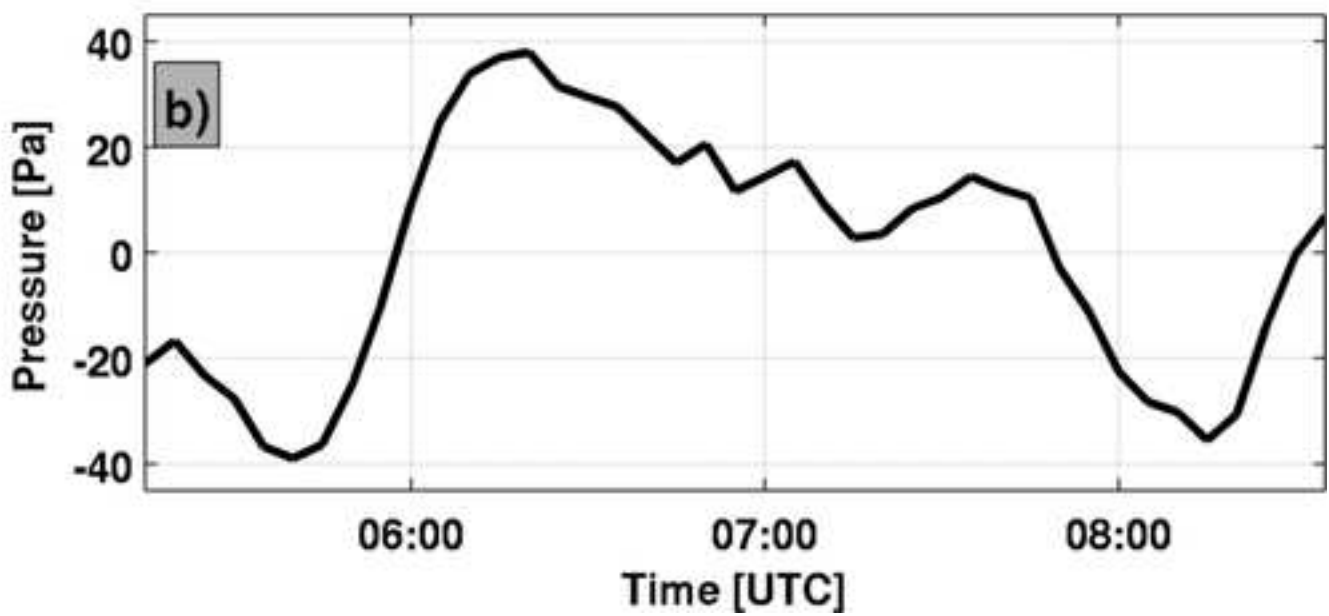
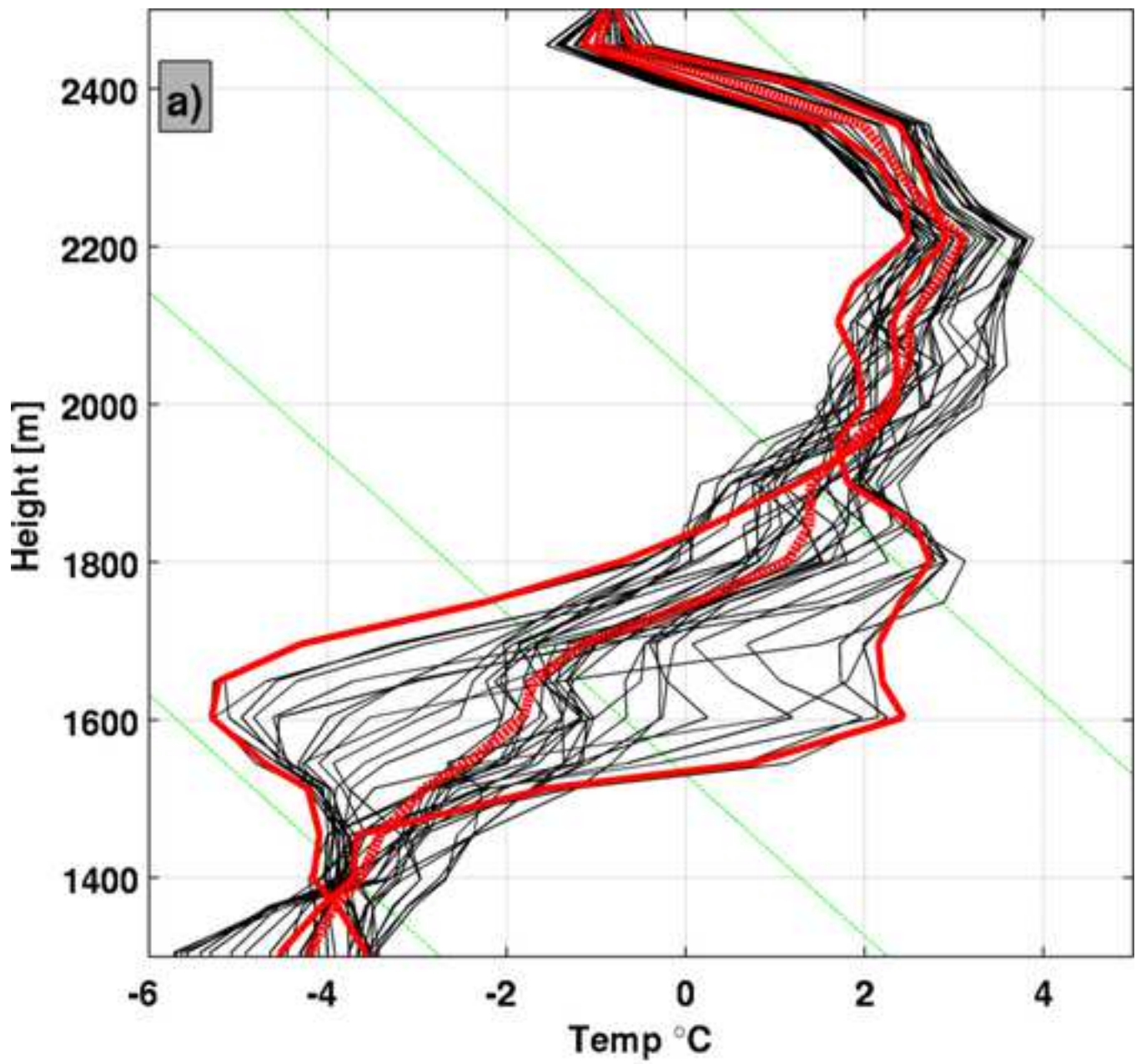
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